## Preview of Lecture 02.29

On 02.29, we will count the number of finite structures with universe of discourse  $\{1, \ldots, n\}$  that satisfy various conditions. We have already noted that there are  $2^{n^2}$  graphs and  $2^{\binom{n}{2}}$  simple graphs with universe of discourse  $\{1, \ldots, n\}$ . We will begin by showing that

- $|\mathsf{mod}(\mathsf{Fun}, n)| = n^n;$
- $|\mathsf{mod}((\mathsf{Fun} \land \mathsf{Inj}), n)| = n!;$
- $|\mathsf{mod}(\mathsf{Tour}, n)| = 2^{\binom{n}{2}};$
- $|\mathsf{mod}(\mathsf{SLO}, n)| = n!;$
- $|\mathsf{mod}(\mathsf{Bfun}, n)| = n^{n^2}$ .

We will then explore several classes of infinite strict linear orders and finite simple graphs, and, in the latter case, address further counting problems.