

# Image Matching via Saliency Region Correspondences

Alexander Toshev

Jianbo Shi

Kostas Daniilidis

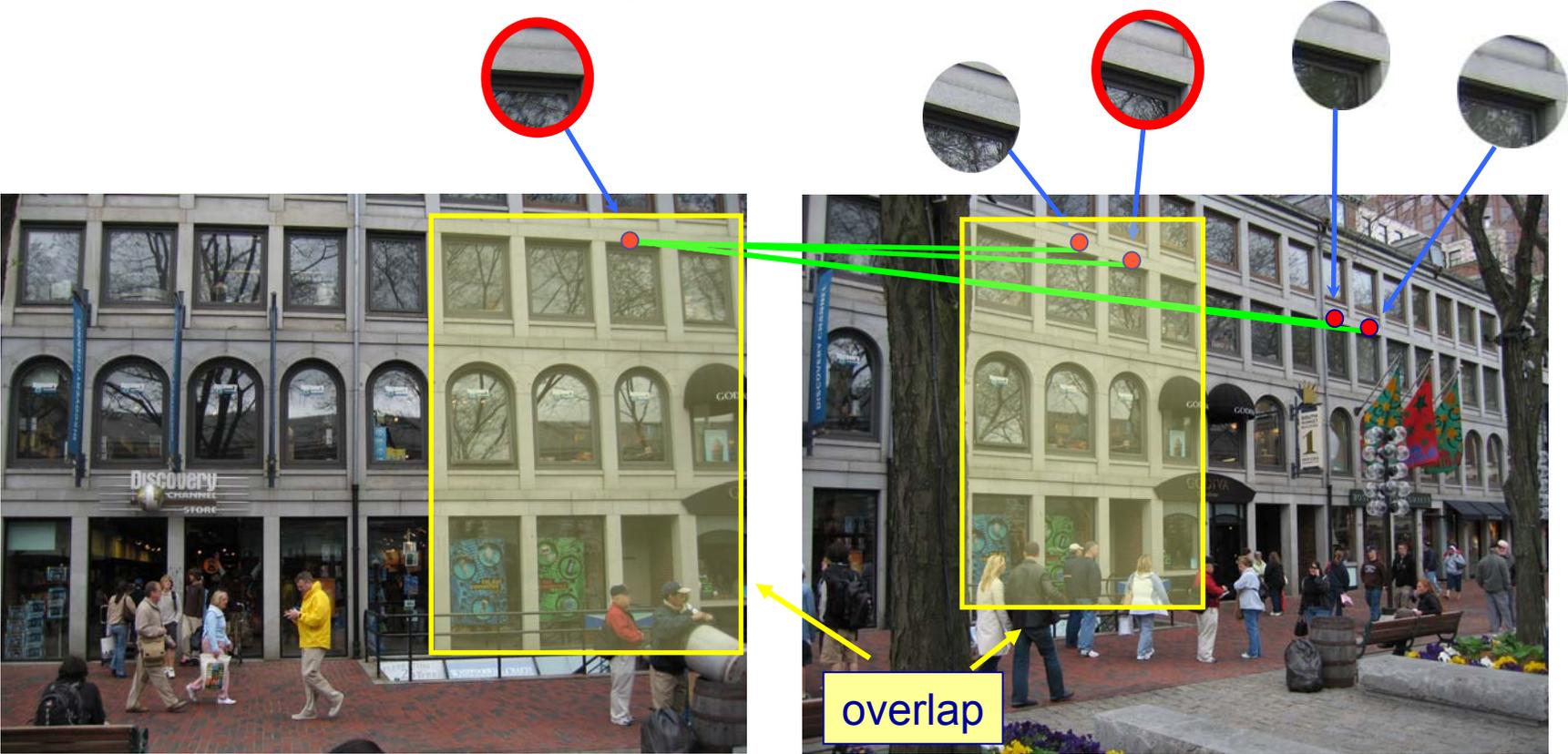
GRASP Laboratory  
University of Pennsylvania



# How to match two pictures with small overlap and repeated patterns?



# How to match two pictures with small overlap and repeated patterns?

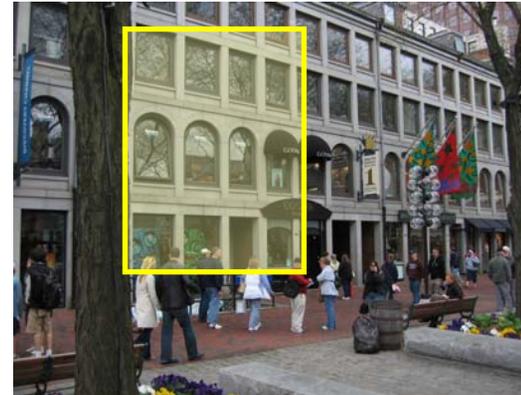


Most approaches assume large dominant overlaps

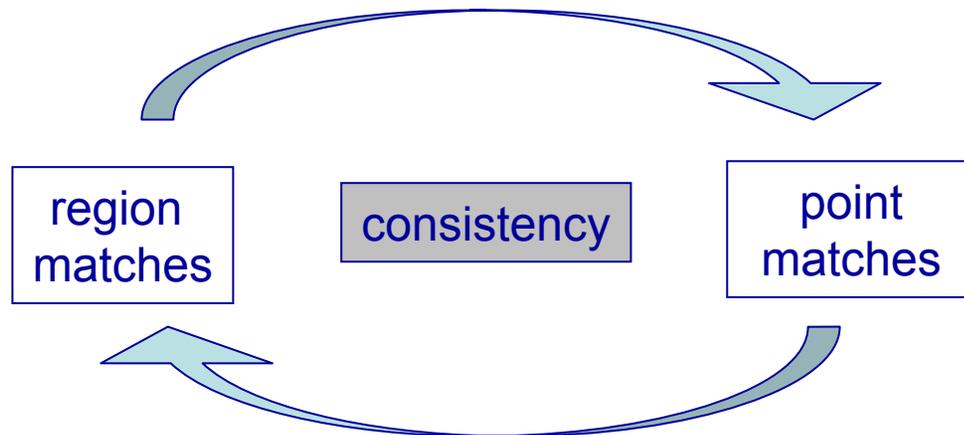
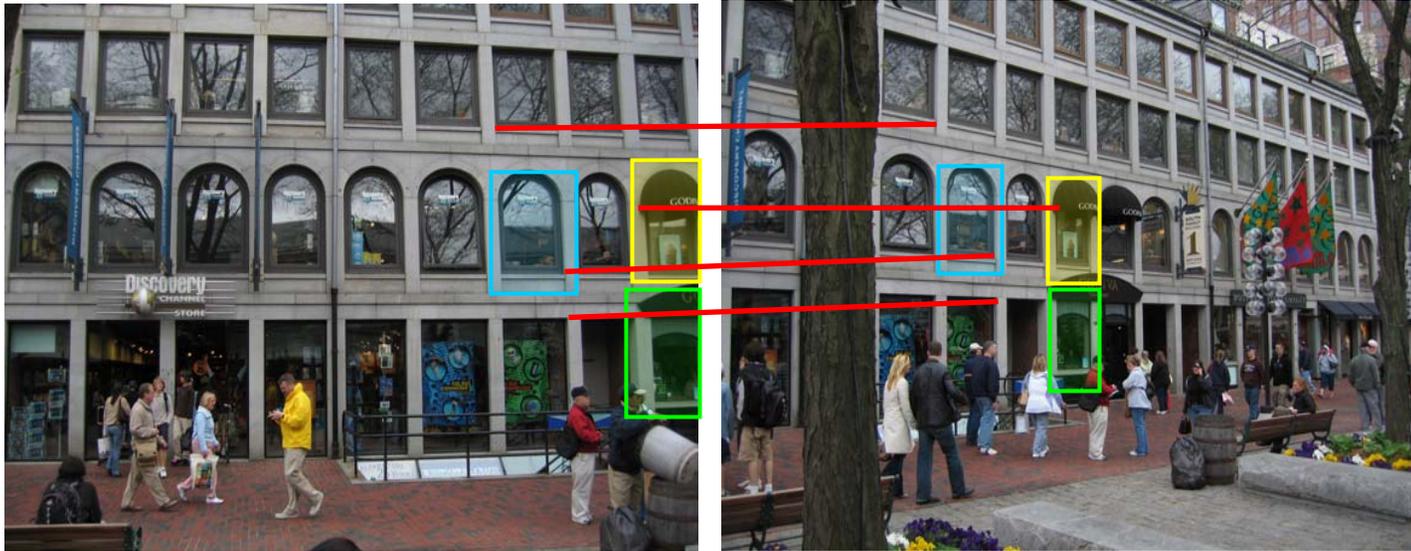


RANSAC needs **sufficient inlier portion** ( $> 30\%$ )  
and assumes a **model**.

Can we match without a model and still deal with small overlap?



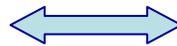
# Using Regions in Matching



# Interplay Between Region and Feature Matches

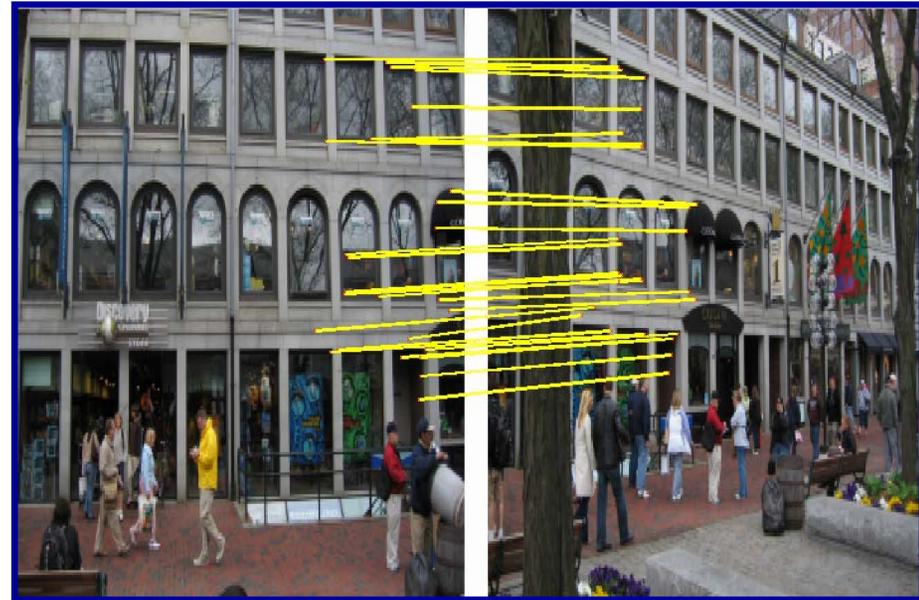


Propagation of feature matches  
to region matches



Restriction of feature matches  
only to ones relating matching  
regions

# Co-Salient Regions



## Goal 1:

Form **coherent image segments**

→ Intra-Image Similarity

## Goal 2:

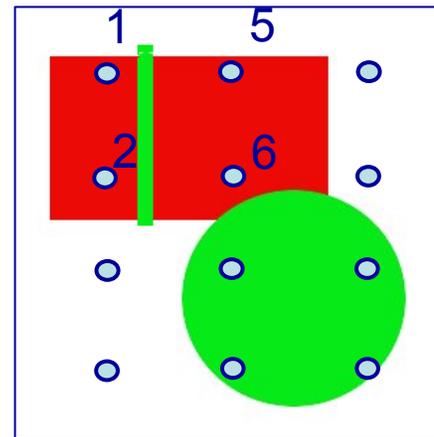
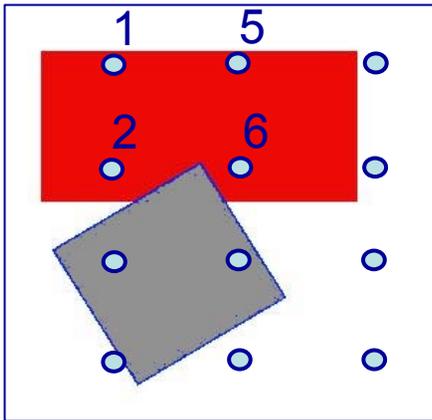
Exhibit strong feature **similarities**

**between the segments**

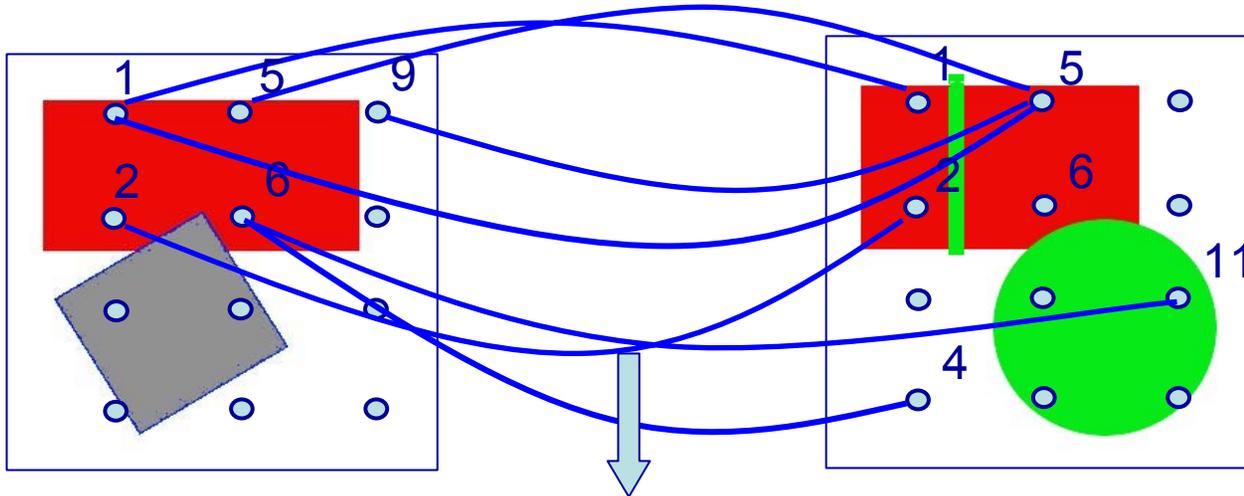
→ Inter-Image Similarity



# Image as a Graph



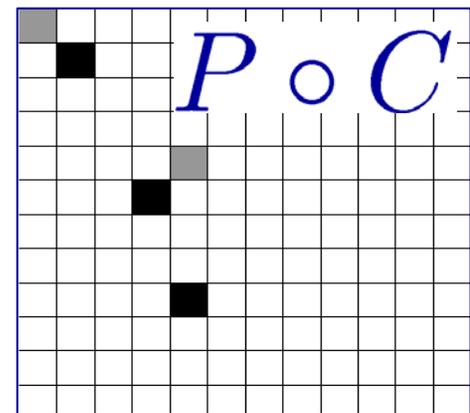
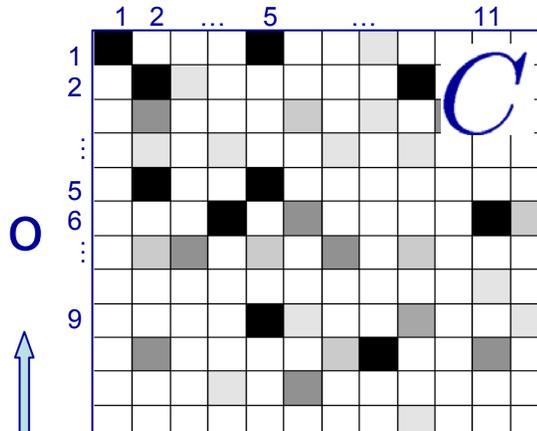
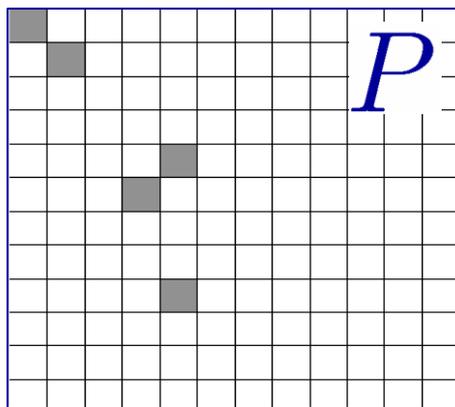
# Correspondence Matrix: $P \circ C$



selection matrix

matrix of measured correspondences

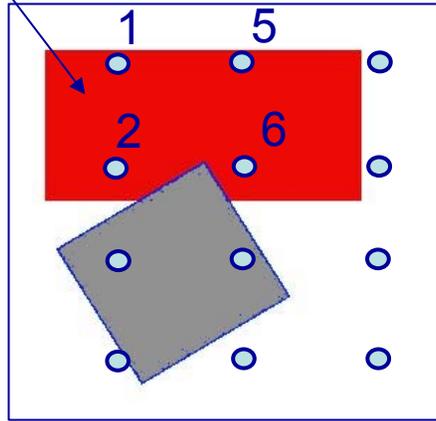
correspondence matrix



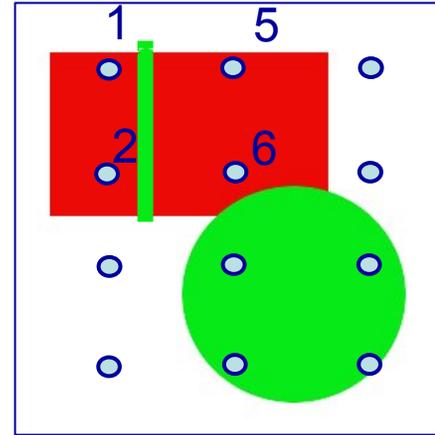
pointwise multiplication

# Segment Indicator Vectors

segment



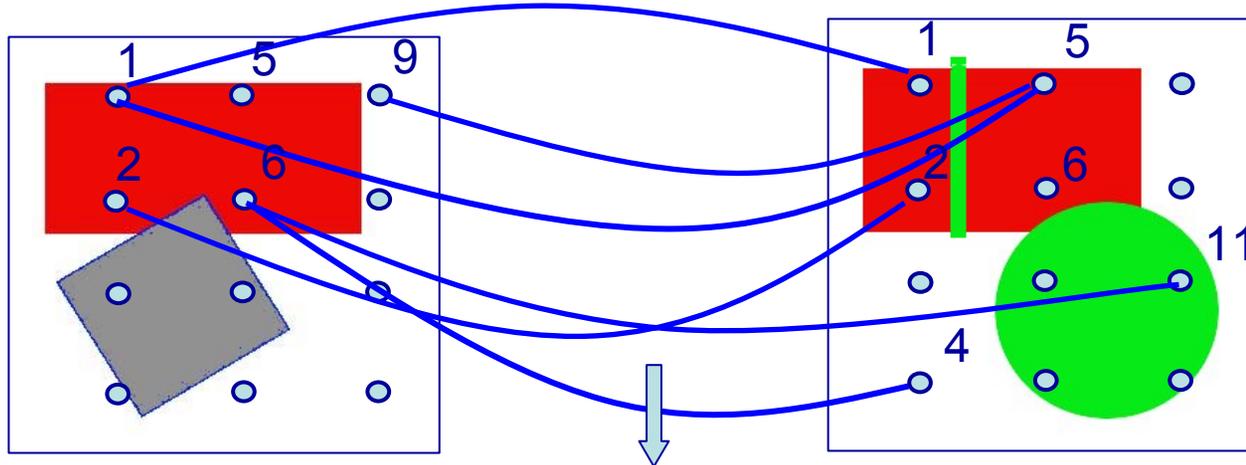
$V_1$



$V_2$



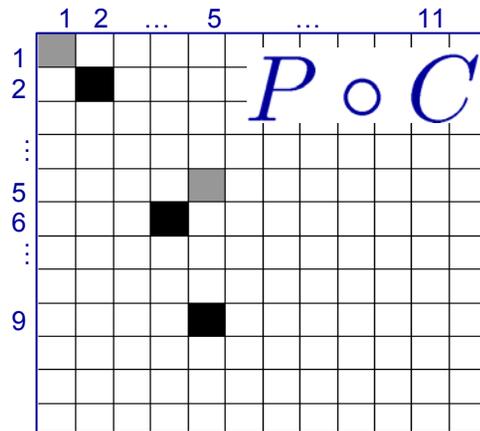
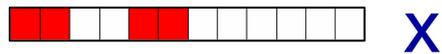
# Inter-Image Similarity



correspondence matrix

segment indicator vector

$V_1$

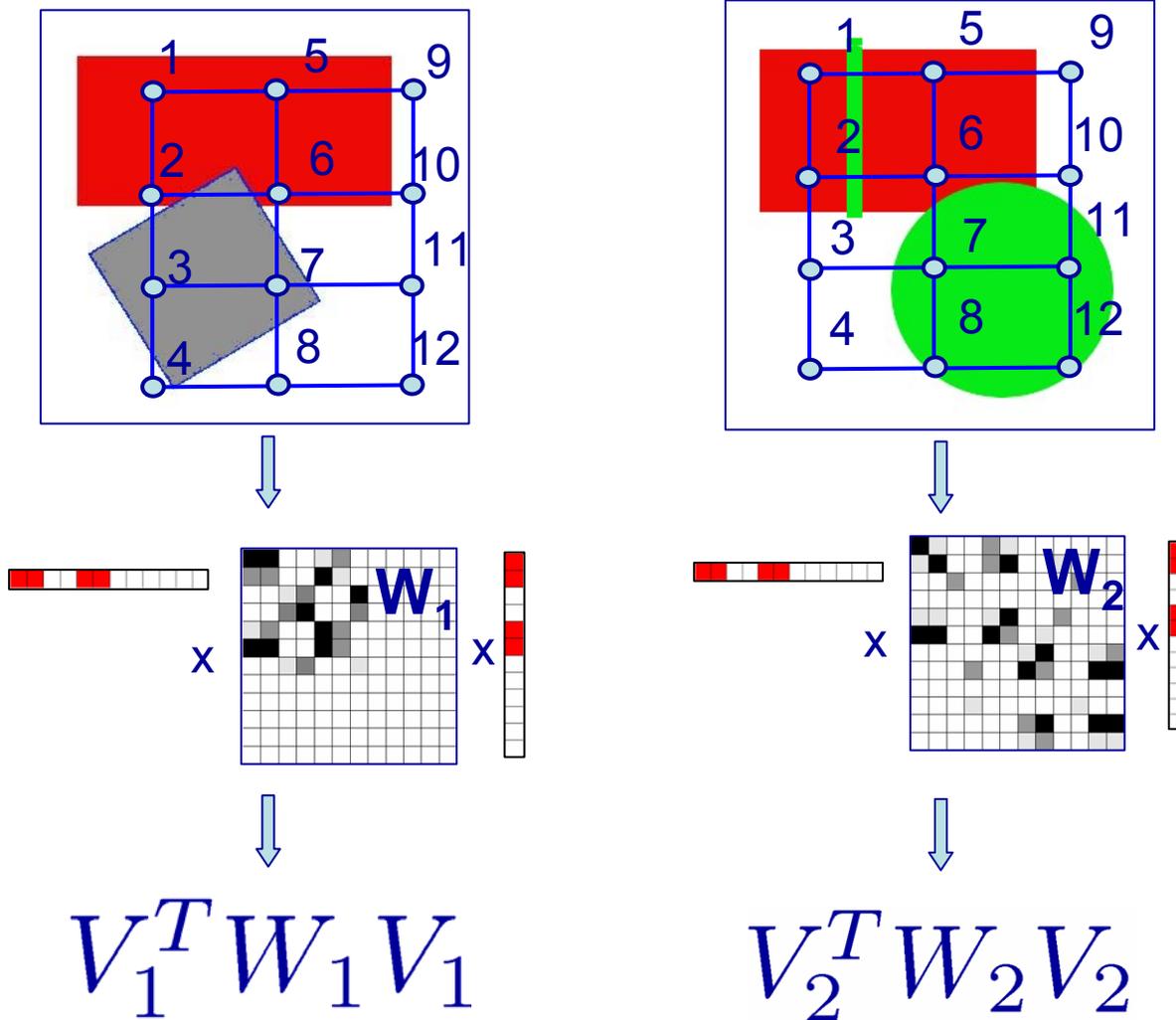


$V_2$

$$x \begin{matrix} \color{red}{\square} \\ \color{red}{\square} \\ \square \\ \square \\ \color{red}{\square} \\ \square \\ \square \\ \square \\ \square \\ \square \\ \square \end{matrix} = V_1^T (P \circ C) V_2$$

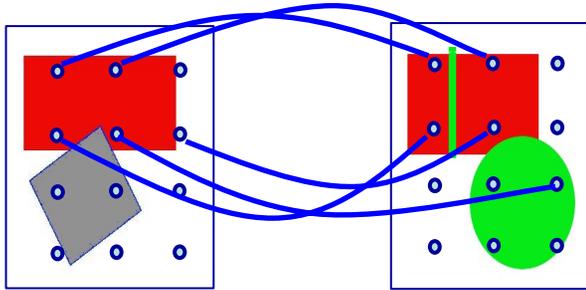


# Intra-Image Similarity

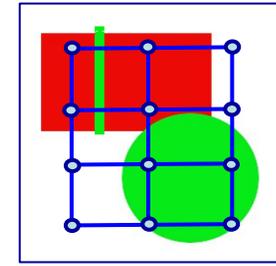
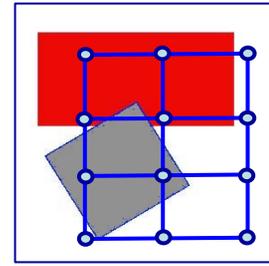


# Co-Salient Region Matching Score

inter-image similarity



intra-image similarities



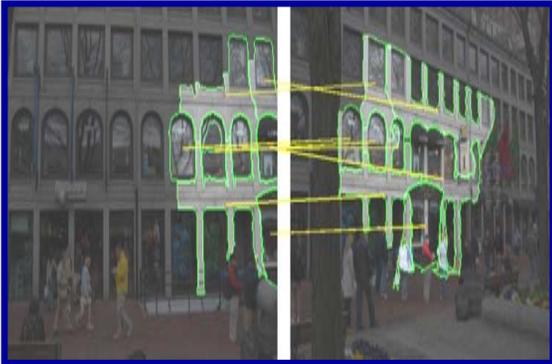
$$V_1^T (P \circ C) V_2 + V_1^T W_1 V_1 + V_2^T W_2 V_2 =$$

$$\text{tr} \left( V^T \begin{pmatrix} W_1 & (P \circ C) \\ (P \circ C)^T & W_2 \end{pmatrix} V \right) \text{ with } V = \begin{pmatrix} V_1 \\ V_2 \end{pmatrix}$$



# Co-Salient Region Matching Score

$$\text{Score}(V, P) = \text{tr} \left( V^T \begin{pmatrix} W_1 & (P \circ C) \\ (P \circ C)^T & W_2 \end{pmatrix} V \right)$$



## Goal 1:

**Matching co-salient regions:** find optimal  $\mathbf{V}$  for given initial selection  $\mathbf{P}$  of matches from  $\mathbf{C}$ .



## Goal 2:

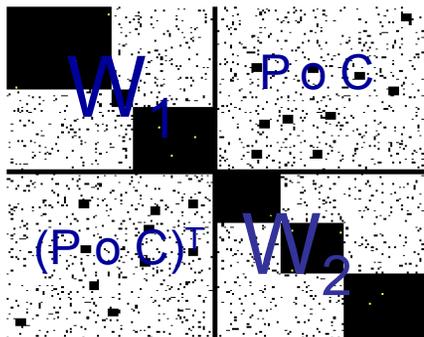
**Inlier selection for point matches:** find optimal selection matrix  $\mathbf{P}$  for given co-salient regions  $\mathbf{V}$ .



# Matching Co-Salient Regions I

$$\text{Maximize } \text{tr} \left( V^T \begin{pmatrix} W_1 & (P \circ C) \\ (P \circ C)^T & W_2 \end{pmatrix} V \right) \text{ w.r.t. } V$$

Naïve attempt – optimization with no restrictions on  $V$  **fails!**



$(P \circ C)$  is much sparser than  $W_1$  and  $W_2$

Intra-image similarities dominate score function



$$\text{Score} = V_1^T (P \circ C) V_2 + V_1^T W_1 V_1 + V_2^T W_2 V_2$$



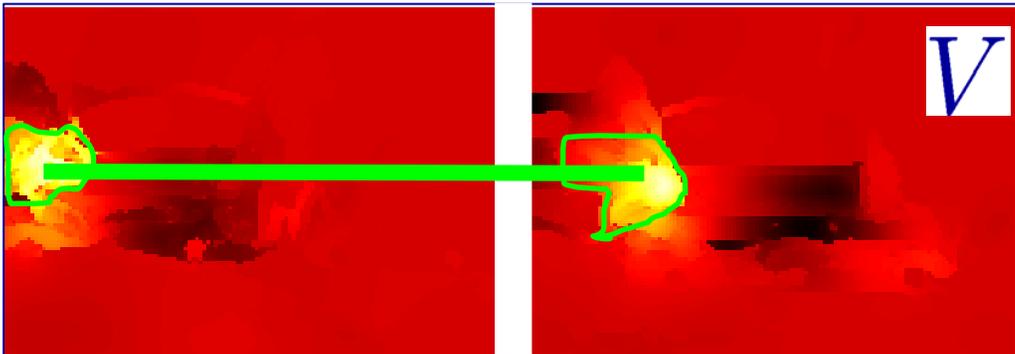


# Matching Co-Salient Regions III

$$\text{Maximize } \text{tr} \left( V^T \begin{pmatrix} W_1 & (P \circ C) \\ (P \circ C)^T & W_2 \end{pmatrix} V \right) \text{ for } V = SA$$



Restrict co-salient regions to a space of dominant segmentation modes

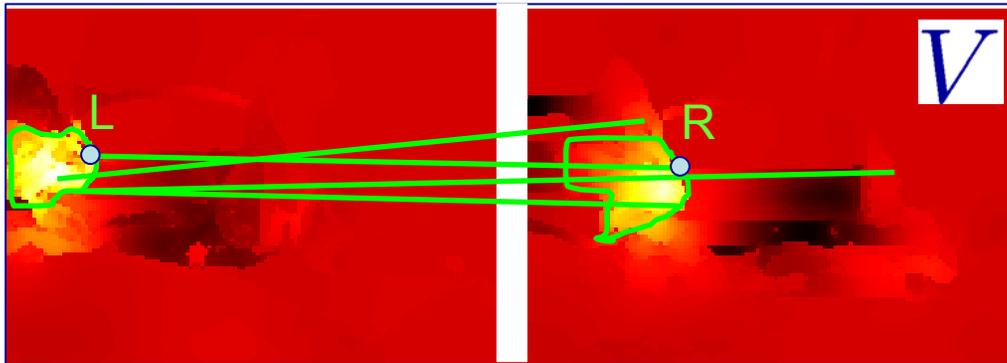


The subspace restriction enables

- **clear matches** of co-salient regions
- **propagation** of feature matches to region matches

# Inlier Selection

$$\text{Maximize } \text{tr} \left( V^T \begin{pmatrix} W_1 & P_{inlier} \circ C \\ (P_{inlier} \circ C)^T & W_2 \end{pmatrix} V \right) \text{ w.r.t. } P_{inlier}$$



Such that:

- $P_{inlier} \subset P$
- Consistency with region matches



Linear Programming

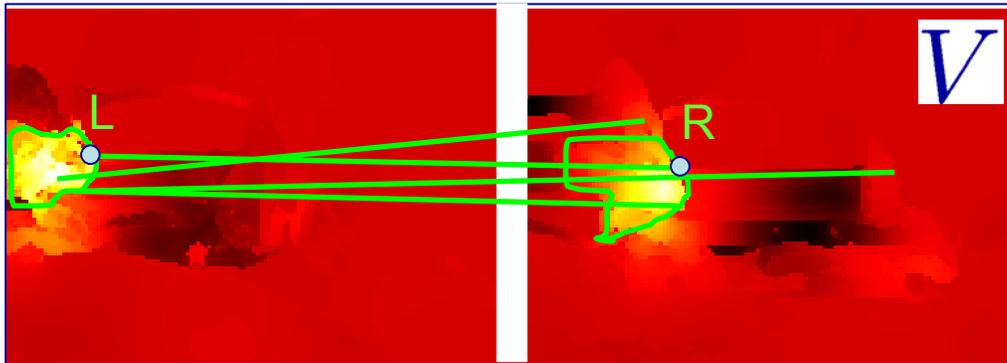
$$P_{inlier} \circ C \leftarrow (P \circ C) \circ V_1 V_2^T$$

$$\begin{pmatrix} \cdot \\ \cdot V_{1,L} \cdot V_{2,R} \cdot \\ \cdot \end{pmatrix}$$



# Inlier Selection

$$\text{Maximize } \text{tr} \left( V^T \begin{pmatrix} W_1 & P_{inlier} \circ C \\ (P_{inlier} \circ C)^T & W_2 \end{pmatrix} V \right) \text{ w.r.t. } P_{inlier}$$



Such that:

- $P_{inlier} \subset P$
- Consistency with region matches



Linear Programming



$$P_{inlier} \circ C \leftarrow (P \circ C) \circ V_1 V_2^T$$

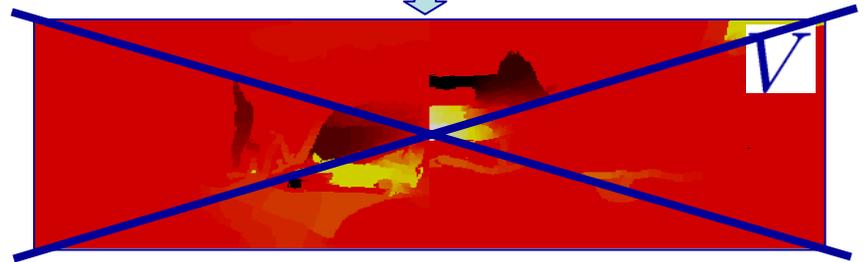
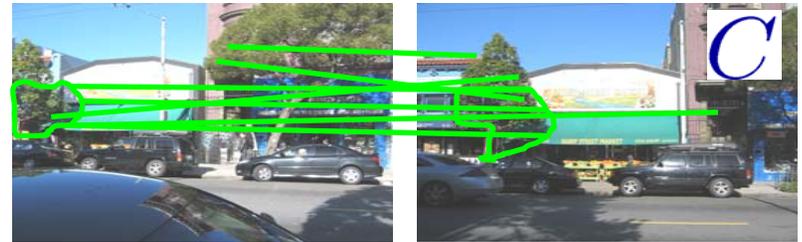
$P_{inlier}$  is consistent with co-salient region matches  $V$



# Inlier Selection – Dense Set of Matches

How can we obtain a dense set of correspondences?

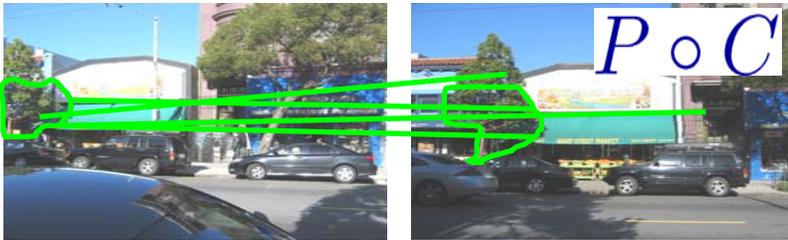
set of **all** matches



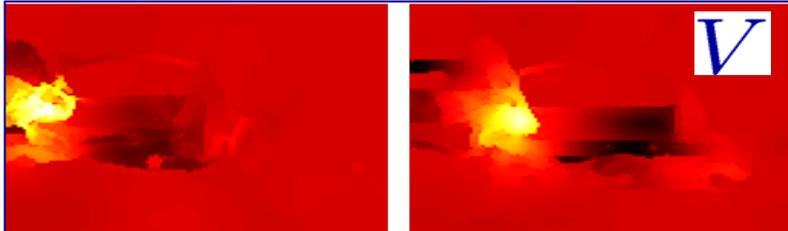
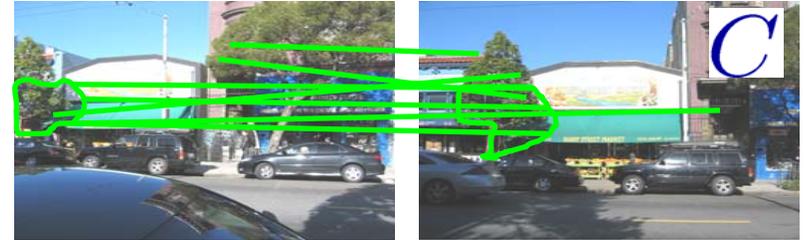
# Inlier Selection – Dense Set of Matches

How can we obtain a dense set of correspondences?

initial sparse set of matches



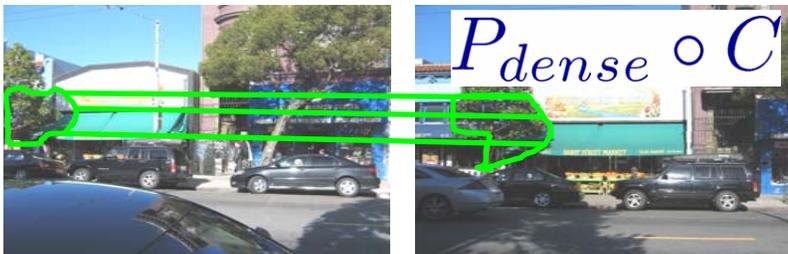
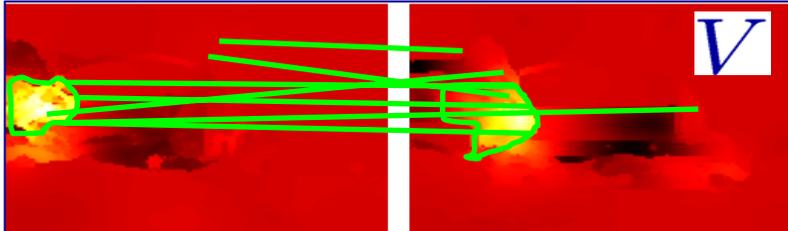
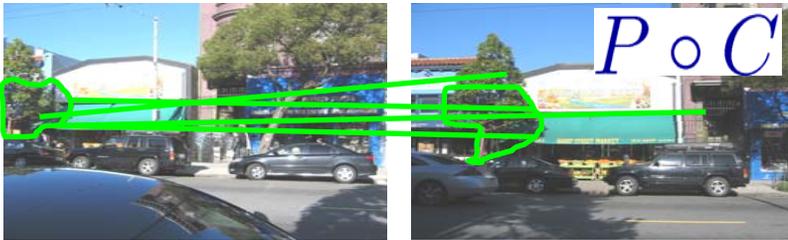
set of **all** matches



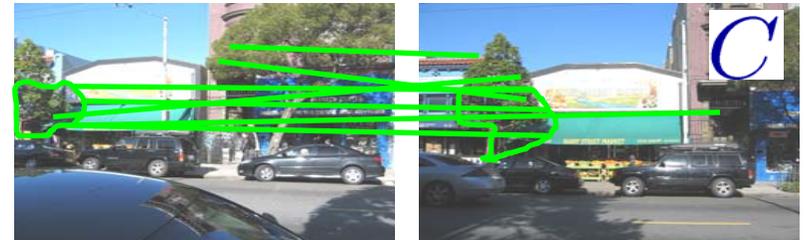
# Inlier Selection – Dense Set of Matches

How can we obtain a dense set of correspondences?

initial sparse set of matches



set of **all** matches



$$C \circ V_1 V_2^T$$

Selection of feature matches from  $C$  based on co-salient region matches  $V$ .



# Algorithm



For given input images

- compute segmentation spaces  $S$



# Algorithm



↓ select P



For given input images

- compute segmentation spaces  $S$
- compute feature matches  $C, P$

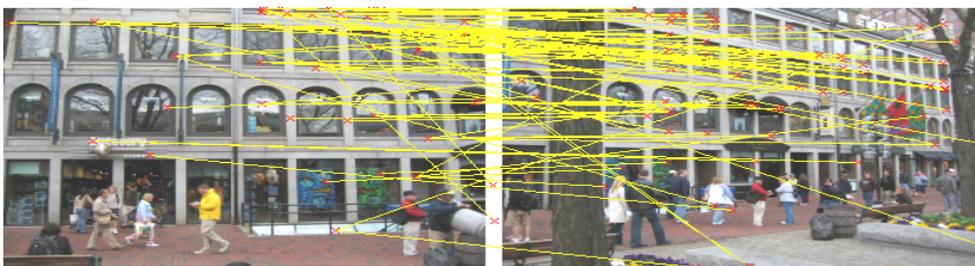
# Algorithm

For given input images

- compute segmentation spaces  $S$
- compute feature matches  $C, P$
- detect co-salient region



↓ select  $P$



↓ solve for  $V$



# Algorithm



↓ select  $P$



↓ solve for  $V$



For given input images

- compute segmentation spaces  $S$
- compute feature matches  $C, P$
- detect co-salient region
- select inliers

solve for  
 $P \circ C$



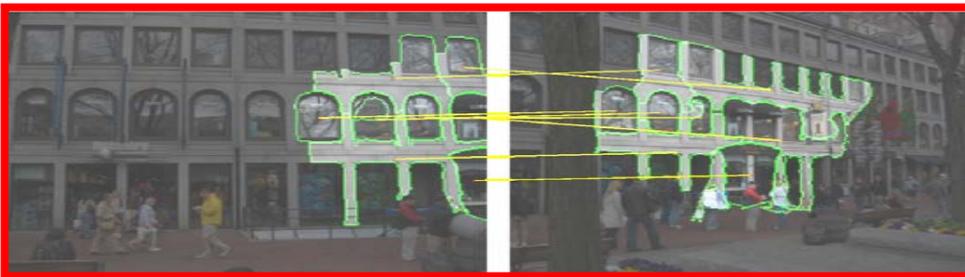
# Algorithm



↓ select  $P$



↓ solve for  $V$



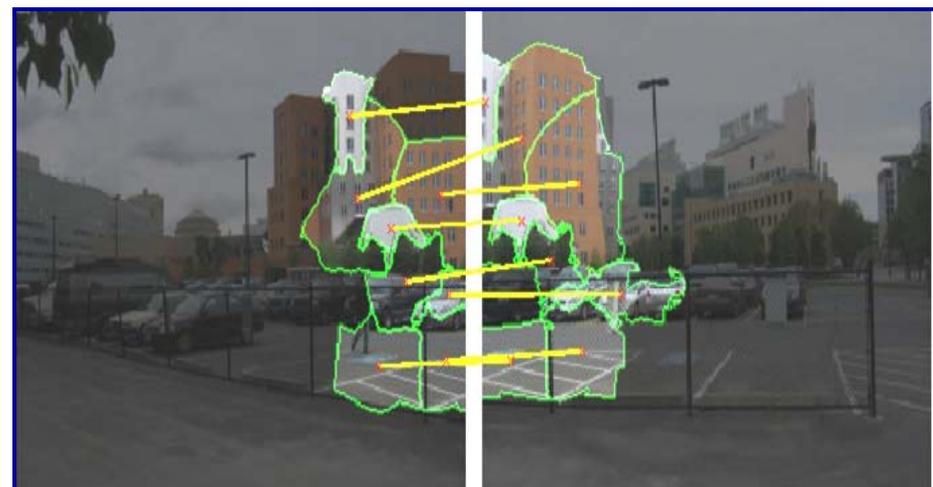
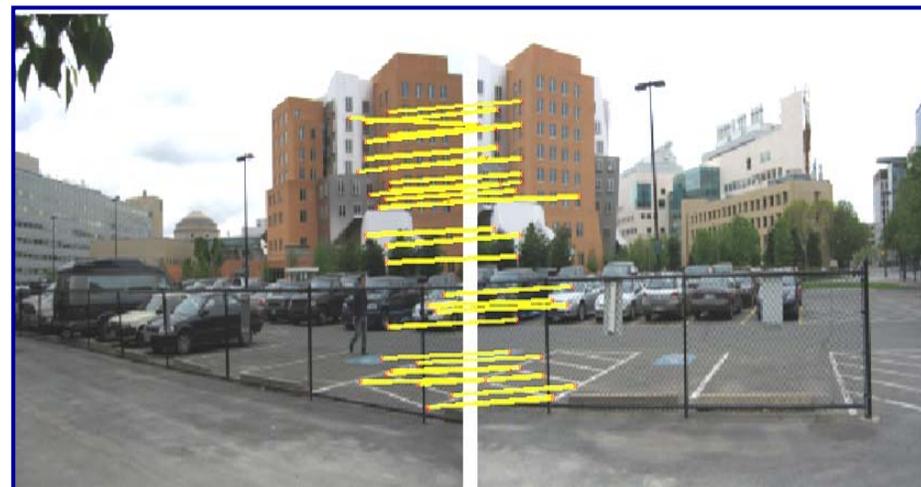
For given input images

- compute segmentation spaces  $S$
- compute feature matches  $C, P$
- detect co-salient region
- select inliers
- goto step 3

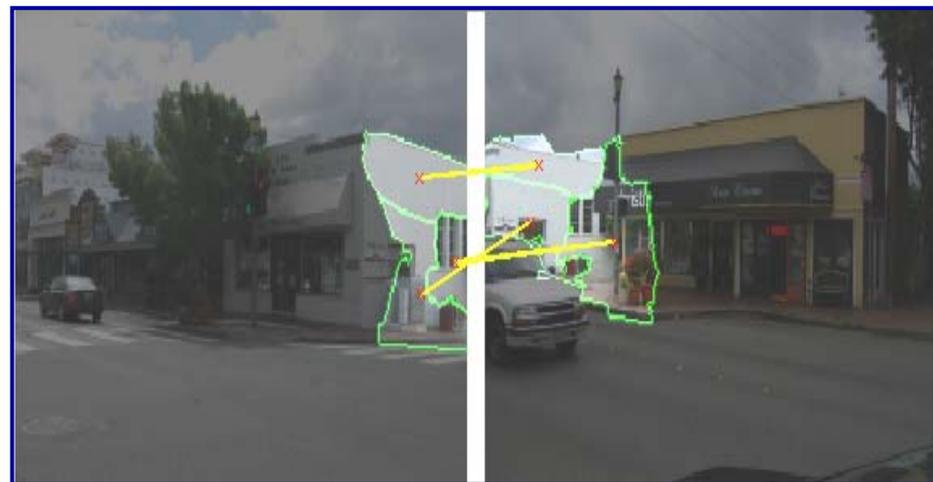
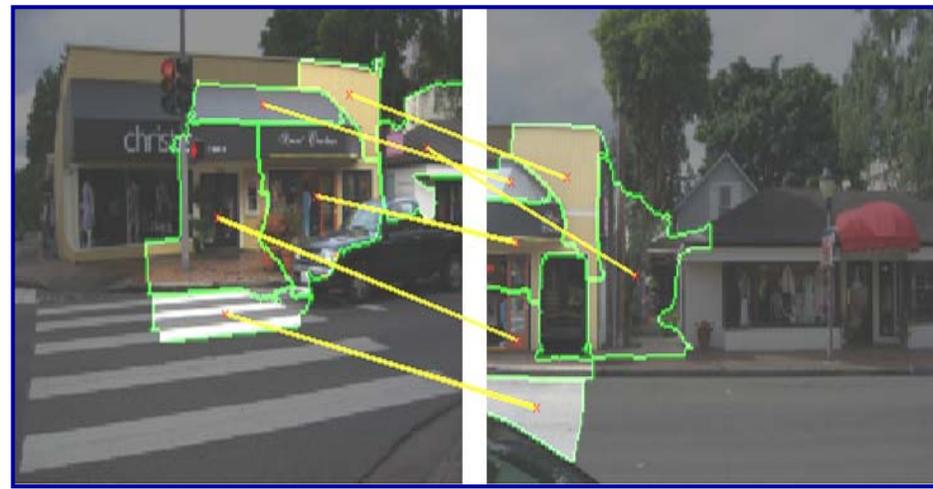
↶ solve for  
 $P \circ C$



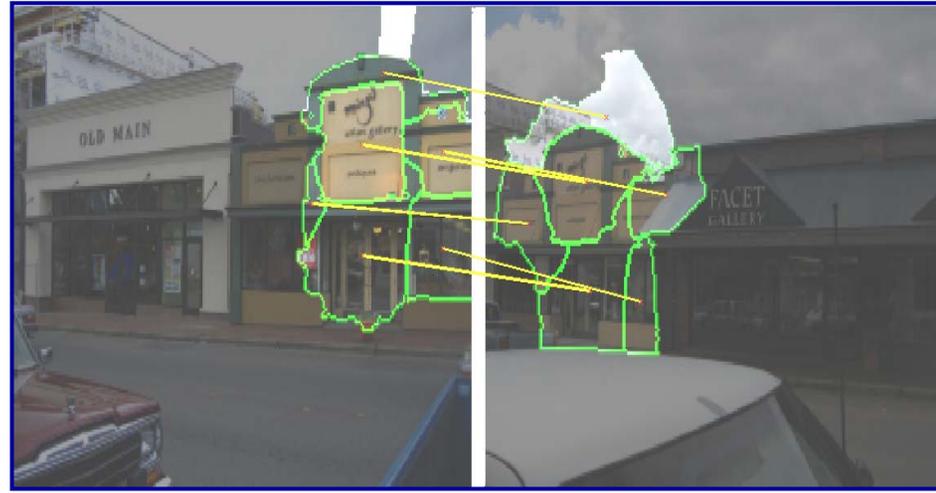
# Results



# Results



# Results



# Results

Where am I?

query:



[ICCV 2005 CV Contest]

accuracy rate of point matches

matches ranked among	initial P	$P_{dense}$
1 – 30	19%	75%
31 - 60	12%	52%
60 - 90	15%	44%

accuracy rate of query results

dataset	accuracy of best match	Accuracy of top 2 matches
Final 5	95%	95%
Test 4	90%	85%



# Thank You!

## Questions?

