Verification of Distributed Protocols Using Decidable Logic

Sharon Shoham

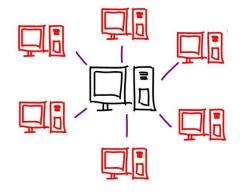
Programming Languages Mentoring Workshop 2019



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Why verify distributed protocols?

- Distributed systems are everywhere
 - Safety-critical systems
 - Cloud infrastructure
 - Blockchains



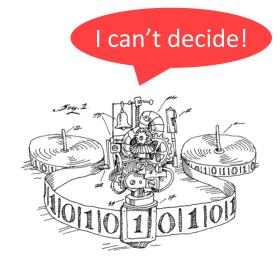
- Distributed protocols are notoriously hard to get right
 - Even small protocols can be tricky
 - Bugs occur on rare scenarios
 - Testing is costly and not sufficient

Verifying distributed protocols is hard

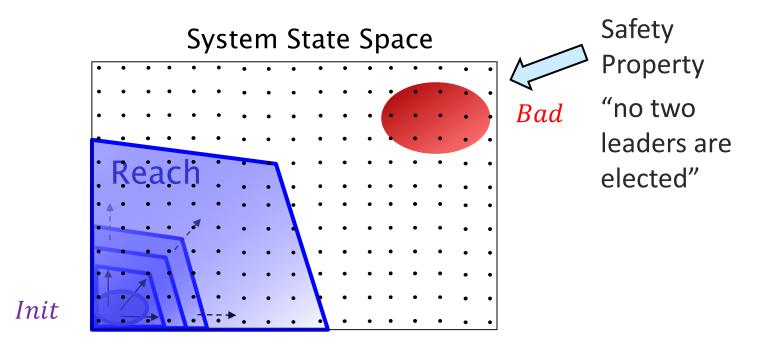
Verify distributed protocols for any number of nodes and resources



- Infinite state-space
 - unbounded #processes
 - unbounded #messages
 - unbounded #objects
- Asymptotic complexity of verification
 - Rice theorem

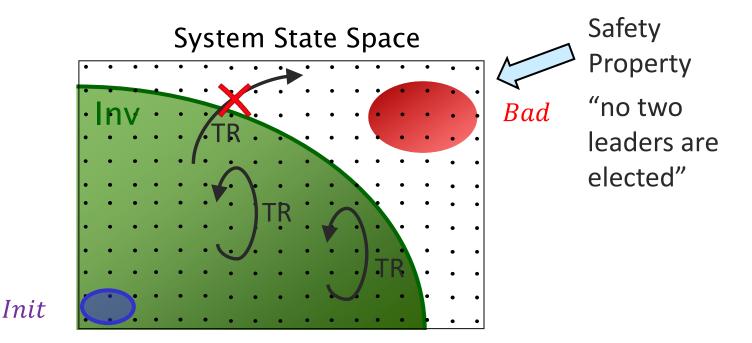


Safety of Infinite State Systems



System S is safe if all the reachable states satisfy the property $P = \neg Bad$

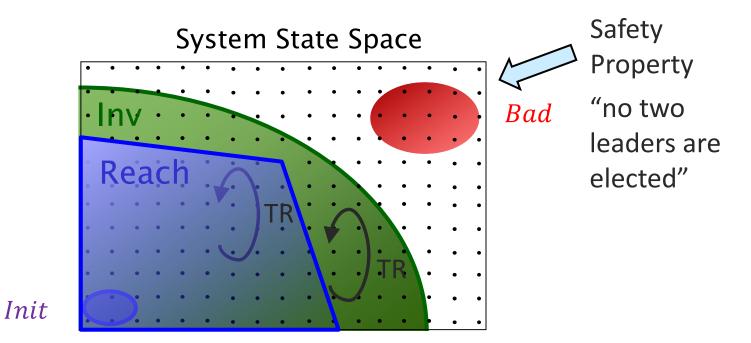
Inductive Invariants



System S is safe if all the reachable states satisfy the property $P = \neg Bad$ System S is safe iff there exists an **inductive invariant** *Inv*:

Init \subseteq *Inv* (Initiation) if $\sigma \in$ *Inv* and $\sigma \rightarrow \sigma'$ then $\sigma' \in$ *Inv* (Consecution) *Inv* \cap *Bad* = \emptyset (Safety)

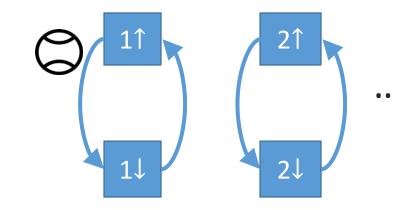
Inductive Invariants



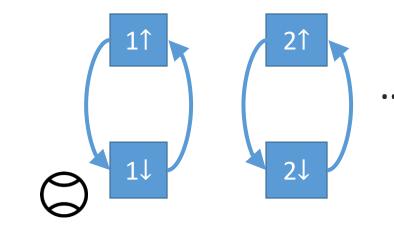
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- N pairs of players pass a ball:
 - 11 will pass to 1 \downarrow
 - − 1↓ will pass to 1 \uparrow
 - 21 will pass to 21
 - $-2\downarrow$ will pass to $2\uparrow$...



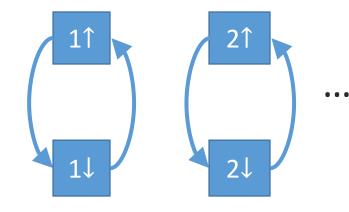
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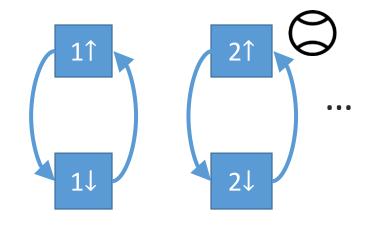
- N pairs of players pass a ball:
 - 11 will pass to 1 \downarrow
 - − 1↓ will pass to 1 \uparrow
 - 21 will pass to 21
 - 2↓ will pass to $2\uparrow$...
- The ball starts at player 11
- Can the ball get to $2\downarrow$?

11	21
1↓	2↓

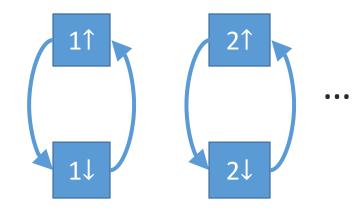
- N pairs of players pass a ball:
 - 11 will pass to 1 \downarrow
 - − 1 \downarrow will pass to 1 \uparrow
 - 21 will pass to $2\downarrow$
 - 2↓ will pass to $2\uparrow$...
- The ball starts at player 1↑
- Can the ball get to $2\downarrow$?
- Is "the ball is not at $2\downarrow$ " an inductive invariant?



- N pairs of players pass a ball:
 - − 11 will pass to 1↓
 - − 1 \downarrow will pass to 1 \uparrow
 - 21 will pass to 21
 - 2↓ will pass to $2\uparrow$...
- The ball starts at player 11
- Can the ball get to $2\downarrow$?
- Is "the ball is not at 2↓" an inductive invariant? No!
 - Counterexample to induction



- N pairs of players pass a ball:
 - − 11 will pass to 1↓
 - − 1 \downarrow will pass to 1 \uparrow
 - 21 will pass to 21
 - 2↓ will pass to $2\uparrow$...
- The ball starts at player 1↑
- Can the ball get to $2\downarrow$?
- Is "the ball is not at 2↓" an inductive invariant? No!
 - Counterexample to induction
- Inductive invariant: "the ball is not at 2↑ nor 2↓"

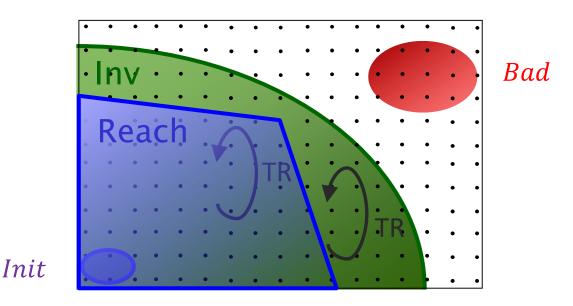


Logic-based verification

Provers/solvers for different logics made huge progress

- Propositional logic (SAT) industrial impact for hardware verification
- Satisfiability modulo theories (SMT) major trend in software verification
- Automated first-order theorem provers
- Interactive theorem provers
- Z3, CVC4, iProver, Vampire, Coq, Isabelle/HOL

Logic-based verification



Represent *Init*, *Tr*, *Bad*, *Inv* by logical formulas: Formula \Leftrightarrow Set of states

Inv(V) is an inductive invariant if the verification conditions (VCs) are valid:InitiationInit(V) \Rightarrow Inv(V)unsat(Init(V) \neg Inv(V))Cons.Inv(V) \land TR(V,V') \Rightarrow Inv(V')unsat(Inv(V) \land TR(V,V') \land Inv(V'))SafetyInv(V) \Rightarrow \neg Bad(V)unsat(Inv(V) \land Bad(V))

Challenges for logic-based verification

Formal specification

Modeling the system and its invariants

Deduction Checking validity of the VCs

Inference Finding an inductive invariant

Deduction

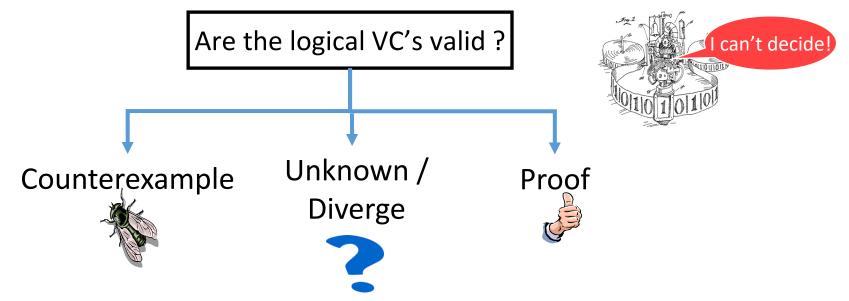
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Safety $Inv(V) \Rightarrow \neg Bad(V)$

Church's Theorem

unsat($Inv(V) \land Bad(V)$)

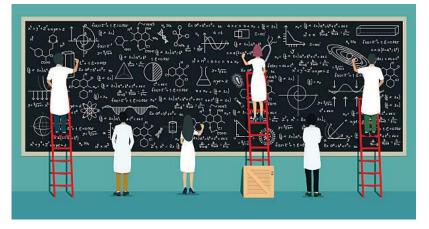


Deduction

Interactive theorem provers (Coq, Isabelle/HOL, LEAN)

- Programmer proves the inductive invariant
- Huge programmer effort (~10-50 lines of proof per line of code)

e.g. Verdi



Automatic solvers/provers

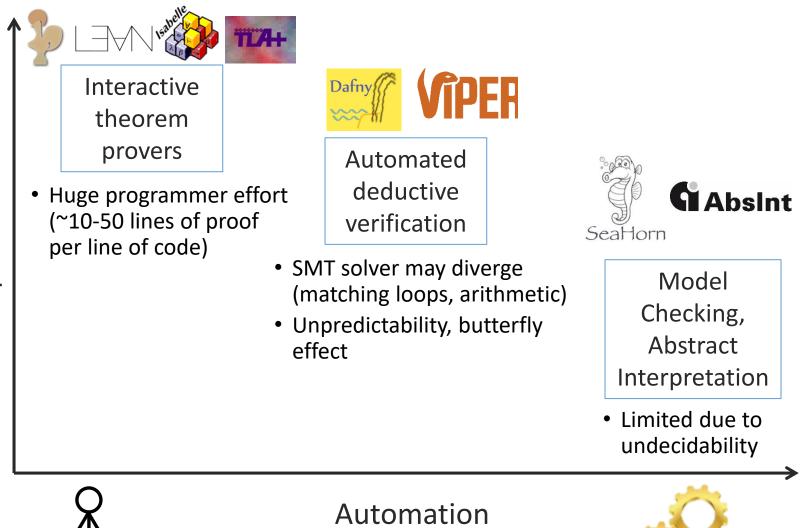
(e.g. Z3, CVC4, Vampire)

- VCs discharged automatically
- Tools may diverge (for SMT: matching loops, arithmetic)
- Unpredictability (butterfly effect)

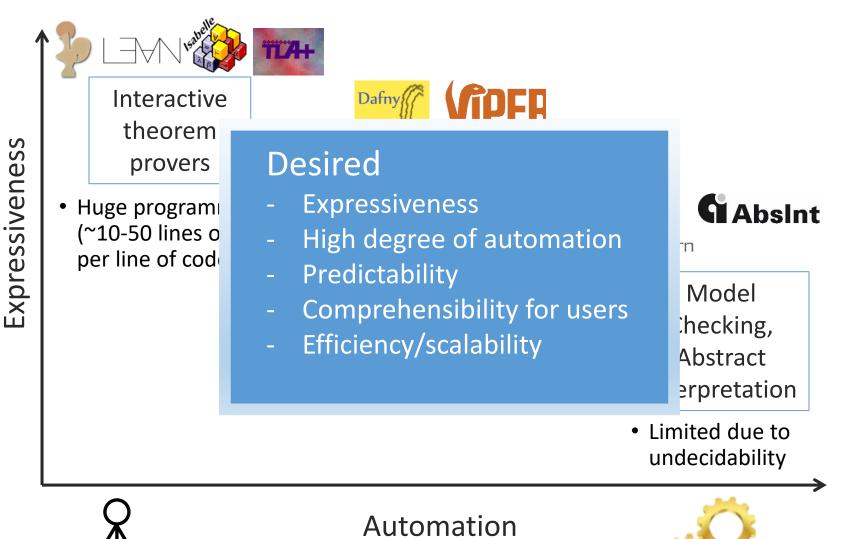
e.g. Ironfleet



Logic-based verification approaches



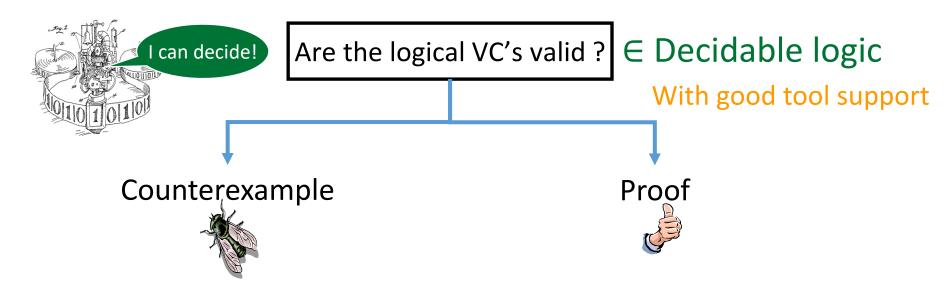
Logic-based verification approaches



This talk: Restrict VC's to decidable logic

Inv(V) is an inductive invariant if the following verification conditions are valid:

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Challenges for verification with decidable logic

Formal specification

Modeling in a decidable logic

Deduction Checking validity of the VC's



Invariant inference

Finding an inductive invariant

This talk

Logic: EPR – decidable fragment of first order logic

Formal specification

Surprisingly expressive

Invariant inference

- Automatic (based on PDR)
 - Semi-algorithm: may diverge
- Interactive
 - Based on graphically displayed counterexamples to induction

Effectively Propositional Logic – EPR

Decidable fragment of first order logic

+ Quantification $(\exists^*\forall^*)$ - Theories (e.g., arithmetic)

☺ Allows quantifiers to reason about unbounded sets

- $\forall x, y$. leader(x) \land leader(y) \rightarrow x = y

- ③ Satisfiability is decidable => Deduction is decidable
- Small model property => Finite cex to induction
- © Turing complete modeling language
- ☺ Limited language for safety and inductive invariants

Suffices for many infinite-state systems

Successful verification with EPR

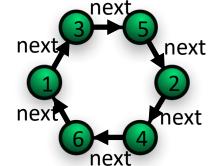
Shape Analysis

[Itzhaky et al. CAV'13, POPL'14, CAV'14, CAV'15]

- Software-Defined Networks [Ball et al. PLDI'14]
- Distributed protocols [Padon et al. PLDI'16, OOPSLA'17, POPL'18, PLDI'18]
- Concurrent Modification Errors in Java programs [Frumkin et al. VMCAl'17]

Example: Leader Election in a Ring

- Nodes are organized in a unidirectional ring
- Each node has a unique numeric id
- Protocol:
 - Each node sends its id to the next



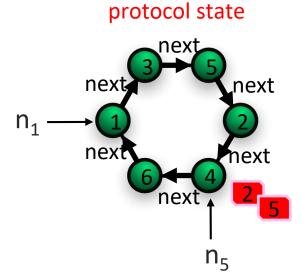
- A node that receives a message passes it to the next if the id in the message is higher than the node's own id
- A node that receives its own id becomes the leader
- Theorem:
 - The protocol selects at most one leader

[CACM'79] E. Chang and R. Roberts. *An improved algorithm for decentralized extrema-finding in circular configurations of processes*

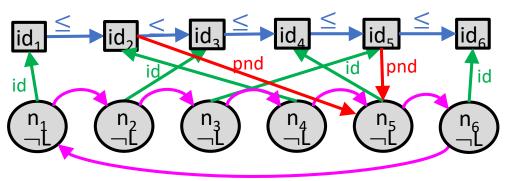
State: finite first-order structure over vocabulary V

- \leq (ID, ID) total order on node id's
- id: Node \rightarrow ID relate a node to its id
- btw (Node, Node, Node) the ring topology
- **pending**(ID, Node) pending messages
- leader(Node) leader(n) means n is the leader

Axiomatized in EPR



structure



 $\langle n_5, n_1, n_3 \rangle \in I(btw)$

- State: finite first-order structure over vocabulary V (+ axioms)
- Initial states and safety property: EPR formulas over V
 - Init(V) initial states, e.g., \forall id, n. \neg pending(id, n)
 - Bad(V) bad states, e.g., $\exists n_1, n_2$. leader $(n_1) \land leader(n_2) \land n_1 \neq n_2$

 Transition relation: expressed as EPR formula TR(V, V'), e.g.: ∃n,s. "s = next(n)" ∧ ∀x,y. pending'(x,y)↔ (pending(x,y) ∨ (x=id[n]∧y=s))
∨ ∃n. pending (id[n],n) ∧ ∀x. leader'(x) ↔ (leader(x) ∨ x=n)

• State: finite first-order structure over vocabulary V (+ axioms)

Propose(n): send(id(n), next(n))

...

Recv(n,msg): if msg = id(n) then leader(n) := true

if msg > id(n) then send(msg,next(n))

Transition relation: expressed as EPR formula TR(V, V'), e.g.:

 $\exists n,s. "s = next(n)" \land \forall x,y. pending'(x,y) \leftrightarrow (pending(x,y) \lor (x=id[n] \land y=s))$

 $\lor \exists n. pending (id[n],n) \land \forall x. leader'(x) \leftrightarrow (leader(x) \lor x=n)$

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Specify and verify the protocol for any number of nodes in the ring

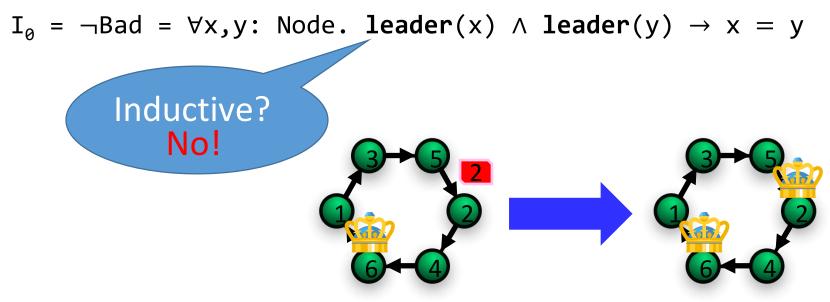
Using EPR for Verification

- System model Init(V), Bad(V), TR(V, V') ∈ EPR
- Inductive invariant $Inv(V) \in \forall^*$
- Verification conditions Initiation Init(V) \Rightarrow Inv(V) unsat(Init(V) \neg Inv(V)) Cons. Inv(V) \land TR(V,V') \Rightarrow Inv(V') unsat(Inv(V) \land TR(V,V') \land \neg Inv(V')) Safety Inv(V) $\Rightarrow \neg$ Bad(V) unsat(Inv(V) \land Bad(V))

Verification conditions ∈ EPR→ Decidable to check

Inductive Invariant for Leader Election

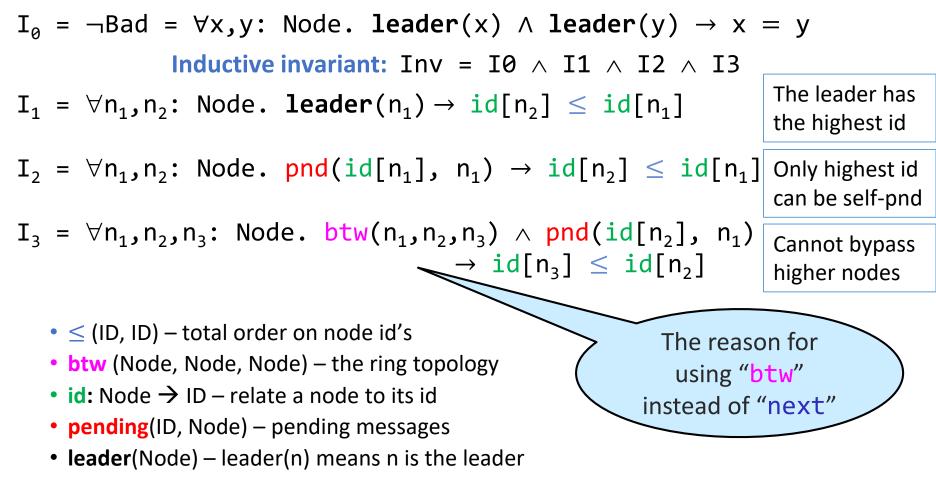
Safety property:



- (ID, ID) total order on node id's
- btw (Node, Node, Node) the ring topology
- id: Node → ID relate a node to its id
- pending(ID, Node) pending messages
- leader(Node) leader(n) means n is the leader

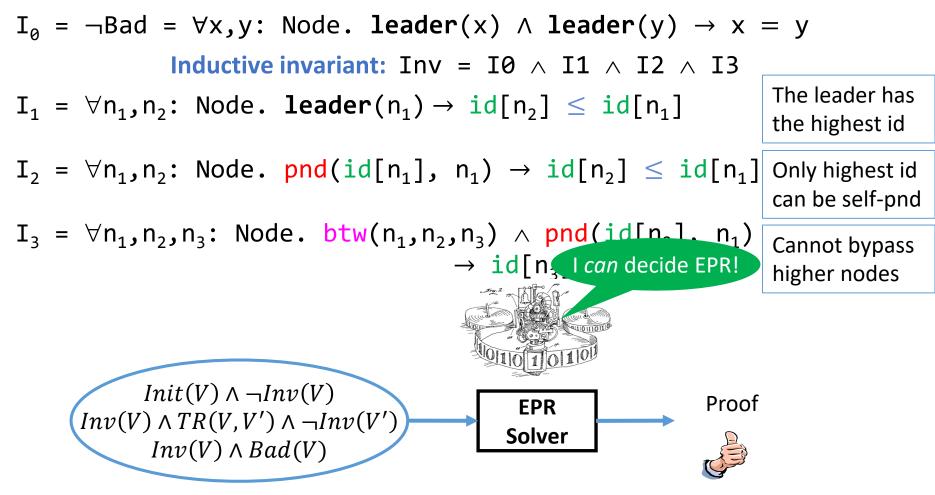
Inductive Invariant for Leader Election

Safety property:



Inductive Invariant for Leader Election

Safety property:



Axioms: Leader Election Protocol

- \leq (ID, ID) total order on node id's
- btw (a: Node, b: Node, c: Node) the ring topology
- id: Node \rightarrow ID relate a node to its unique id
- pending(ID, Node) pending messages
- leader(Node) leader(n) means n is the leader

	Intention	EPR Modeling
Node ID's	Integers	$ \begin{array}{l} \forall i: ID. \ i \leq i \ \text{Reflexive} \\ \forall i, j, k: ID. \ i \leq j \land j \leq k \rightarrow i \leq k \ \text{Transitive} \\ \forall i, j: ID. \ i \leq j \land j \leq I \rightarrow i = j \ \text{Anti-Symmetric} \\ \forall i, j: ID. \ i \leq j \lor j \leq i \ \text{Total} \\ \forall x, y: \text{Node.} \ id(x) = id(y) \rightarrow x = y \ \text{Injective} \end{array} $
Ring Topology	Next edges + Transitive closure	$\forall x, y, z: Node. btw(x, y, z) \rightarrow btw(y, z, x)$ Circular shifts $\forall x, y, z, w: Node. btw(w, x, y) \land btw(w, y, z) \rightarrow btw(w, x, z)$ Transitive $\forall x, y, w: Node. btw(w, x, y) \rightarrow \neg btw(w, y, x)$ Anti-Symmetric $\forall x, y, z, w: Node. distinct(x, y, z) \rightarrow btw(w, x, y) \lor btw(w, y, x)$
		"next(a)=b" = $\forall x: Node. x \neq a \land x \neq b \rightarrow btw(a,b,x)$

So far

Formal specification with EPR

- Surprisingly expressive
 - Integers: numeric id's expressed with \leq
 - Transitive closure: ring topology expressed with btw
 - Network semantics: pending messages
 - Sets and cardinalities (for consensus protocols) [OOPSLA'17]
 - Liveness properties [POPL'18, FMCAD'18]
 - Implementations [PLDI'18]

Not in this talk

Next

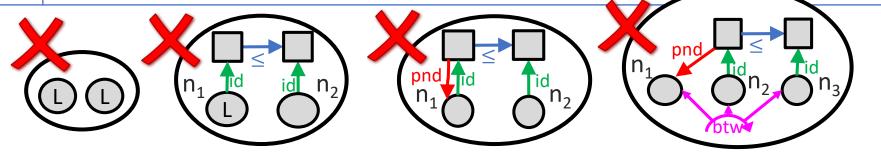
Invariant inference: finding inductive invariants

- (1) Automatically
 - Adapt techniques from finite-state model checking (PDR)
- (2) Interactively
 - Based on graphically displayed counterexamples to induction

How can we find a universally quantified inductive invariant?

Inductive Invariant for Leader Election

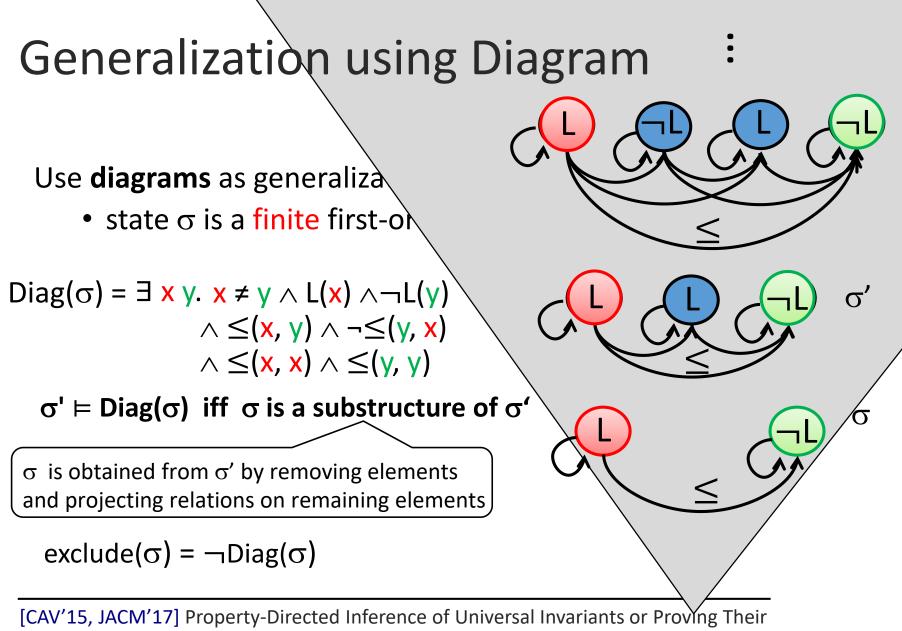
I₀ ⊣Bad	$\forall n_1, n_2 : Node. leader(n_1) \land leader(n_2) \rightarrow n_1 = n_2$ $\neg \exists n_1, n_2 : Node. leader(n_1) \land leader(n_2) \land n_1 \neq n_2$	At most one leader elected
I	$\forall n_1, n_2: \text{ Node. } \textbf{leader}(n_1) \rightarrow \textbf{id}[n_2] \leq \textbf{id}[n_1] \\ \neg \exists n_1, n_2: \text{ Node. } \textbf{leader}(n_1) \land \textbf{id}[n_2] > \textbf{id}[n_1] \end{cases}$	The leader has the highest id
I ₂	$\forall n_1, n_2: \text{ Node. } pnd(id[n_1], n_1) \rightarrow id[n_2] \leq id[n_1] \\ \neg \exists n_1, n_2: \text{ Node. } pnd(id[n_1], n_1) \land id[n_2] > id[n_1] \end{cases}$	
I ₃		higher nodes
	$\neg \exists n_1, n_2, n_3$: Node. $btw(n_1, n_2, n_3) \land pnd(id[n_2], n_1) \land id[n_3] > id[n_2]$	



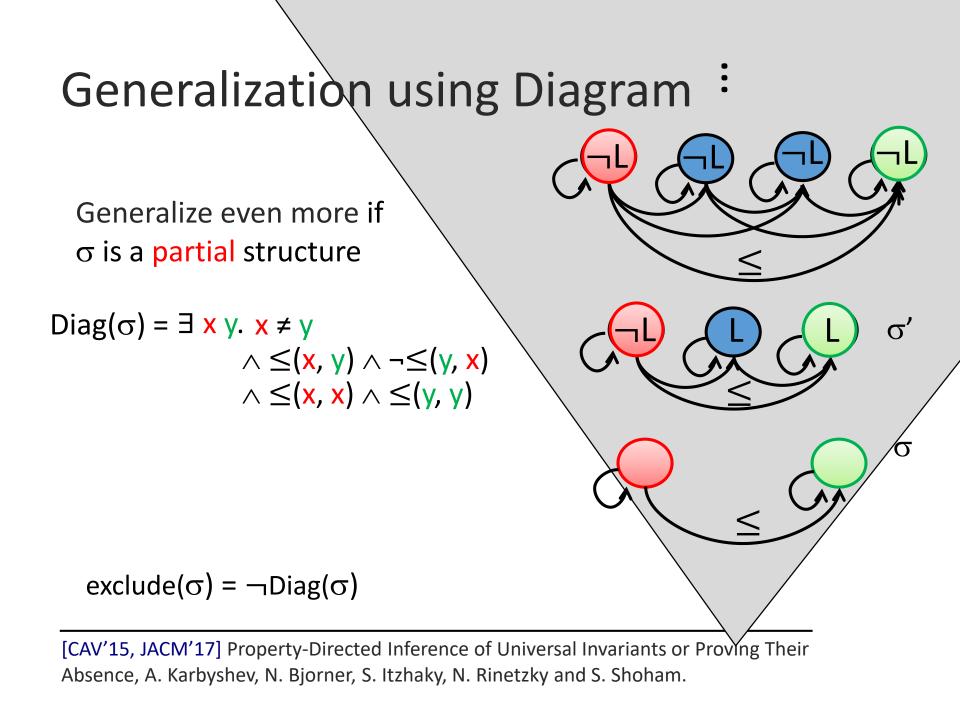


Construct Inv by excluding "bad" states

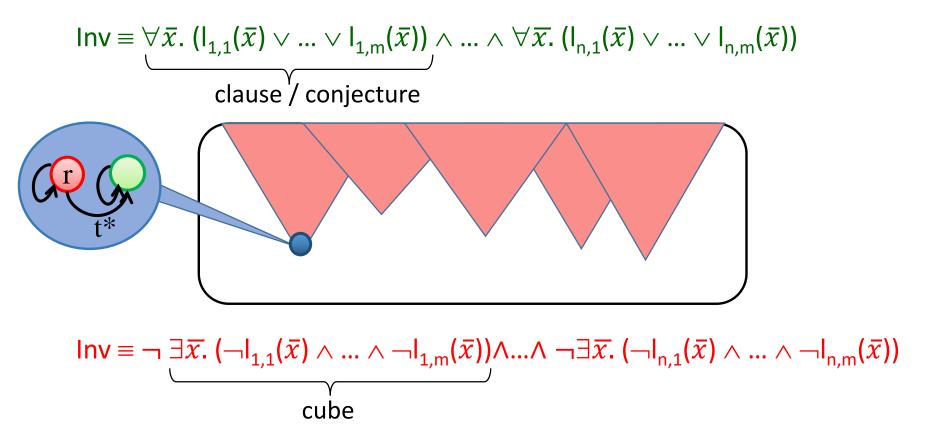
- 1. How to find these states?
- 2. How to generalize into conjectures?



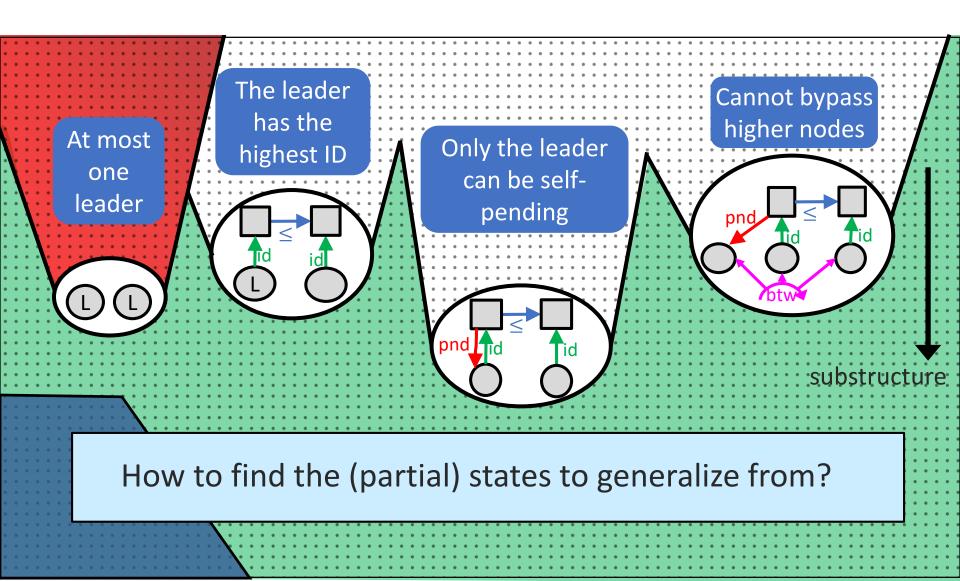
Absence, A. Karbyshev, N. Bjorner, S. Itzhaky, N. Rinetzky and S. Shoham.



∀* Invariant - excluded substructures



Leader election example



(1) Automatic inference: UPDR

• Based on Bradley's IC3/PDR [VMCAI11,FMCAD11]

SAT-based verification of finite-state systems

- Abstracts concrete states using their logical diagram
- Backward traversal performed over diagrams
- Blocking of CTI excludes a *generalization* of its diagram → generates universally quantified lemmas

- [CAV'15, JACM'17] Property-Directed Inference of Universal Invariants or Proving Their Absence, A. Karbyshev, N. Bjorner, S. Itzhaky, N. Rinetzky and S. Shoham.
- [VMCAI'17] Property Directed Reachability for Proving Absence of Concurrent Modification Errors, A. Frumkin, Y. Feldman, O. Lhoták, O. Padon, M. Sagiv and S. Shoham.

UPDR: Possible outcomes

- Universal inductive invariant found
 - System is safe

Used to infer inductive invariants / procedure summaries of:

- Heap-manipulating programs, e.g.
 - Singly/Doubly/Nested linked list
 - Iterators in Java Concurrent modification error (CME)
- Distributed protocols
 - Spanning tree
 - Learning switch

No need for user-defined predicates/ templates!

UPDR: Possible outcomes

- Universal inductive invariant found
 - System is safe
- Proof that no universal inductive invariant exists

Safety not determined*



* can use Bounded Model Checking to find real counterexamples

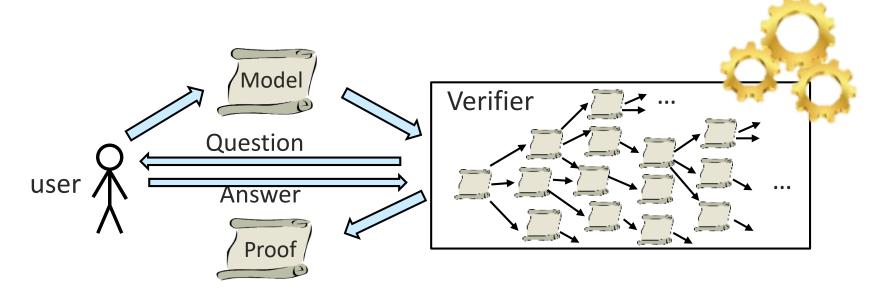
UPDR: Possible outcomes

- Universal inductive invariant found
 - System is safe
- Proof that no universal inductive invariant exists
 - Safety not determined*
- Divergence
 - In general, inferring universal ind. inv. is undecidable
 - For linked lists it is decidable, UPDR will also terminate
 - Proof uses well-quasi-order and Kruskal's tree theorem
- [POPL'16] Decidability of Inferring Inductive Invariants, O. Padon, N. Immerman, S. Shoham, A. Karbyshev, and M. Sagiv.

Automatic Inference (e.g., UPDR)

Ultimately limited by undecidability

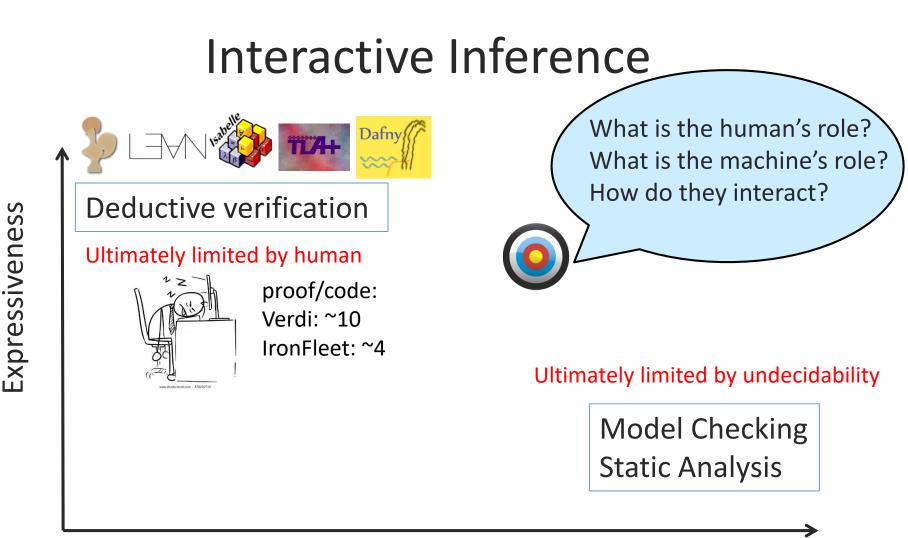
(2) Interactive Inference



- Let the user guide the tool
 - User has intuition about the essence of the proof
 - Computer is good at handling corner cases



Supervised Verification of Infinite-State Systems



Automation



Supervised Verification of Infinite-State Systems

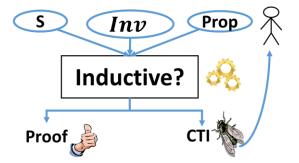
Ivy: Interactive Generalization

$$In\nu = I_0 \wedge \dots \wedge I_k$$



Displays "minimal" CTI to exclude

Generalizes to a partial state



• removes "irrelevant" facts (graphical interface - checkboxes)



Translates to universally quantified conjecture (via diagram) Provides auxiliary automated checks:

1. BMC(K): uses SAT solver to check if conjecture is true up to K

• User determines the right K to use

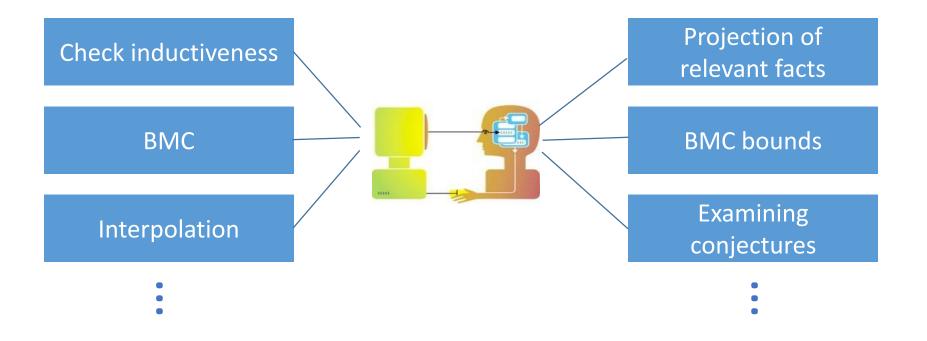
2. ITP(K): uses SAT solver to discover more facts to remove



Examines the proposed conjecture – it could be wrong Adds I_{k+1}

[PLDI'16] IVy: Safety Verification by Interactive Generalization. O. Padon,K. McMillan, A. Panda, M. Sagiv, S. Shoham https://github.com/Microsoft/ivy

Interactive Verification in IVy



Decidable Problems Predictable Automation

Proof intuition and creativity Graphical interaction

Summary 1

Verification with decidable logic

- EPR decidable fragment of FOL
 - Deduction is decidable
 - Finite counterexamples

- Domain knowledge and axioms
- Derived relations
- Modularity
- Prophecy

- Can be made surprisingly powerful
 - Transitive closure: linked lists, ring topology [PLDI'16]
 - Paxos, Multi-Paxos, [OOPSLA'17]
 - Liveness and Temporal Properties [POPL'18]
 - Developing verified implementations [PLDI'18]

Summary 2

Invariant Inference

- Automatic inference: UPDR [CAV'15, JACM]
- Interactive inference: lvy [PLDI'16]
- Use logical diagram to infer $\mathsf{Inv} \in \forall^*$
- Can also prove absence of $Inv \in \forall^*$

Take away

Decidable logic is useful
facilitates automation

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Proof Assistants	Supervised	
Ultimately limited by human proof/code: Verdi: ~10 IronFleet: ~4	Verification proof/code: IVy ~1/10 Ultimately limited by undecidab	
	Model Checking Static Analysis	

litv

- We need ways to guide verification tools
- How to divide the problem between human and machine?
- Different inference schemes
- Different Forms of interaction
- Other logics
- Theoretical understanding of limitations and tradeoffs



Supervised Verification of Infinite-State Systems