

LGIC 010 & PHIL 005

Problem Set 9

Spring Term, 2012

For each of the following pairs consisting of a set of schemata  $X$  and a schema  $S$  determine whether  $X$  implies  $S$ . If so, provide a deduction to establish the implication. If not, specify a structure which makes  $S$  false and all the schemata in  $X$  true.

1.  $X : \{(\forall x)Rxx, \neg(\forall x)(\forall y)Rxy\}$   
 $S : \neg(\exists x)(\forall y)x = y$
2.  $X : \{(\exists x)(\forall y)Lxy\}$   
 $S : (\forall x)(\exists y)Lxy$
3.  $X : \{(\forall x)(\exists y)Lxy\}$   
 $S : (\exists x)(\forall y)Lxy$
4.  $X : \{(\forall x)(Fx \supset (\exists y)(\neg Fy \wedge (\forall z)(Rxz \equiv z = y))),$   
 $(\forall x)(\neg Fx \supset (\exists y)(Fy \wedge (\forall z)(Rzx \equiv z = y))),$   
 $(\forall x)(\forall y)(\forall z)((Pxy \wedge Pxz) \supset y = z), (\forall x)(\exists y)(Fy \wedge Pyx)\}$   
 $S : p \wedge \neg p$
5.  $X : \{(\exists x)Fx \wedge (\forall x)(\forall y)((Fx \wedge Fy) \supset x = y)\}$   
 $S : (\exists x)(\forall y)(Fy \equiv x = y)$