

Global Time

Insup Lee
Department of Computer and Information Science
School of Engineering and Applied Science
University of Pennsylvania
www.cis.upenn.edu/~lee/



CIS 541, Spring 2010

Ordering in the Distributed Real-Time System

- The distributed computer system performs a multitude of different functions concurrently.
 - The monitoring of RT-entities
 - The detection of alarm conditions
 - The display of the observations
 - The execution of control algorithms
- All nodes process all events in the same consistent order.
 - To guarantee a consistent behavior of the entire distributed system ♪

Temporal Order

- A timeline consists of an infinite set $\{T\}$ of *instants* with the following properties.
 - $\{T\}$ is an ordered set, if p and q are any two instants, then either p is simultaneous with q , or p precedes q , or q precedes p , where these relations are mutually exclusive. We call the order of instants on the timeline the temporal order.
 - $\{T\}$ is a dense set : There is at least one q between p and r iff p is not the same instance as r , where p , q and r are instants.
- A section of the time line is called a *duration*.
- An *event* takes place at an instant of time.
- If two events occur at an identical instant, then the two events are said to occur *simultaneously*.

Causal Order

- In many real-time applications, the causal dependencies among events are of interests.
 - A nuclear reactor equipped with many sensors.
 - In case a pipe ruptures, what is the primary event that triggers the alarm shower?
 - The temporal order of two events is necessary, but not sufficient, for their *causal* order.
- Causal order is more than temporal order.

Delivery Order

- A weaker order relation than temporal or causal order is a consistent **delivery order**.
- All host computers in the nodes see the sequence of events in the same delivery order.
- The delivery order is not necessarily related to the temporal order or the causal relationship between events.

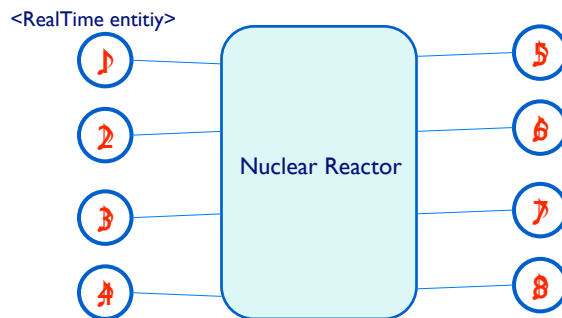
Spring '10

CIS 541

5

Why need Temporal Order in Real-Time Systems?

- In case of sudden unexpected changes in the nuclear reactor, system causes an *alarm shower*.
- What is the primary event that triggers the alarm shower?
 - Knowledge of the exact temporal order is helpful to identify the primary event.



6

Issues in the Temporal Order

- What is the condition to reconstruct temporal order between two events?
- Need the following concepts
 - Clocks
 - Physical clock
 - Reference clock
 - Timestamp
 - Offset , Precision and Accuracy
 - Time measurement
 - Global Time
 - Reasonableness Condition of Global Time
 - Condition to reconstruct temporal order.

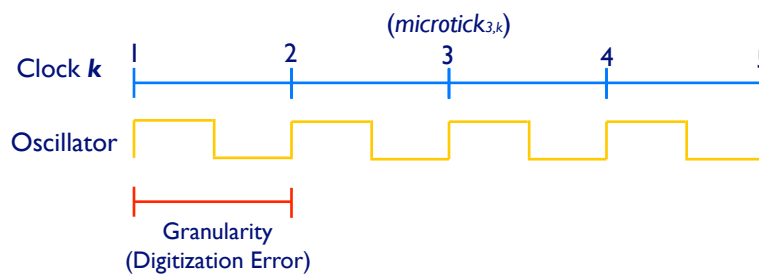
Spring '10

CIS 541

7

Clocks : Physical Clock

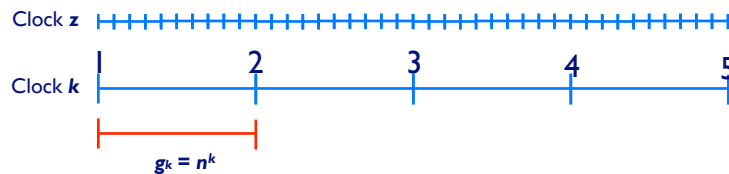
- Physical Clock
 - A device for measuring time with counter and a physical oscillation mechanism.
 - **Microtick** : The periodic event generated by a oscillation mechanism. (Denoted by $microtick_{i,k}$ for i th microtick of clock k)
 - **Granularity** : The duration between two consecutive microticks.♪



8

Clocks : Reference Clock

- Reference Clock
 - Assume an *omniscient external observer* who can observe all events that are of interest in a given context.
 - A unique reference clock **z** with granularity g_z which is in perfect agreement with the international standard of time.
 - (Assume g_z is really really really small, say 10^{-15} second)
- The relationship between reference clock **z** and a given clock **k**
 - n^k : a nominal number of microticks of clock **z** which occur between **microtick_{i,k}** and **microtick_{i+1,k}**



9

Clocks : Timestamp

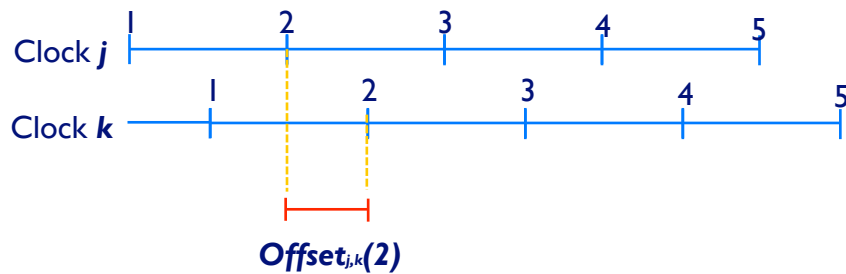
- **Clock(event)** : denotes the **timestamp** generated by the use of a given clock to timestamp an event.
 - Ex) **z(e)** : The timestamp of event **e** which is observed by clock **z** (the absolute timestamp)
- What if the interval of two events is less than g_z ?
 - The temporal order of events that occur between any two consecutive microticks of the reference clock **z** cannot be reestablished from their absolute timestamps.
 - => *Limitation of this time measurement.*

10

Clocks : Offset

- Offset

- The offset at microtick i between two clocks j and k with the same granularity.
- $\text{Offset}_{j,k}(i) = |z(\text{microtick}_{i,j}) - z(\text{microtick}_{i,k})|$



12

Clocks : Precision

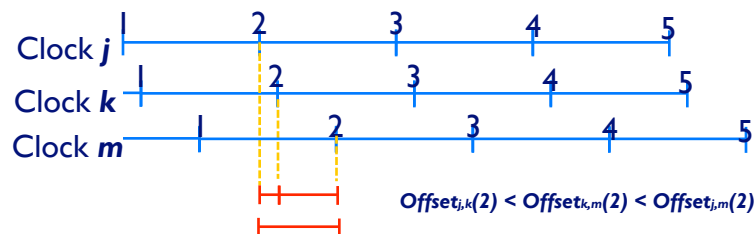
- Precision

- Given an ensemble of clocks $\{1, 2, \dots, n\}$, the maximum offset between any two clocks of the ensemble

$$\square_i = \max\{\text{offset}_{j,k}(i)\} \text{ for all } 1 \leq j, k \leq n$$
- The precision of ensemble \square : the maximum \square_i of over an interval of interest.

- Internal synchronization

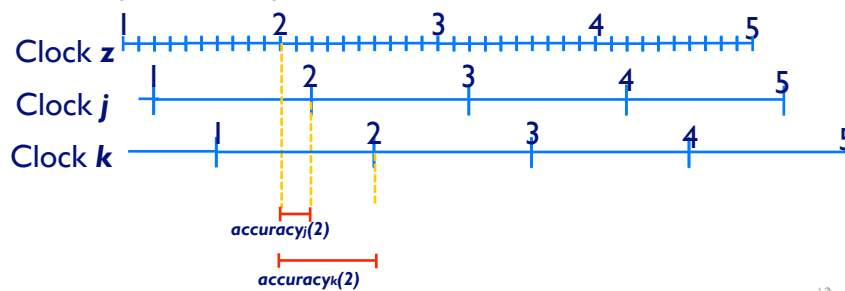
- The process of mutual resynchronization of an ensemble of clocks to **maintain a bounded precision**



12

Clocks : Accuracy

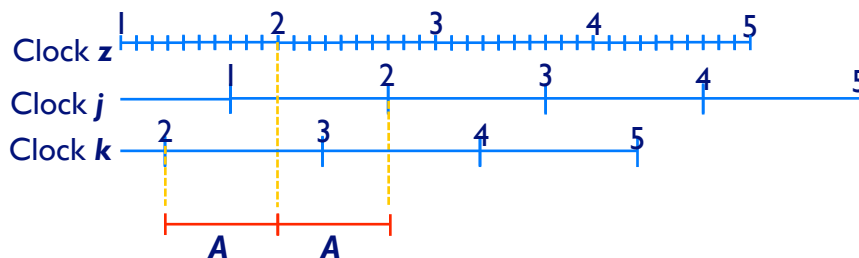
- Accuracy
 - $accuracy_k(i)$: The offset of clock k with respect to the reference clock z at microtick i
 - $accuracy_k$: The maximum offset over **all microticks** i that are of interest in clock k
- External synchronization
 - The process of resynchronization of a clock with the reference clock z



10

Clocks : Precision and Accuracy

- Relationship between Precision and Accuracy
 - If all clocks are **externally** synchronized with an **accuracy** A , then the clocks are also **internally** synchronized with a **precision** of **at most $2A$** .
 - *The converse is not true*



10

Time Measurement

- Easiest way to achieve temporal order of every event
 - Having a perfect synchronization with a single reference clock z among all real-time clocks of nodes
- Challenge
 - In loosely coupled distributed system, every node has its own local clock.
 - A tight synchronization of clocks is not possible.
- The concept of *global time*
 - A weaker notion of a universal time reference
 - With local clock, achieve **local implementation of a global notion of time.**

10

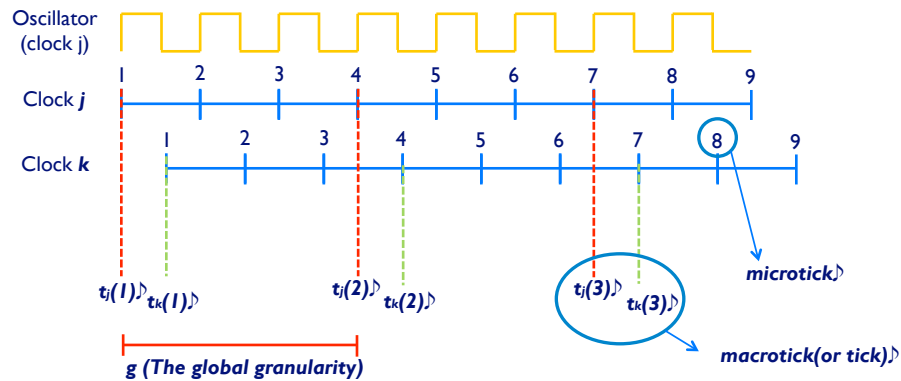
Global Time(1/2)

- How to achieve the local implementation of a global notion of time?
- Assumption
 - Each node has its own local physical clock c_k with granularity g_k .
 - All local clocks are internally synchronized with a precision \square .
$$|z(\text{microtick}_j(i)) - z(\text{microtick}_k(i))| < \square$$
for any two clocks j, k and all microticks i
- Macrotick
 - A subset of the *microticks* of each local clock.
 - The local implementation of a global notion of time.
 - Ex) Every tenth microtick of a local clock k may be interpreted as the global tick, the macrotick $t_k(i)$.

10

Global Time(2/2)

- Illustration of the relationship between microtick and macrotick.



12

Reasonableness Condition(1/3)

- The global time t is called **reasonable**.
 - If all local implementations of the global time satisfy the condition

$$g > \Pi$$

- The impact of reasonable condition
 - The synchronization error is bounded to less than **one macrogranule g** .
 - For a single event e , that is observed by any two different clocks which satisfy the reasonable condition

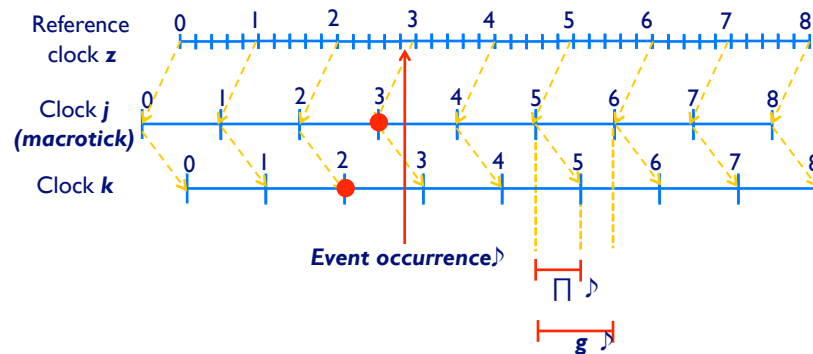
$$|t_j(e) - t_k(e)| \leq 1$$

- i.e. the global timestamps for a single event can differ by at most one tick. **This is the best we can achieve.**

13

Reasonableness Condition(2/3)

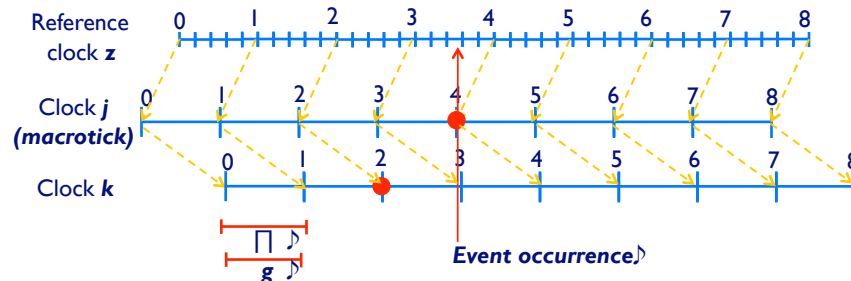
- Illustration of the reasonableness condition ($g > \Delta$)
 - Timestamp of a single event, $|t_j(e) - t_k(e)| \leq I$



19

Reasonableness Condition(3/3)

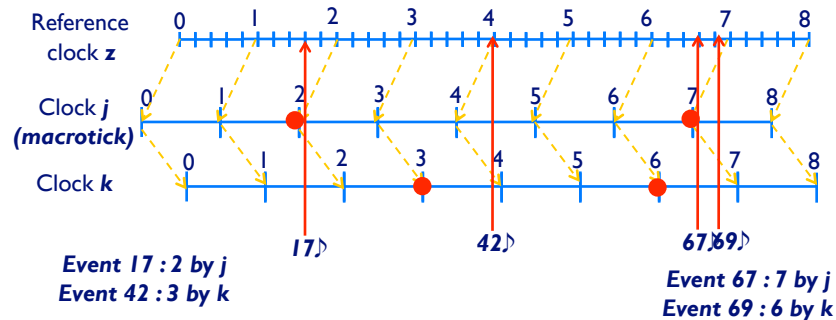
- Illustration of the impact unless the reasonableness condition meets.
 - Timestamp of a single event $|t_j(e) - t_k(e)| > I$ at some point. (not all points.)



20

The meaning of one tick difference

- Both duration (17, 42), (67, 69) observed by clock j and k have one tick difference.
- Problem ? $z(67) < z(69)$, but $t_k(67) > t_k(69)$
 - Because of the accumulation of the synchronization error and the digitalization error.♪



22

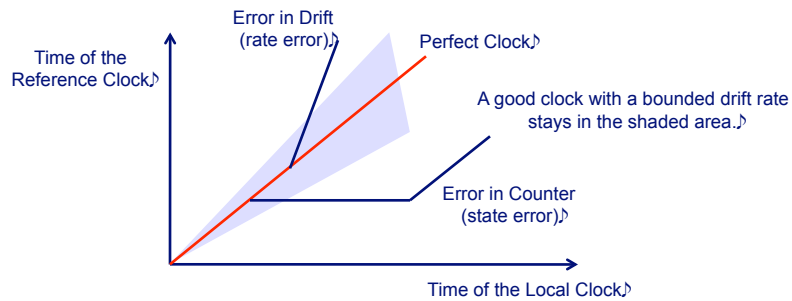
The Condition to Reconstruct Temporal Order

- One tick difference between two events
 - Not possible to reconstruct the temporal order.
 - (We are not sure : Some of them can be reconstructed, but some cannot be.)
- Two tick difference between two events
 - The temporal order can be reconstructed.
 - (Guaranteed : All such events can be reconstructed.)
 - WHY? **The sum of the synchronization and digitalization error is always less than 2 granules.♪**

22

Why need Clock Synchronization?

- Failure modes of a clock
 - Error in Counter (state error)
 - Error in Drift (rate error)



Spring '10

CIS 541

23

Internal Clock Synchronization

- The parameters for synchronization condition
 - Resynchronization interval : R_{int}
 - Convergence function : the offset of the time values immediately after the resynchronization.
 - Drift offset : the maximum divergence of any two good clocks from each other during R_{int} .
 - The maximum specified drift rate : ρ

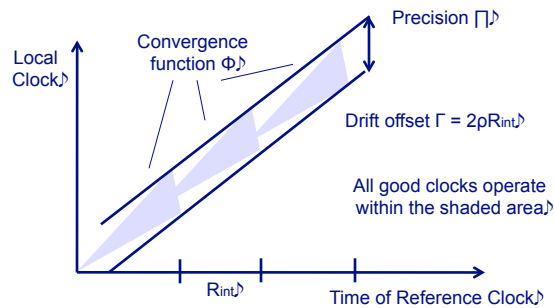
Spring '10

CIS 541

24

The Synchronization Condition

- The synchronization condition
 - $\Phi + \Gamma \leq \Pi$
- =>The synchronization algorithm must bring the clocks so close together that the amount of divergence during the next resynchronization interval will not cause a clock to leave the precision interval



Spring '10

CIS 541

25

Synchronization Algorithms (I)

- The goal is to achieve the synchronization condition.
- Central Master Synchronization
 - A unique node, the central master, periodically sends the value of its time counter in synchronization messages to all other nodes, the slave nodes.
 - The slave node corrects the clock based on the master's time and the latency of the message.

Spring '10

CIS 541

26

Synchronization Algorithms (2)

- **Distributed Synchronization Algorithms**
 - Step 1) Every node acquires knowledge about the state of the global time counters in all the other nodes.
 - Step 2) Every node analyzes the collected information to detect errors, and calculate a correction value for the local global time counter.
 - Step 3) The local time counter of the node is adjusted by the calculated correction value.

External Clock Synchronization

- **External synchronization links the global time of a cluster to an external standard of time.**
 - Time server
 - GPS
- **Internal and external synchronization**
 - Internal sync. : a cooperative activity among all the members of a cluster.
 - External sync. : an authoritarian process (the time server forces its view of external time on all its subordinates.) ♪

Clock Synchronization

- State correction
- Rate correction

Event-Triggered versus Time-Triggered

- Chap 4.4 (pp. 82-86)
- Event-triggered (ET) system – the control signal derived from state change, an event, in the environment or within the computer system
- Time-triggered (TT) system – the control signal derived from the progression of time
- Example in Elevator
 - Two buttons pushed repeatedly, very closed to each other