

LGIC 010 & PHIL 005

Problem Set 1

Spring Term, 2012

1. (33 points) Test the following schemata for validity.

(a) $(p \equiv q) \vee (p \equiv r) \vee (q \equiv r)$

(b) $(p \supset q) \vee (q \supset p)$

(c) $(p \oplus (q \oplus r)) \equiv ((p \oplus q) \oplus r)$ (Recall that " \oplus " represents exclusive disjunction.)

2. (55 points) In each case, determine whether the first schema implies the second.

(a) $(p \oplus r) \equiv (q \oplus r) \quad p \equiv q$

(b) $(p \oplus (q \equiv r)) \quad ((p \oplus q) \equiv (p \oplus r))$

(c) $(q \supset p) \quad (\neg p \supset \neg q)$

(d) $(p \wedge q) \vee r \quad p \wedge (q \vee r)$

(e) $p \wedge (q \vee r) \quad (p \wedge q) \vee r$

3. (12 points) How many truth assignments to the six sentence letters p_1, \dots, p_6 satisfy the following schema?

$$(((p_1 \oplus p_2) \oplus p_3) \oplus p_4) \vee (p_5 \wedge p_6)$$