LGIC 010 & PHIL 005 Problem Set 4 Spring Term, 2017 DUE IN CLASS MONDAY, FEBRUARY 20

For the purposes of this problem set, we restrict attention to pure monadic quantificational schemata all of whose predicate letters are among F and G, and to structures which interpret exactly these predicate letters. We employ the following terminology in the problems below.

- A list of pure monadic schemata is *succinct* if and only if no two schemata on the list are equivalent.
- A pure monadic schema *implies a list of schemata* if and only if it implies every schema on the list.
- The *power* of a pure monadic schema is the length of a longest succinct list of pure monadic schemata it implies.
- If X is a finite set, we write |X| for the number of members of X.
- If S is a schema, we write mod(S, n) for the set of structures A such that $A \models S$ and $U^A = \{1, \ldots, n\}.$
- 1. (25 points) What is the length of a longest succinct list of schemata none of which imply the schema $(\exists x)(Fx \land Gx)$?
- 2. (25 points) What is the length of a longest succinct list of schemata all of which have power strictly less than the power of $(\forall x)(Fx \land Gx)$?
- 3. (25 points) What is the length of a longest succinct list of schemata S such that |mod(S, 4)| = 24?
- 4. (25 points) Suppose that a schema S satisfies the following properties.
 - |mod(S, 3)| = 0.
 - $|\mathsf{mod}(\mathsf{S},\mathsf{10})| \neq 0.$

Are these properties adequate to determine the power of S? If not, explain why. If so, what is the power of S?