

# Scaling Abstraction Refinement via Pruning

PLDI - San Jose, CA

June 8, 2011

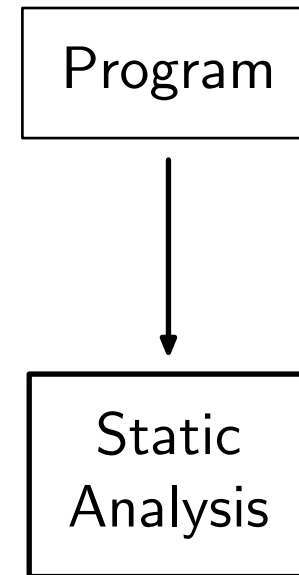
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UC Berkeley

Mayur Naik  
Intel Labs Berkeley

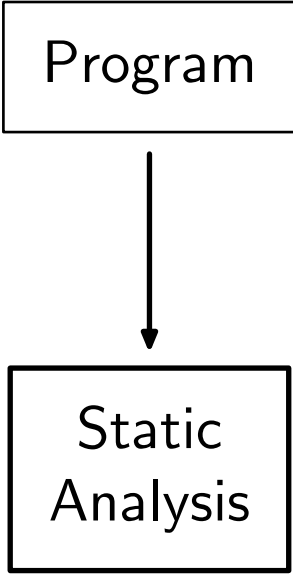
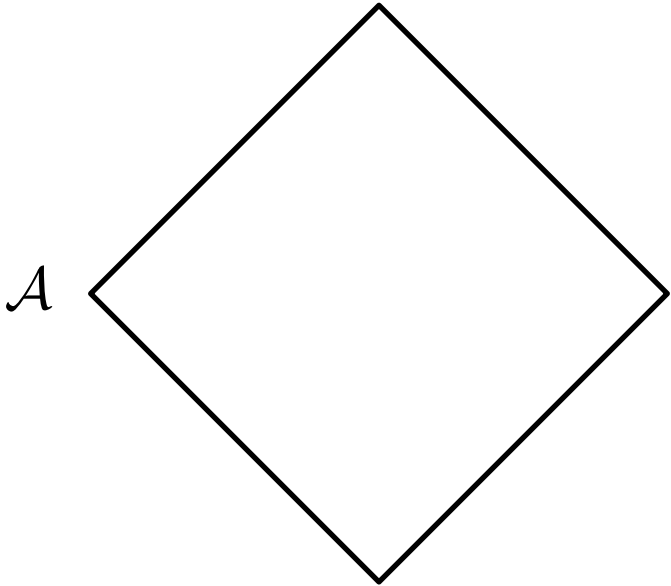
# The Big Picture

Program

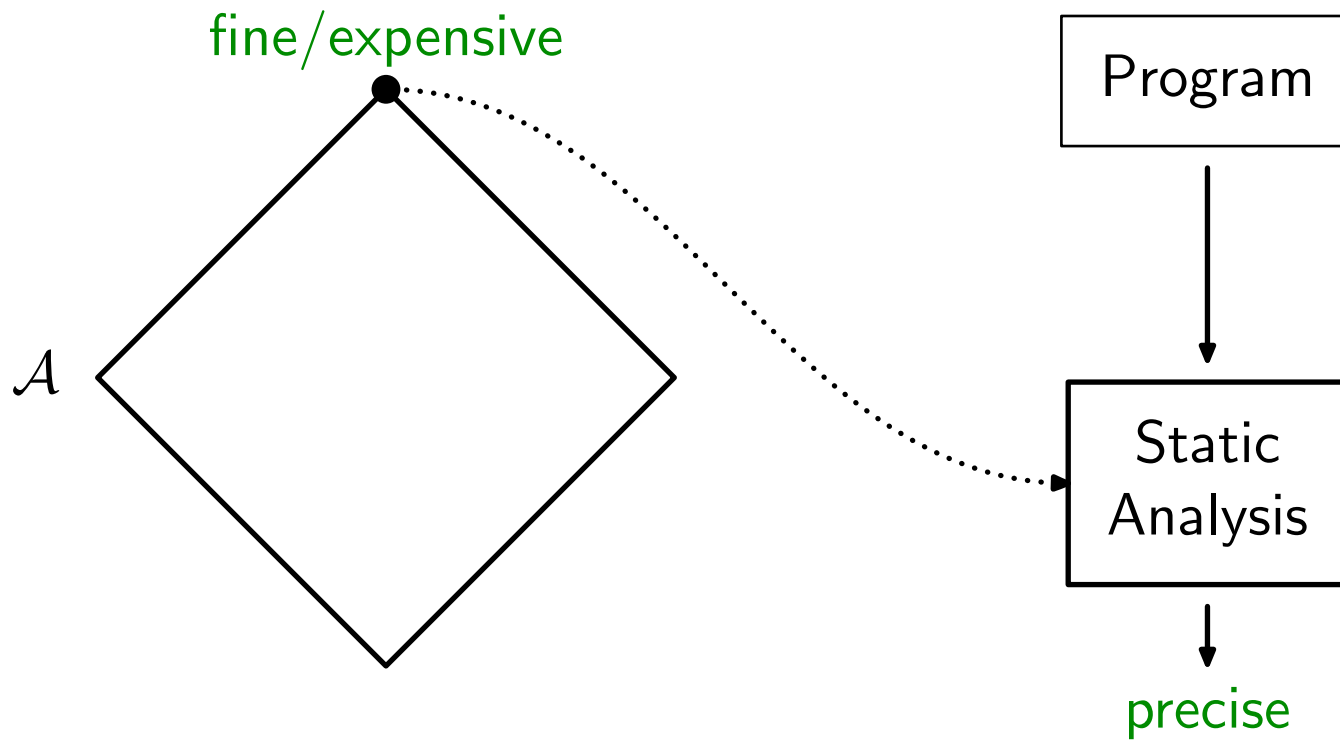
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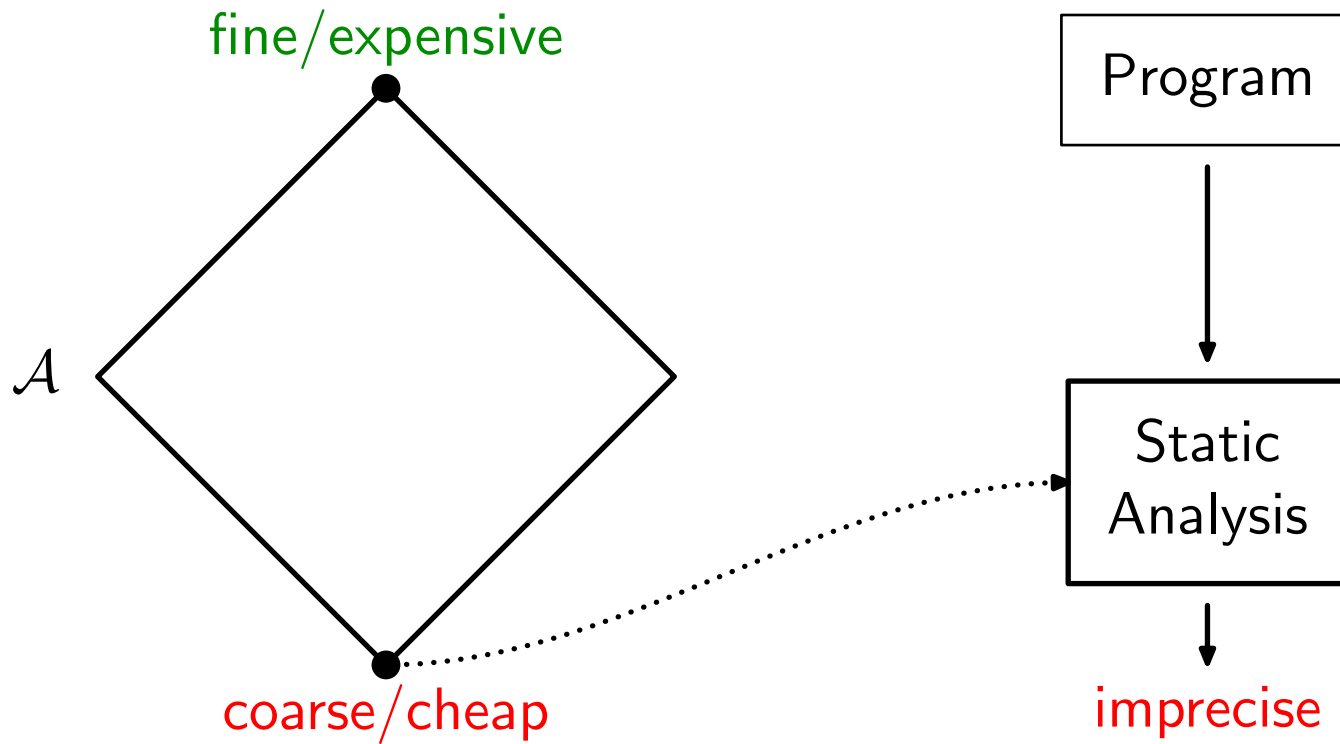
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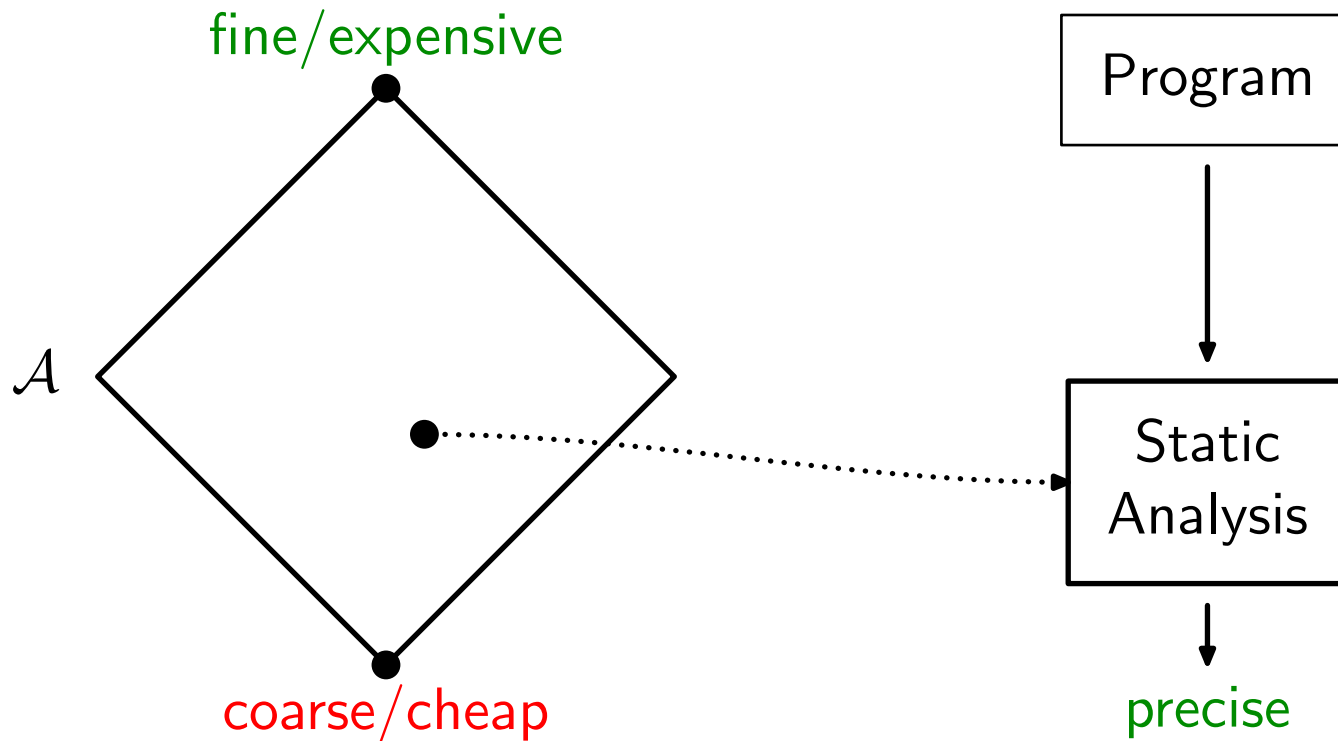
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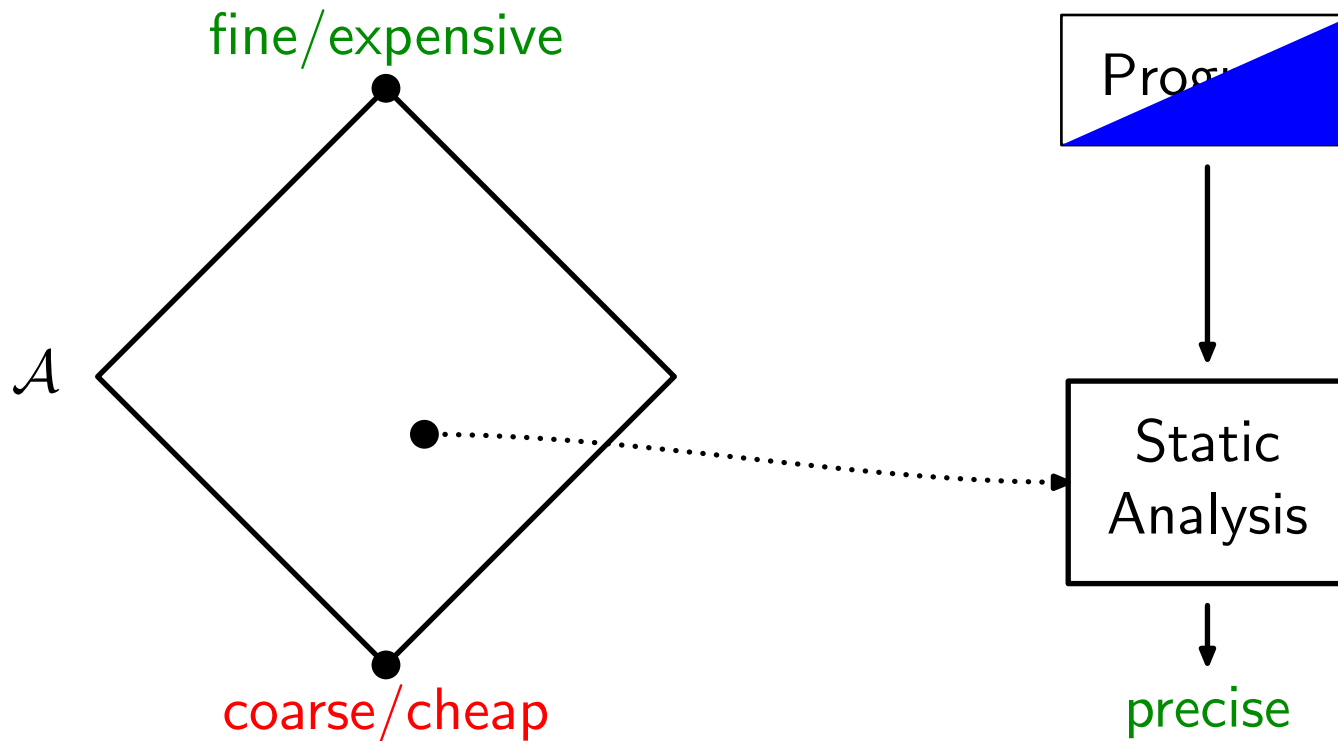
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## selected refinement

- [Heintze & Tardieu 2001]
- [Guyer & Lin 2003]
- [Sridharan et al. 2005]
- [Zheng & Rugina 2008]
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# The Big Picture



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pruning

**NEW!**



# An Example of Pruning

```
    getnew() {  
h1:    u = new C  
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**Query:** do x and y alias? (no)

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0-CFA:

u = new C

v = new C

x = getnew()

y = getnew()

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u → h1

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u → h1

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v → h2

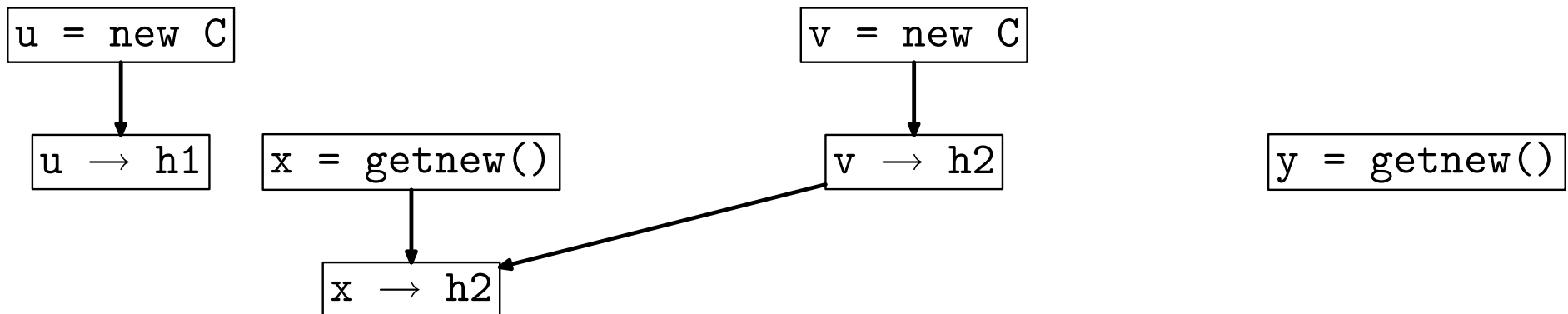
y = getnew()

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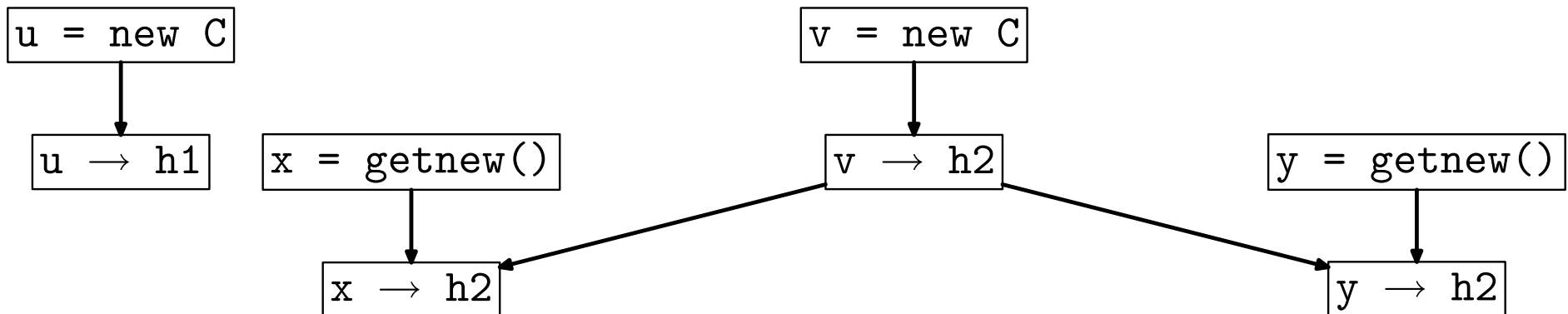


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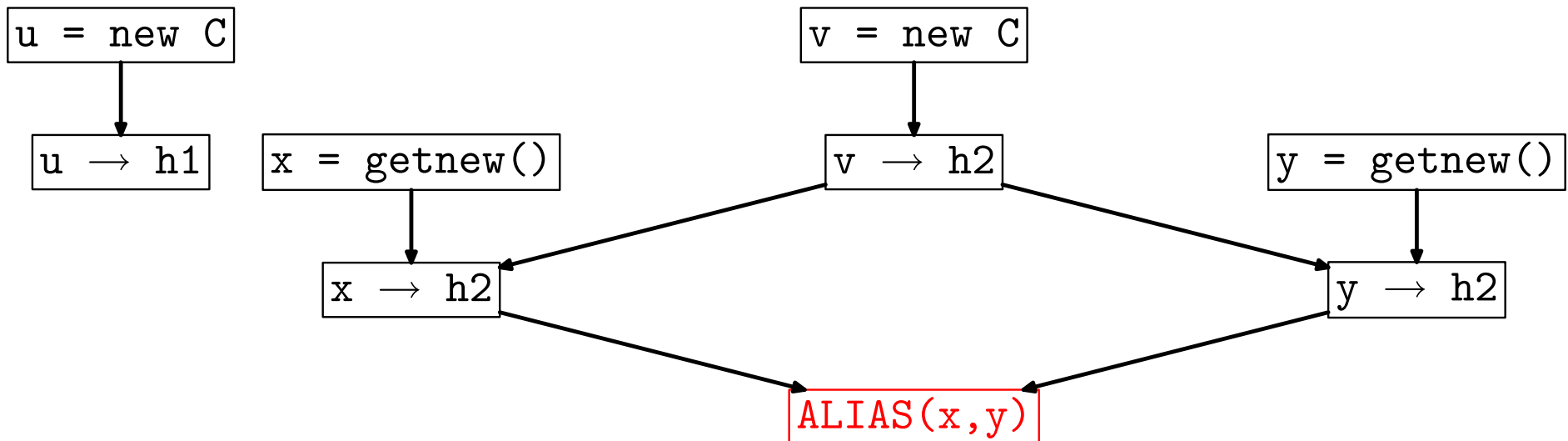


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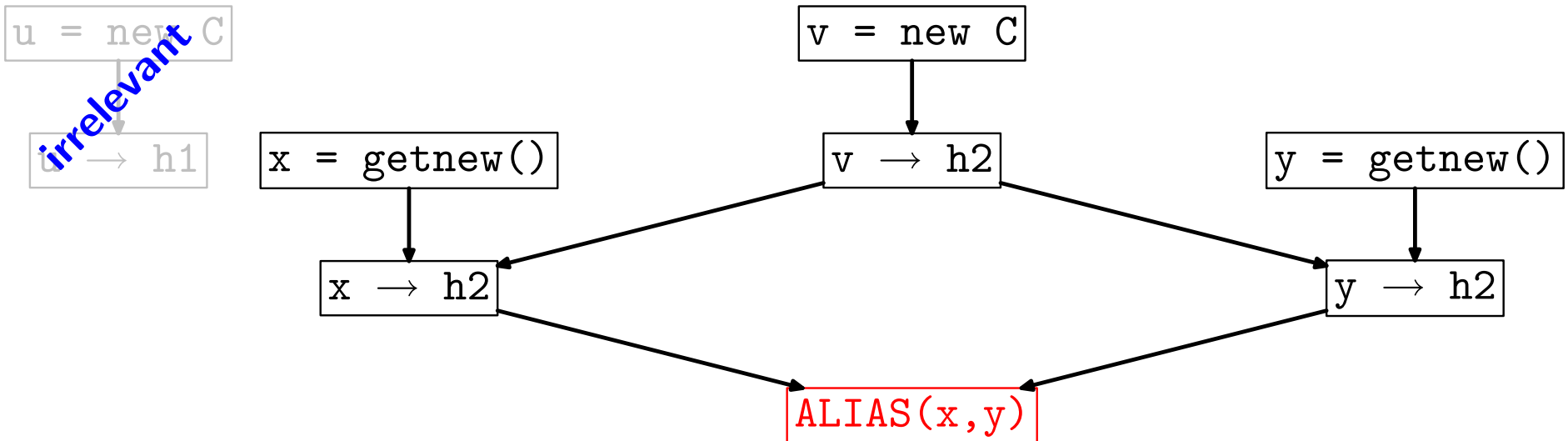


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Query: do x and y alias? (no)

1-CFA on pruned:

u = new C

irrelevant  
↓  
u → h1

x = getnew()

v:i1 = new C

v:i2 = new C

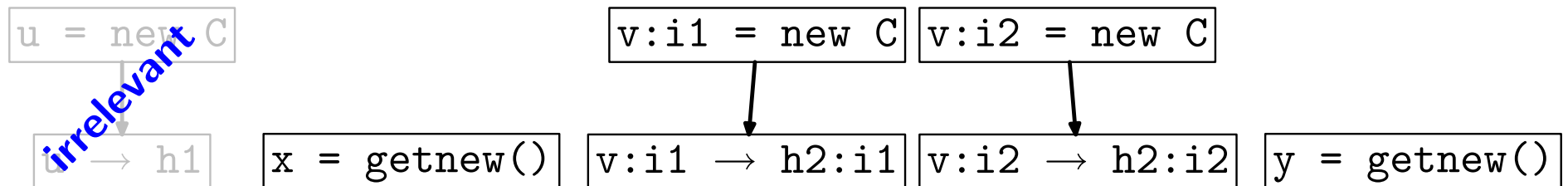
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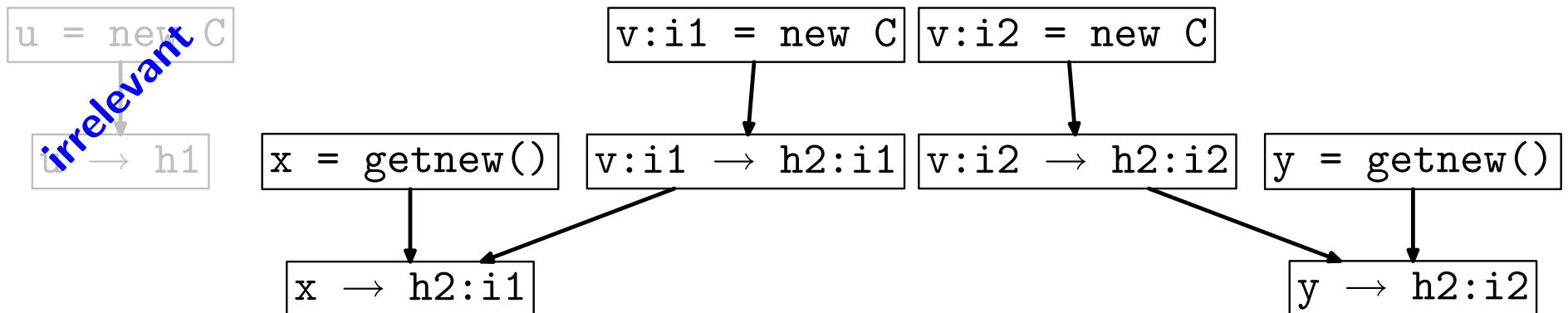


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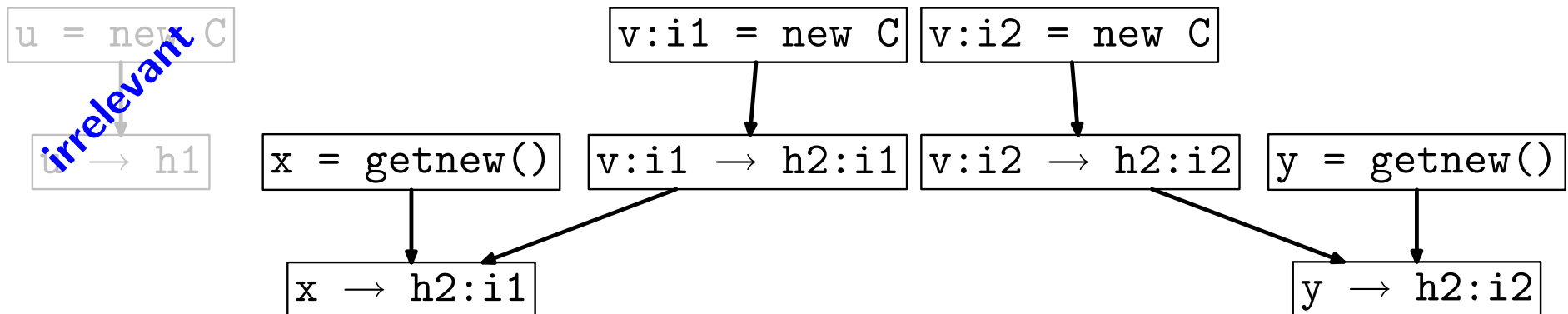


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1-CFA on pruned:



(not aliasing - query proven)

# General Pruning Framework

Input tuples  $A_0$

$v = \text{new } C \dots$

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`v = new C` ...

Query tuple  $x_Q$

`ALIAS(x, y)`

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$\text{ALIAS}(x, y)$

Datalog rules

$v_2 \rightarrow h \Leftarrow v_2 = v_1, v_1 \rightarrow h$

$\dots$



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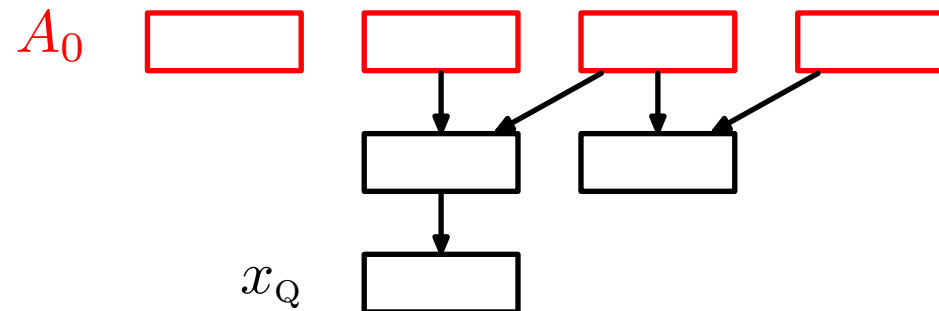
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Prune/prove operator  $\mathbf{P}$

$A_0 \xrightarrow{\mathbf{P}}$  subset of  $A_0$  used to derive  $x_Q$



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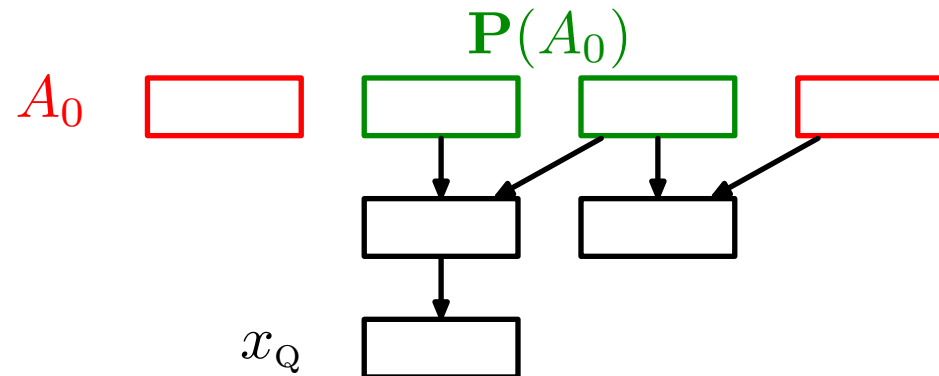
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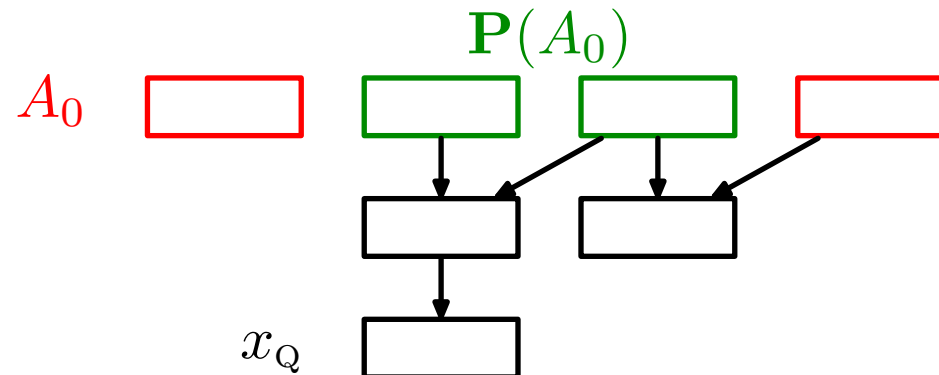
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Query proven  $\Leftrightarrow \mathbf{P}(A_0) = \emptyset$

# Prune and Refine

(abstract tuples)  $A_0$  `u = new C` `v = new C` ...

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(abstract tuples)

$A_0$

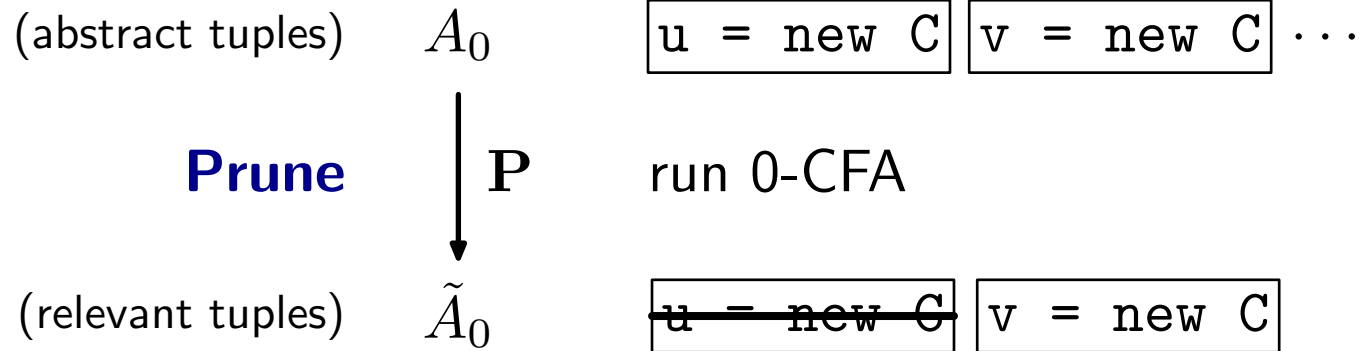
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**Prune**

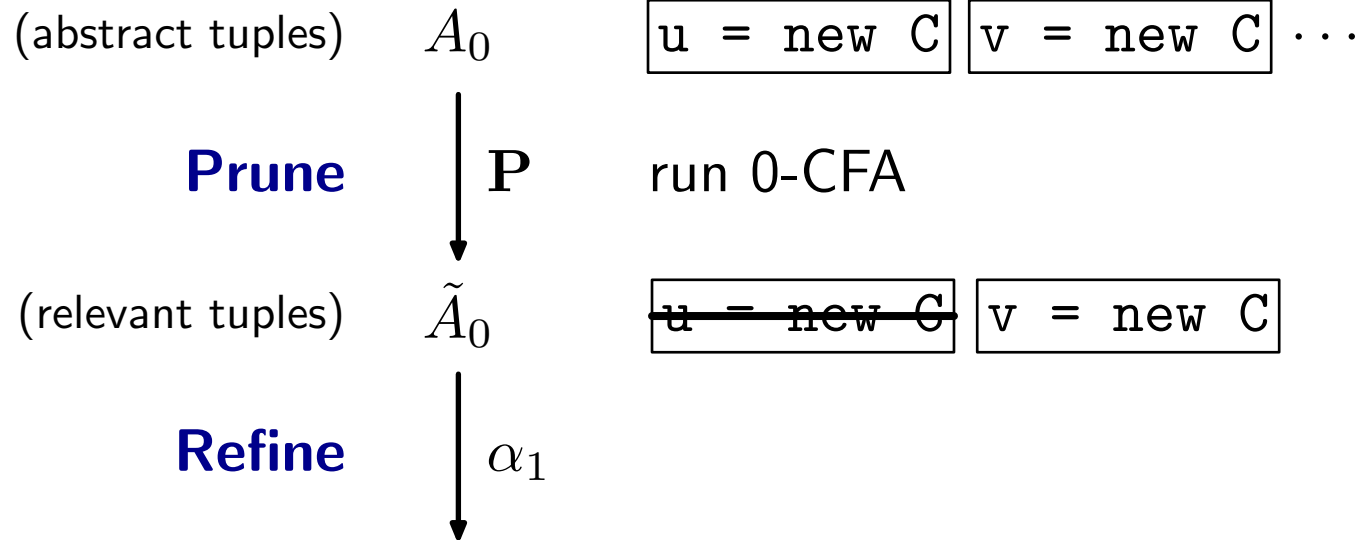


run 0-CFA

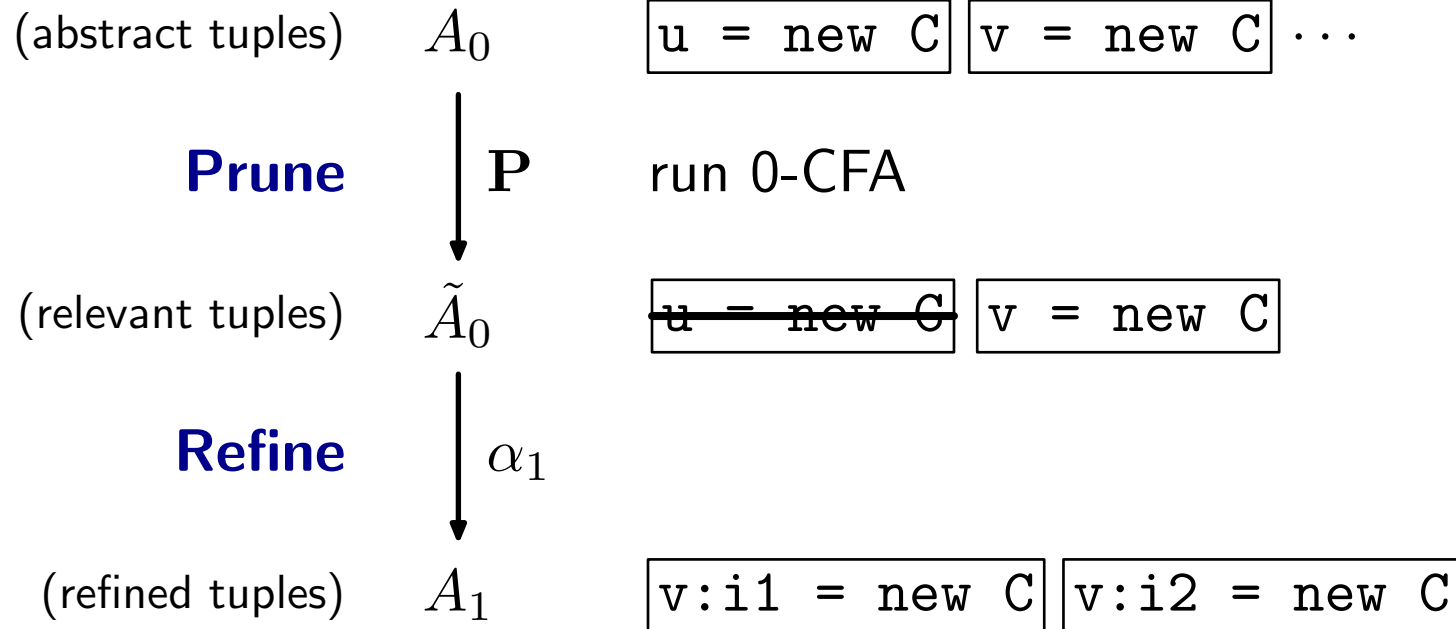
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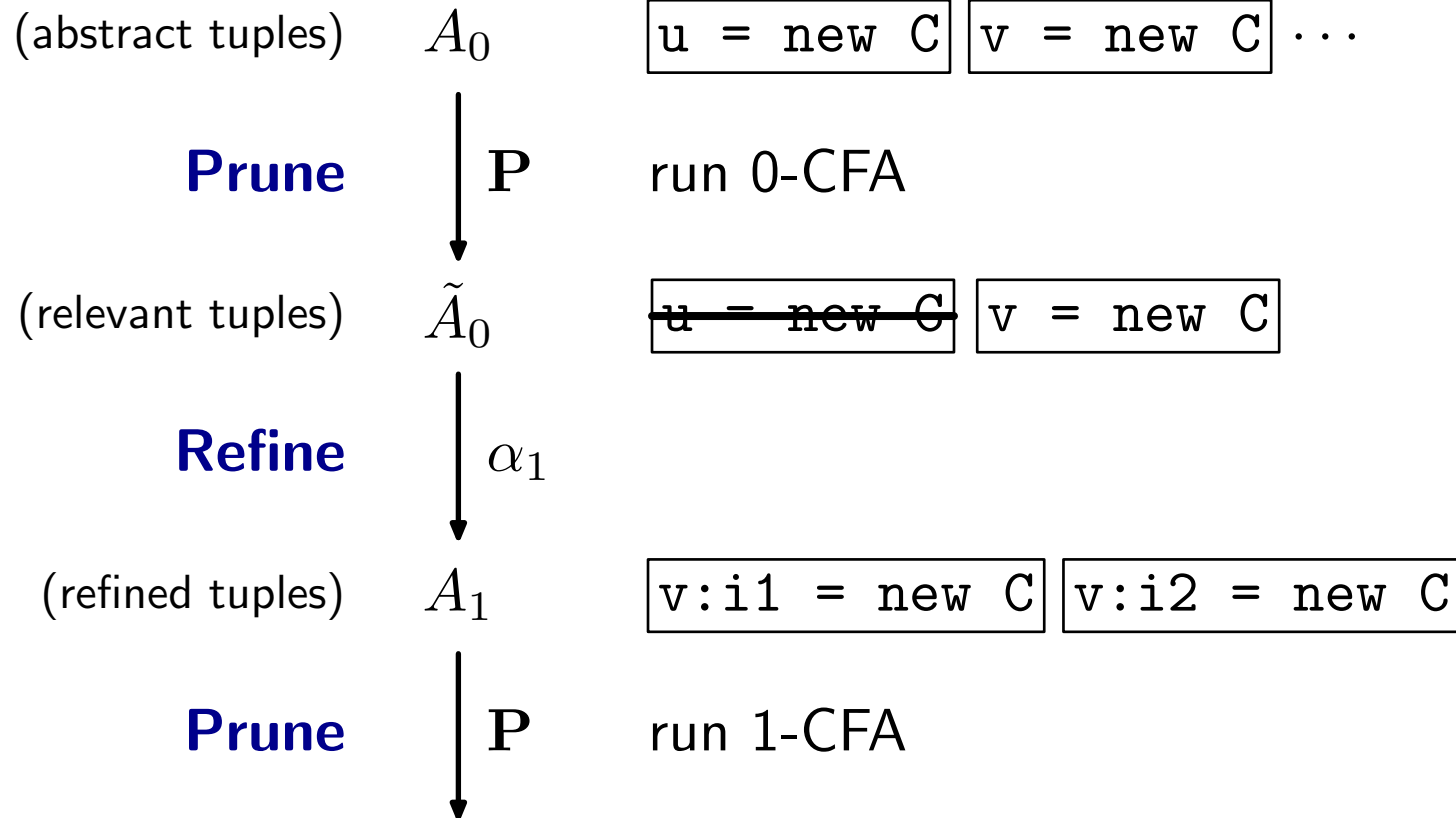


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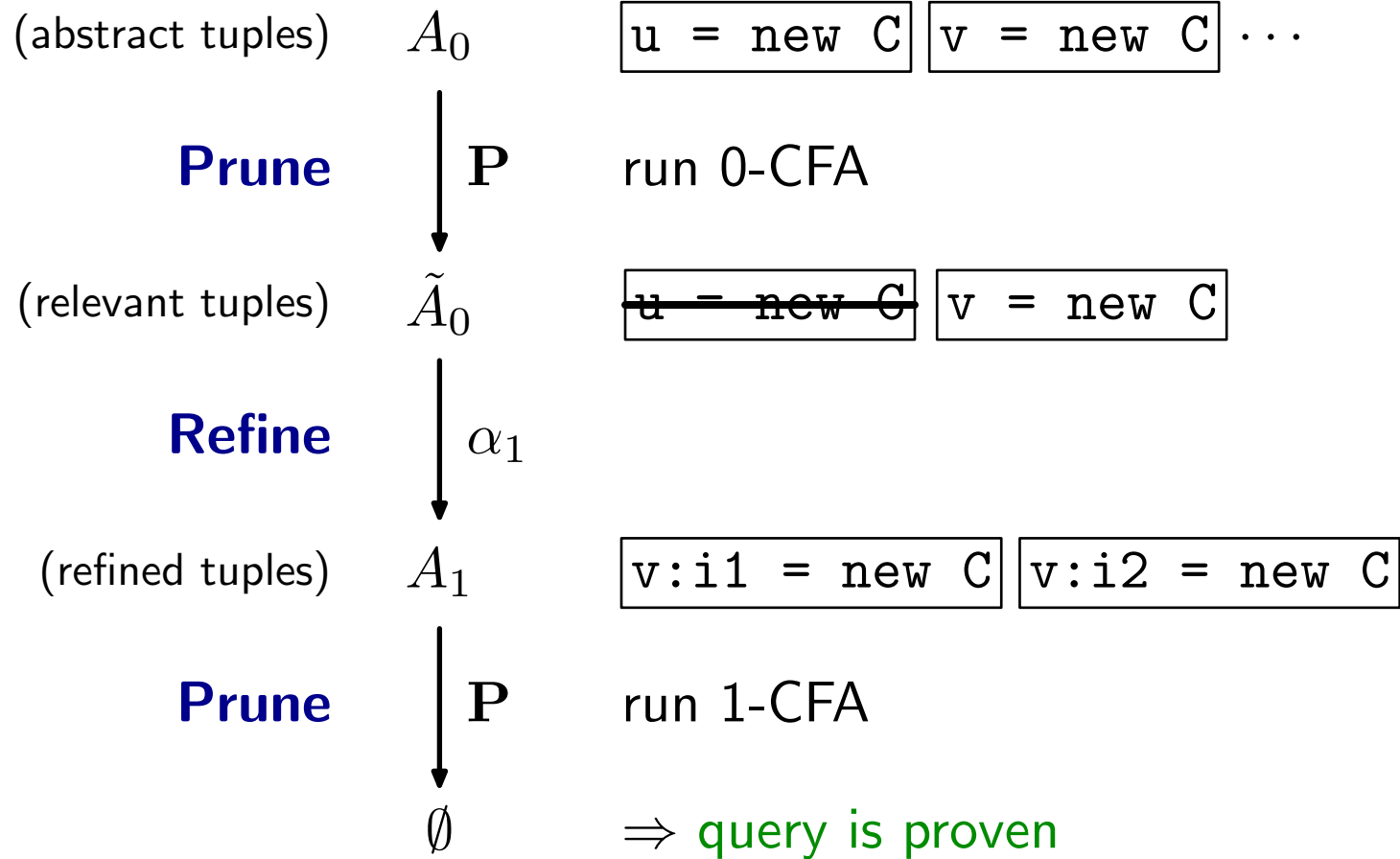




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Sequence of abstractions:  $\alpha_0 \preceq \alpha_1 \preceq \alpha_2 \preceq \dots$

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For  $t = 0, 1, 2, \dots$ :

**Prune:**  $\tilde{A}_t = \mathbf{P}(A_t)$ . If  $\tilde{A}_t = \emptyset$ : return proven.

**Refine:**  $A_{t+1} = \alpha_{t+1}(\tilde{A}_t)$ .

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Prune-Refine after  $t$  iterations

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Full Analysis on  $\alpha_t$

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Full Analysis on  $\alpha_t$

fast

slow

# Rest of Talk

Pre-Pruning Extension

Experiments

# Pre-Pruning

$$\tilde{A}_{t-1}$$

$$v = \text{new } C$$

# Pre-Pruning

$$\tilde{A}_{t-1}$$

$v = \text{new } C$
---------------------

Refine  $\alpha_t$



$$A_t$$

$v:h0 = \text{new } C$
$v:h1 = \text{new } C$
$v:h2 = \text{new } C$
$v:h3 = \text{new } C$
$v:h4 = \text{new } C$
$v:h5 = \text{new } C$

# Pre-Pruning

$\tilde{A}_{t-1}$   
v = new C

Refine  $\alpha_t$   
→

$A_t$

v:h0 = new C
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Prune P  
→

expensive!

# Pre-Pruning

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$A_t$

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Prune P  
→

↓  $\beta_t \preceq \alpha_t$

$B_t$

v:t0 = new C
v:t1 = new C

# Pre-Pruning

$$\tilde{A}_{t-1}$$

v = new C

Refine  $\alpha_t$

→

$$A_t$$

v:h0 = new C

v:h1 = new C

v:h2 = new C

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→

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Prune **P**

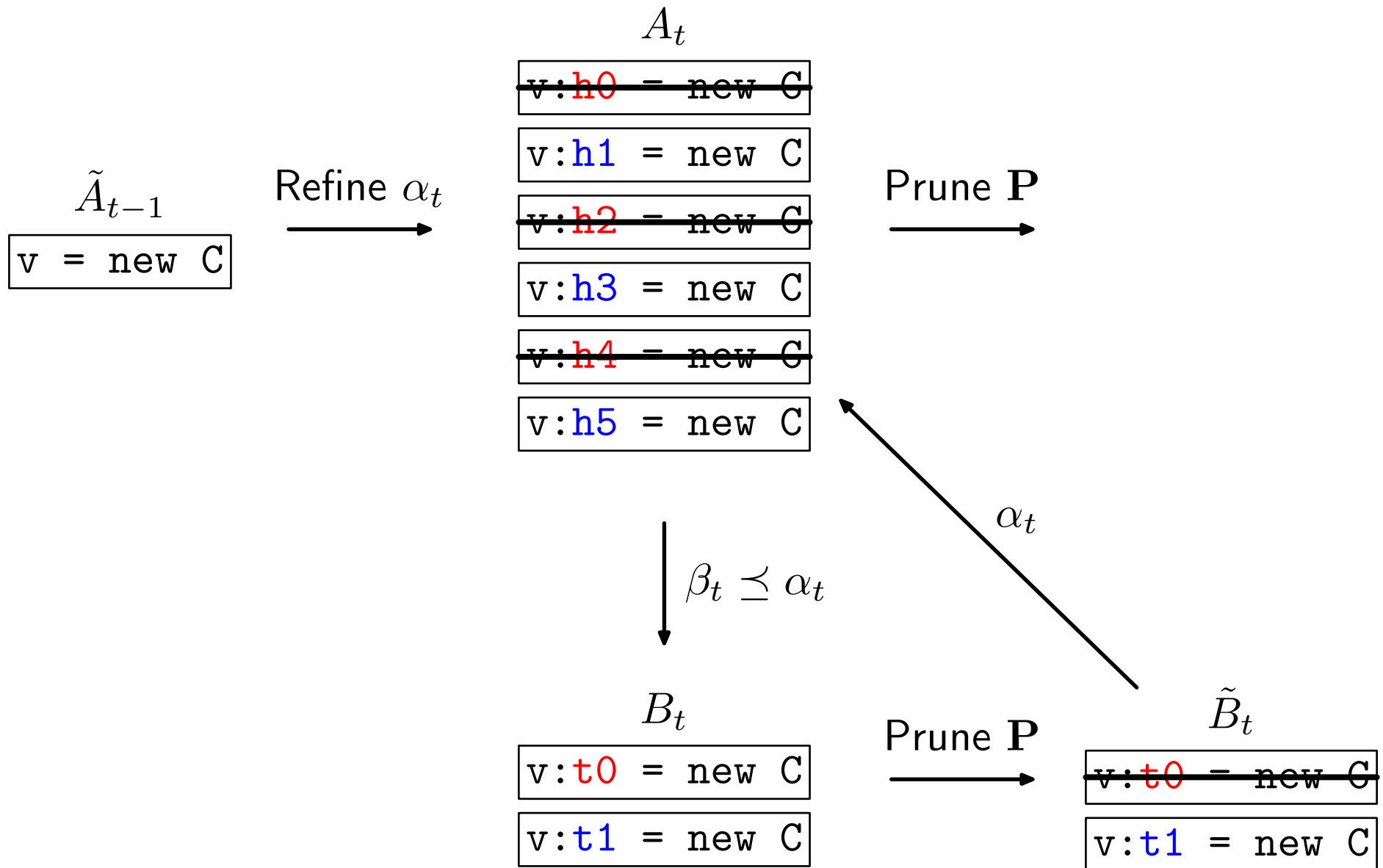
→

$$\tilde{B}_t$$

~~v:t0 = new C~~

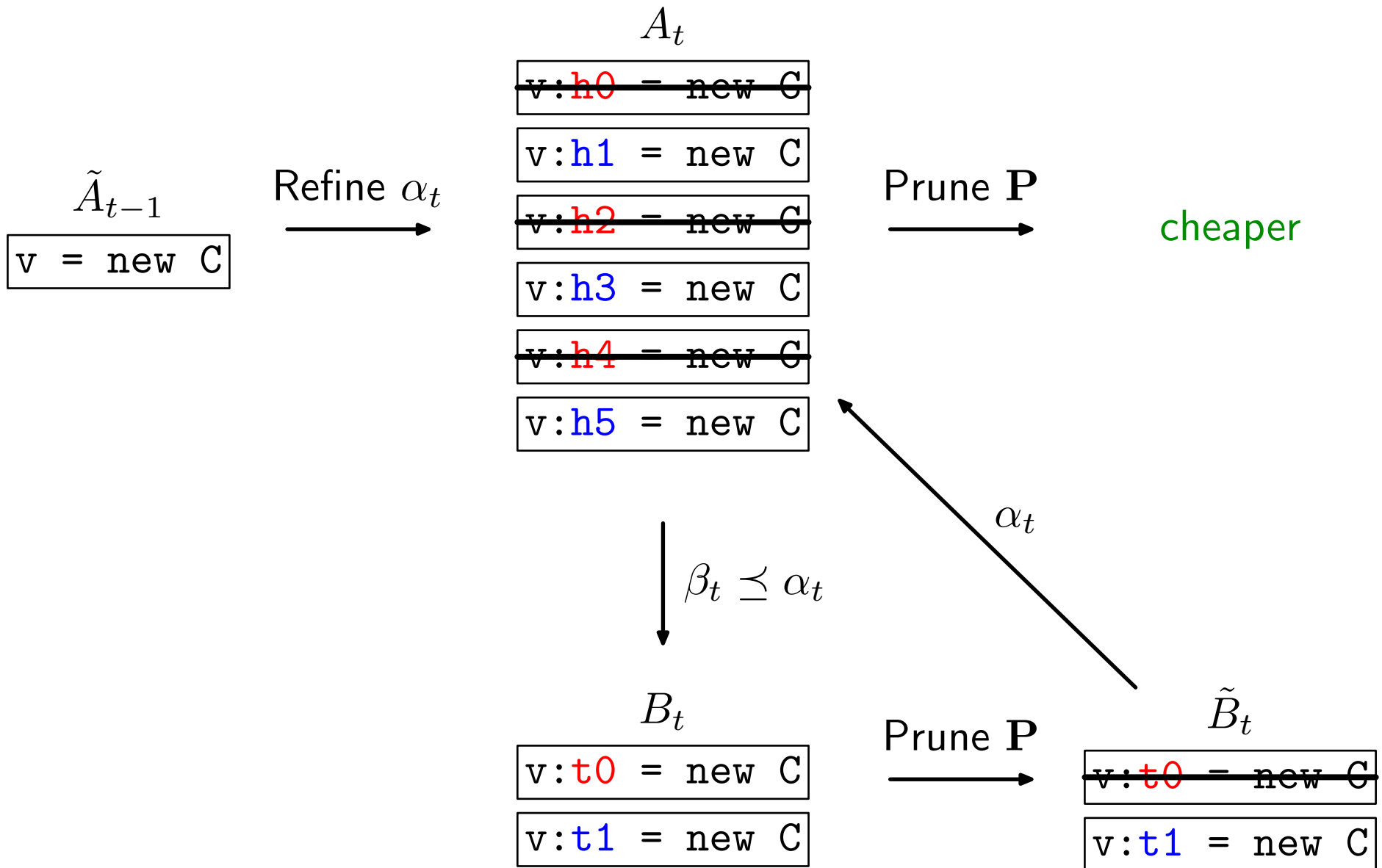
v:t1 = new C

# Pre-Pruning





# Pre-Pruning



# Which Abstractions for Pre-Pruning?

(main)  $\alpha_0 \sqsupseteq \alpha_1 \sqsupseteq \alpha_2 \sqsupseteq \dots$   
 $\Upsilon \mid \quad \quad \Upsilon \mid \quad \quad \Upsilon \mid$

(auxiliary)  $\beta_0 \sqsupseteq \beta_1 \sqsupseteq \beta_2 \sqsupseteq \dots$

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$$\begin{array}{l} \text{(main)} \quad \alpha_0 \sqsupseteq \alpha_1 \sqsupseteq \alpha_2 \sqsupseteq \dots \\ \quad \quad \quad \gamma_1 \quad \quad \quad \gamma_1 \quad \quad \quad \gamma_1 \\ \text{(auxiliary)} \quad \beta_0 \sqsupseteq \beta_1 \sqsupseteq \beta_2 \sqsupseteq \dots \end{array}$$

Choose abstraction  $\tau$ ;

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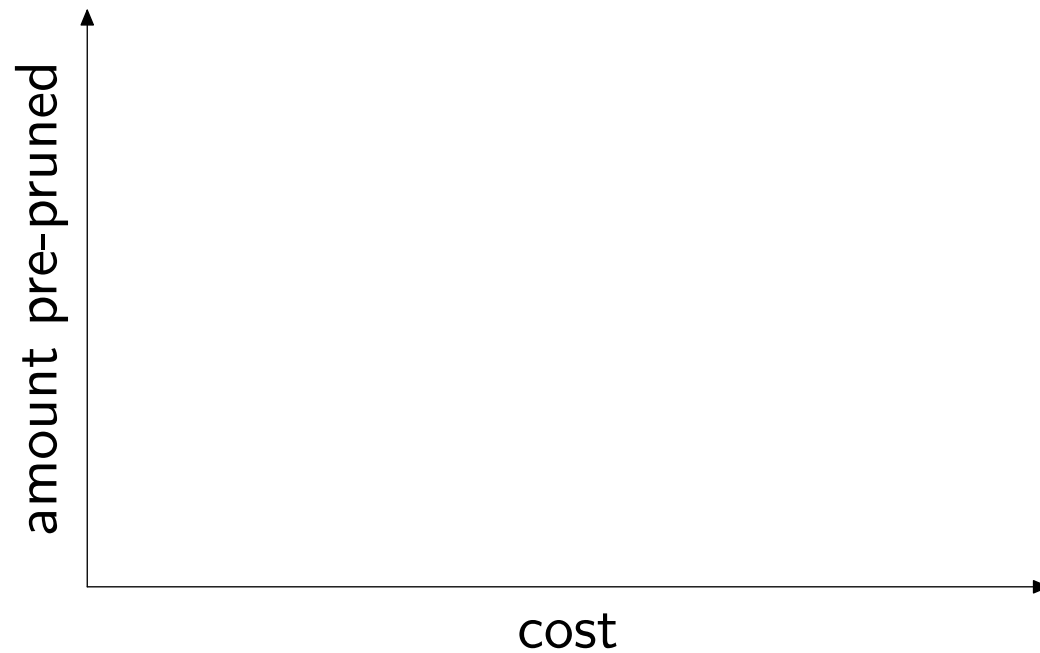
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Choose abstraction  $\tau$ ; set  $\beta_t = \alpha_t \circ \tau$

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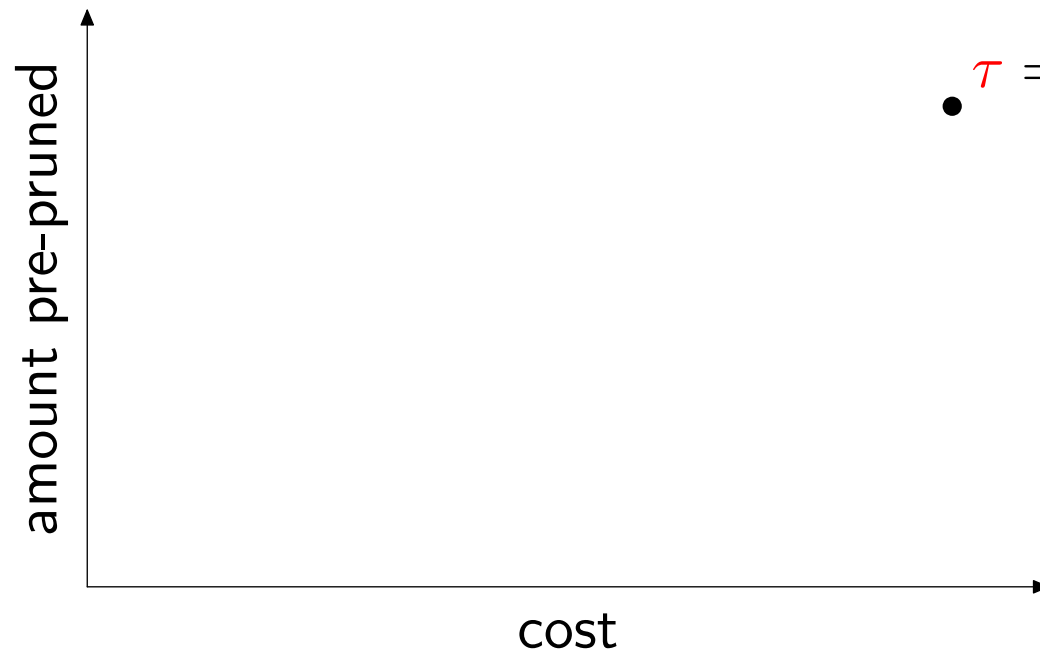
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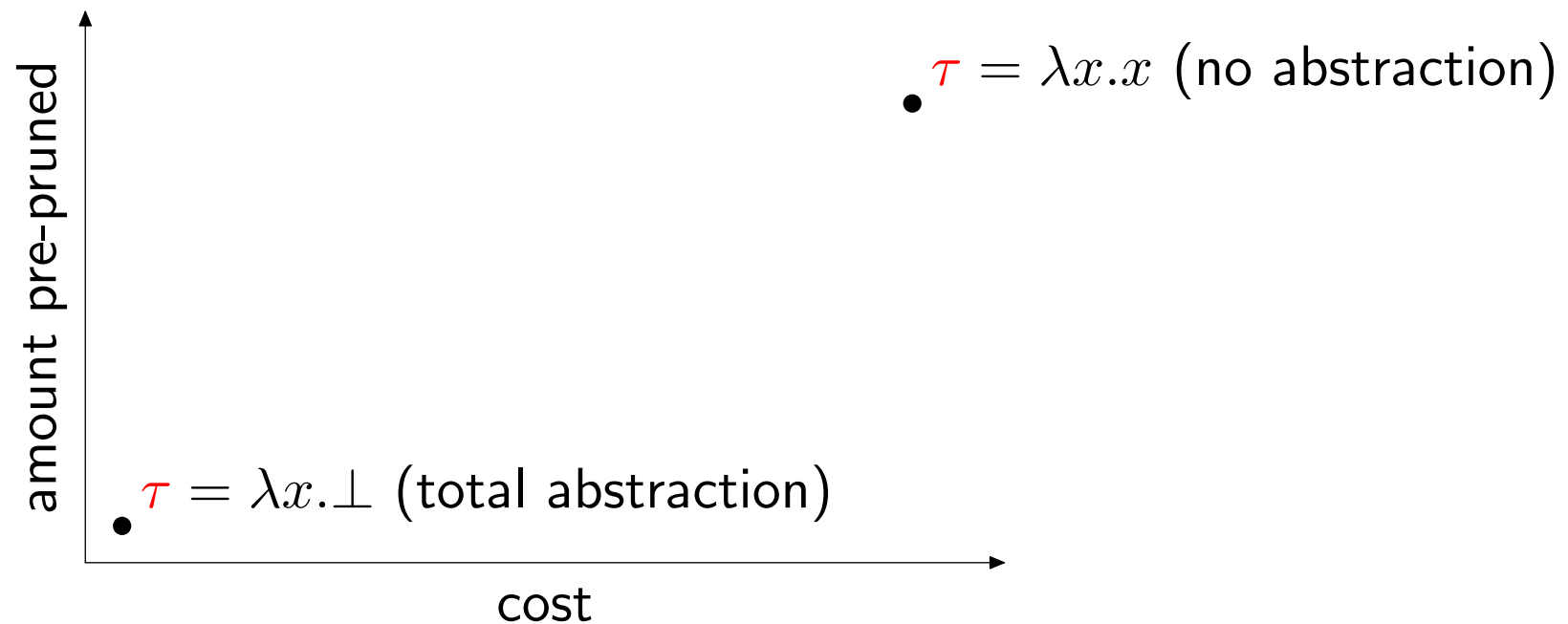


•  $\tau = \lambda x.x$  (no abstraction)

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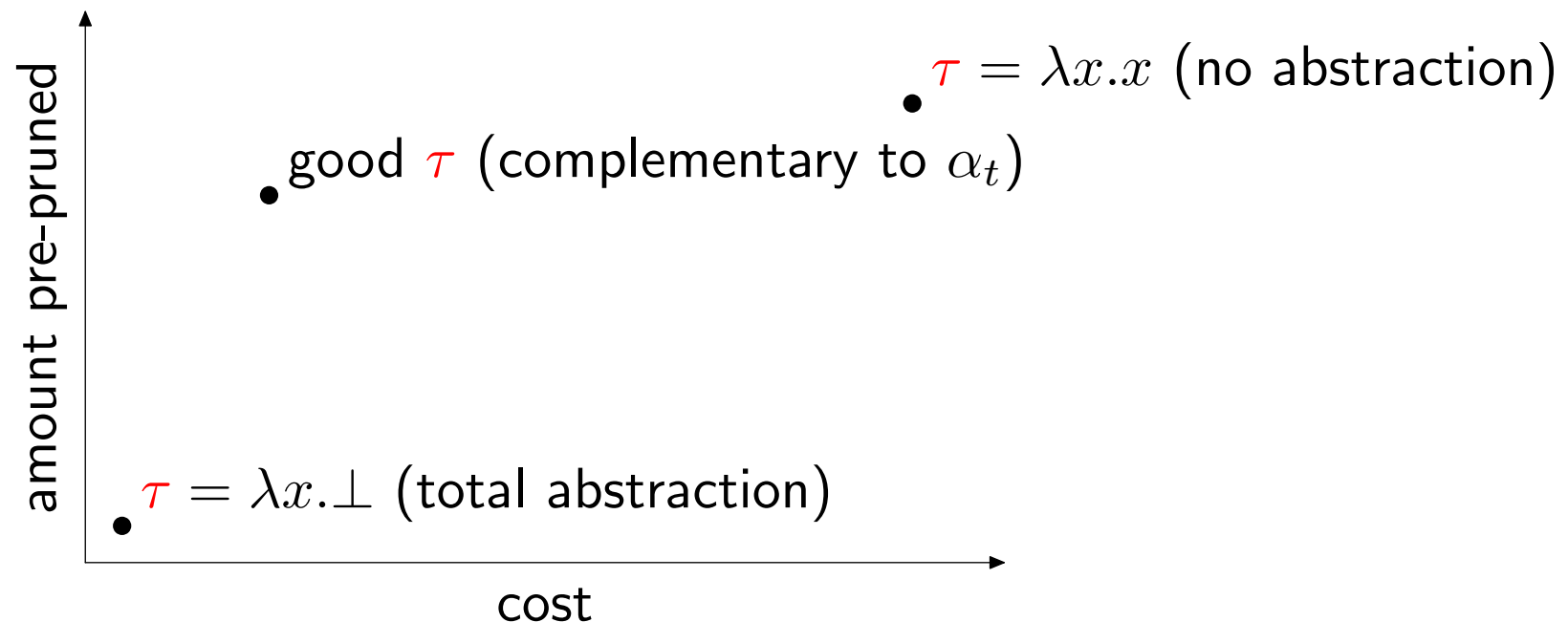
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# Type-Based Abstractions for Pre-Pruning

$k$ -limited:  $\alpha_k = \text{take length } k \text{ prefix}$

$$\boxed{v:h5:h8 = \text{new } C} \xrightarrow{\alpha_1} \boxed{v:h5 = \text{new } C}$$

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Type-based:  $\tau =$  replace alloc. sites with **types** [Smaragdakis et al. 2011]

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class C1 {  
  h1: x = new C2  
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We use  $\tau =$  **type** of containing class  $\times$  **type** of allocation site

```
class C1 {  
h1:   x = new C2  
}
```

$$h1 \xrightarrow{\tau} (C1, C2)$$

# Type-Based Abstractions for Pre-Pruning

$k$ -limited:  $\alpha_k =$  take length  $k$  prefix

$$\boxed{v:h5:h8 = \text{new } C} \xrightarrow{\alpha_1} \boxed{v:h5 = \text{new } C}$$

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$$h1 \xrightarrow{\tau} (C1, C2)$$

Composed:  $\beta_1 = \alpha_1 \circ \tau$

$$\boxed{v:h5:h8 = \text{new } C} \xrightarrow{\beta_1} \boxed{v:t1 = \text{new } C}$$

# Rest of Talk

Pre-Pruning Extension

Experiments

# Experimental Setup

Clients (based on flow-insensitive  $k$ -object-sensitivity):



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## Benchmarks:

	description	# bytecodes	# alloc. sites
elevator	discrete event simulation program	39K	637
hedc	web crawler	151K	1,494
weblech	website downloading and mirroring tool	230K	2,545
lusearch	text indexing and search tool	267K	2,822
avrora	AVR microcontroller simulation/analysis framework	312K	4,823

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## Details:

64-bit IBM J9VM 1.6, Chord with bddb Datalog solver

Terminate a process if it exceeds 8GB of memory

# Curbing the Exponential Growth

Methods:

- | no pruning

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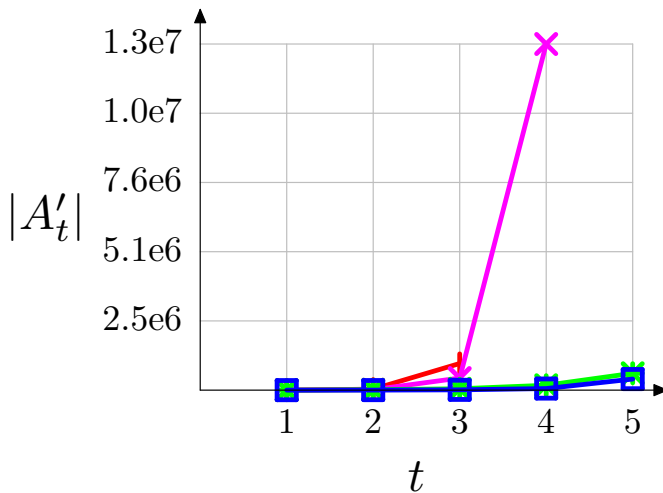
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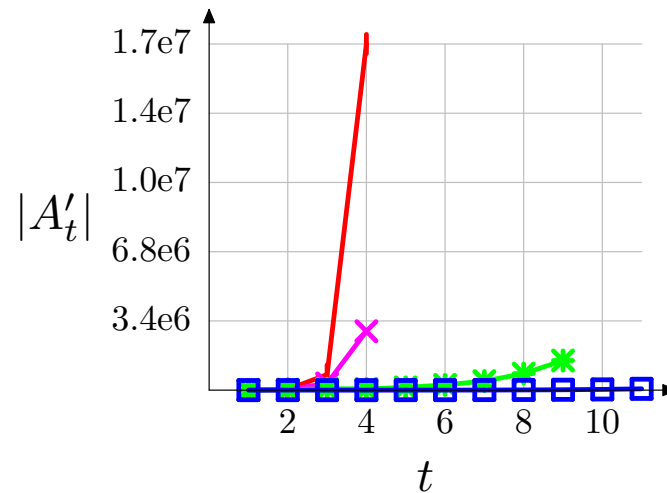
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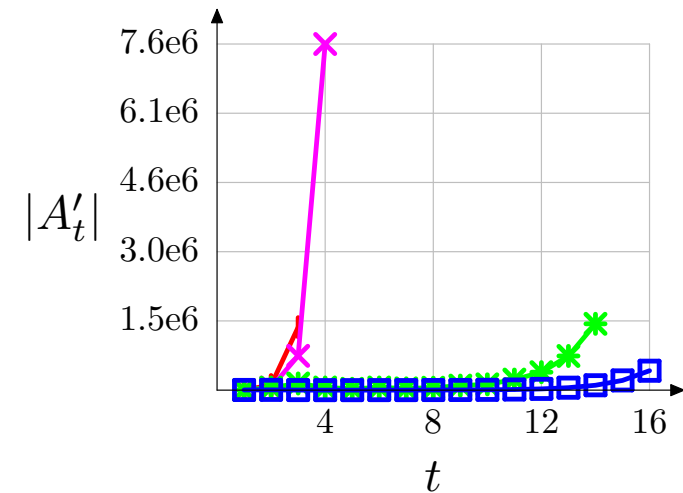
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(a) DOWNCAST/weblech



(b) DOWNCAST/lusearch



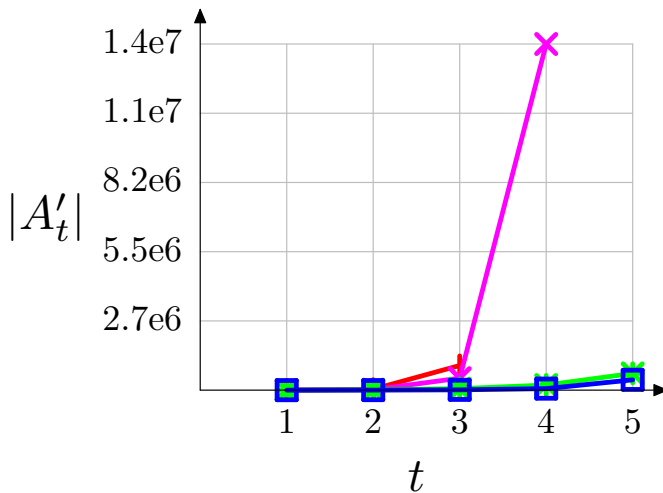
(c) DOWNCAST/avrora

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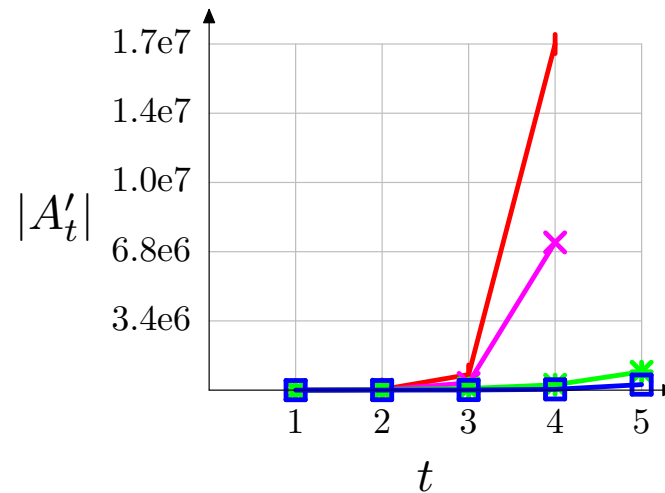
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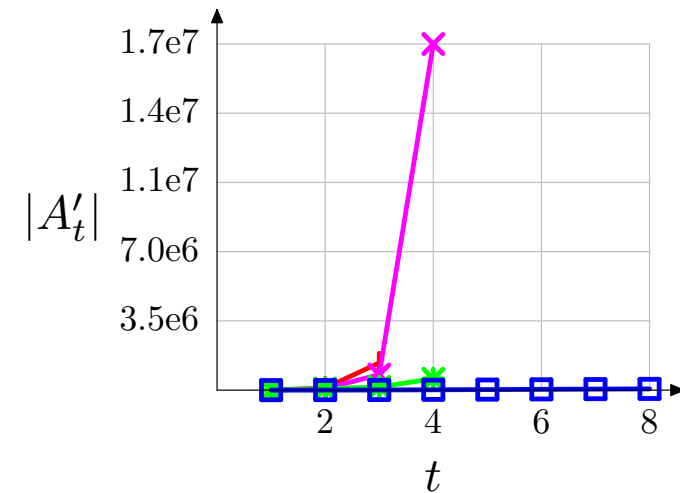
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(a) MONOSITE/weblech



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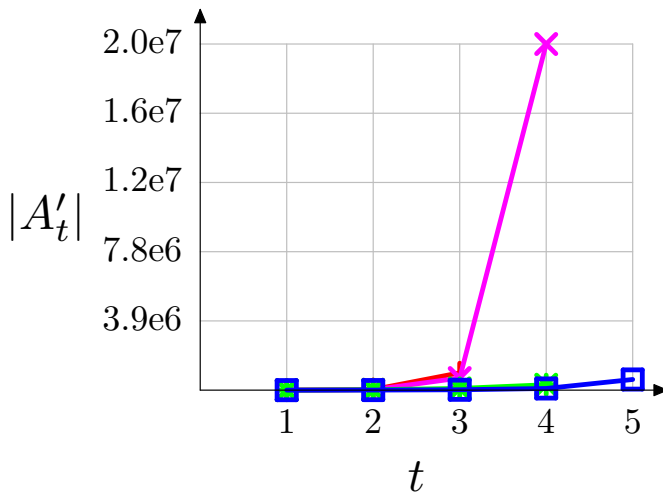
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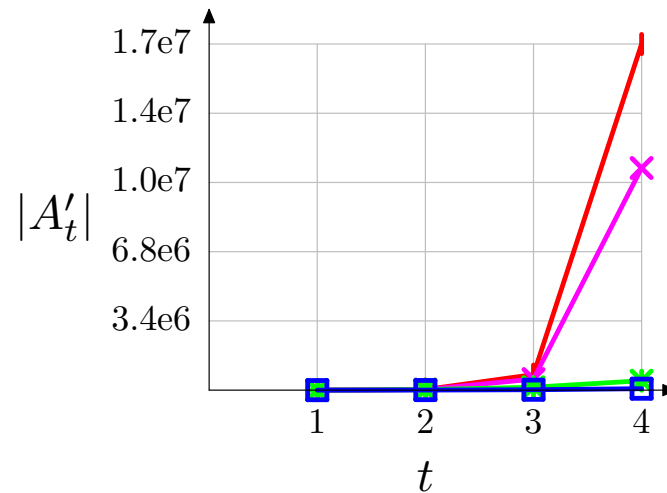
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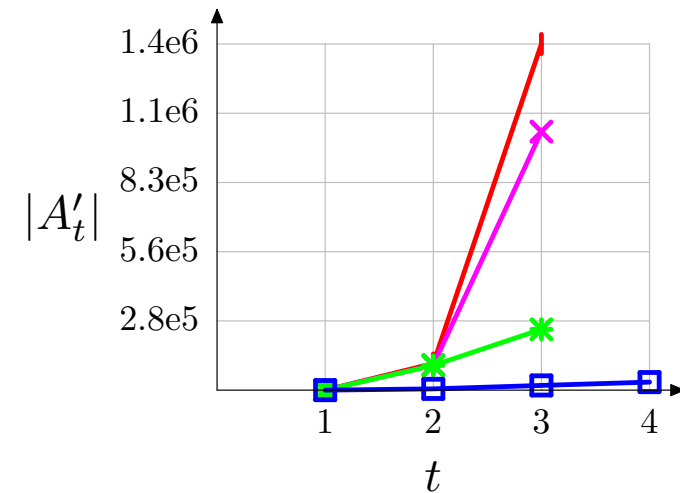
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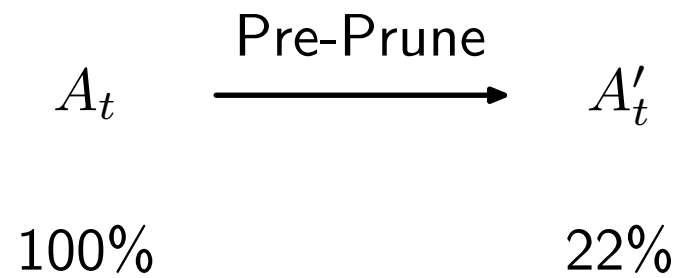
In each iteration, what fraction of tuples are kept?

$A_t$

100%

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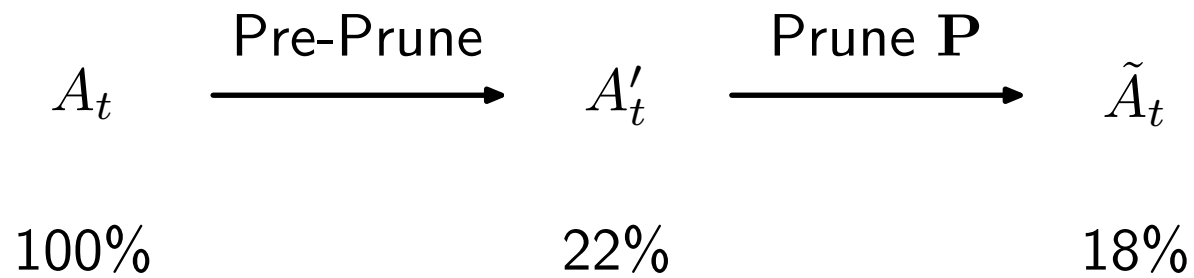
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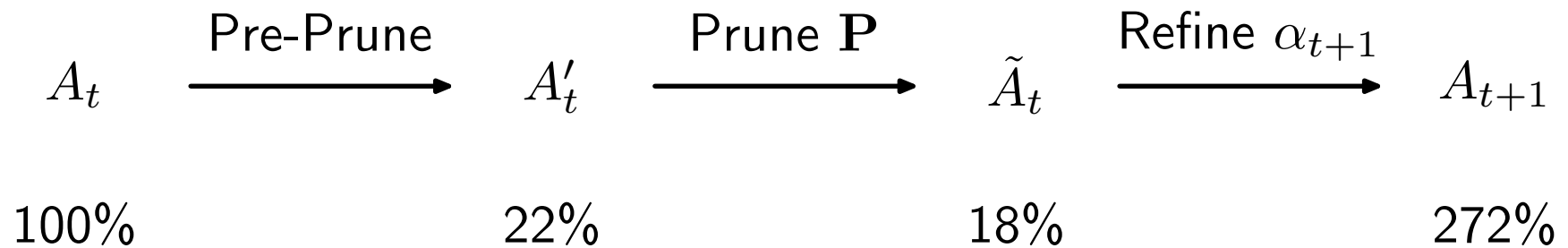
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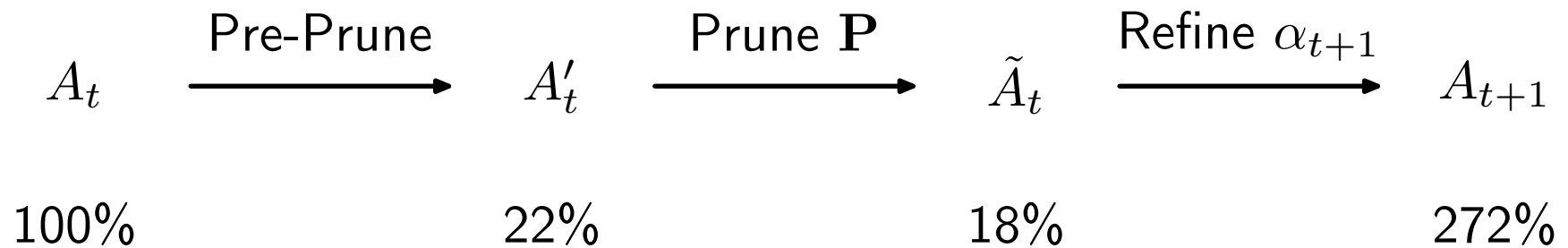
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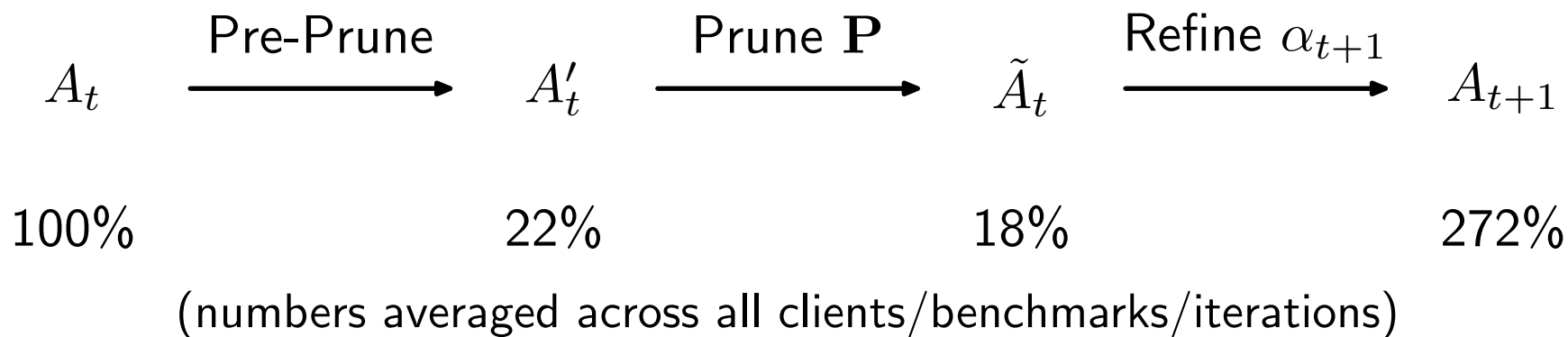
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(numbers averaged across all clients/benchmarks/iterations)

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**Take Away:** Pruning (especially pre-pruning) helps a lot to maintain tractability

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DOWNCAST/hedc	10	8	3	<b>2</b>	<b>2</b>
DOWNCAST/weblech	24	14	6	<b>6</b>	-
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DOWNCAST/avrrora	12	10	6	<b>6</b>	<b>6</b>
MONOSITE/elevator	1	1	1	1	1
MONOSITE/hedc	164	149	149	<b>149</b>	-
MONOSITE/weblech	273	258	252	<b>252</b>	-
MONOSITE/lusearch	593	454	447	<b>447</b>	-
MONOSITE/avrrora	288	278	272	-	-
RACE/elevator	475	440	437	437	437
RACE/hedc	23,033	22,043	21,966	-	-
RACE/weblech	7,286	4,742	4,669	-	-
RACE/lusearch	33,845	23,509	16,957	-	-
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**Take Away:** By using Prune-Refine, able to prove two additional queries

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<http://code.google.com/p/jchord>

Thank you!