

LGIC 010 & PHIL 005

Problem Set 3

Spring Term, 2012

1. (25 points) How many structures with universe of discourse $\{1, 2\}$ interpreting only the monadic predicate letters “ F ” and “ G ” make true the schema

$$(\forall x)(Fx \vee Gx).$$

2. (25 points) Write down a satisfiable schema involving only the monadic predicate letters “ F ,” “ G ” and “ H ,” which is satisfied by no structure with universe of discourse $\{1, 2, 3, 4\}$.

3. (25 points) How many structures with universe of discourse $\{1, \dots, 10\}$ interpreting only the monadic predicate letters “ F ” and “ G ” make true the schema

$$(\exists x)Fx \equiv (\exists x)Gx.$$

4. (25 points) How many structures with universe of discourse $\{1, \dots, 10\}$ interpreting only the monadic predicate letters “ F ” and “ G ” make true the schema

$$(\exists x)(Fx \equiv Gx).$$