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# Real-Time Scheduling

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CIS700

Insup Lee

# Outline

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- Real-time systems
- Real-time scheduling algorithms
  - Fixed-priority algorithm (RM)
  - Dynamic-priority algorithm (EDF)

# Real-Time Systems

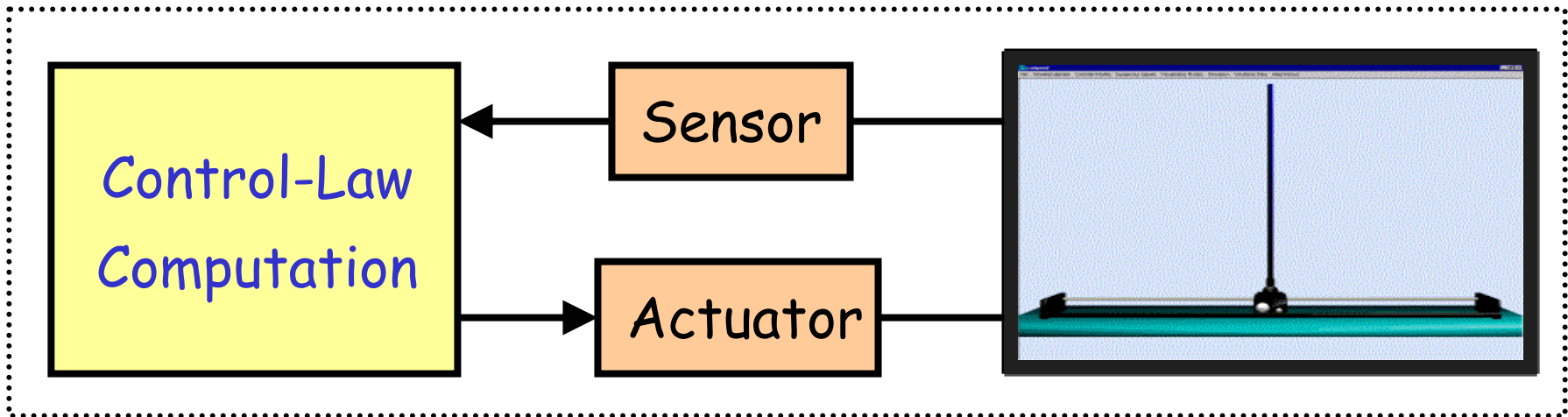
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- Definition
  - Systems whose correctness depends on their **temporal** aspects as well as their **functional** aspects
- Performance measure
  - **Timeliness** on timing constraints (deadlines)
  - Speed/average case performance are less significant.
- Key property
  - **Predictability** on timing constraints

# Real-Time System Example

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- Digital control systems
  - periodically performs the following job:  
*senses* the system status and  
*actuates* the system according to its current status



# Real-Time System Example

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- Multimedia applications
  - periodically performs the following job:  
*reads, decompresses, and displays* video and audio streams

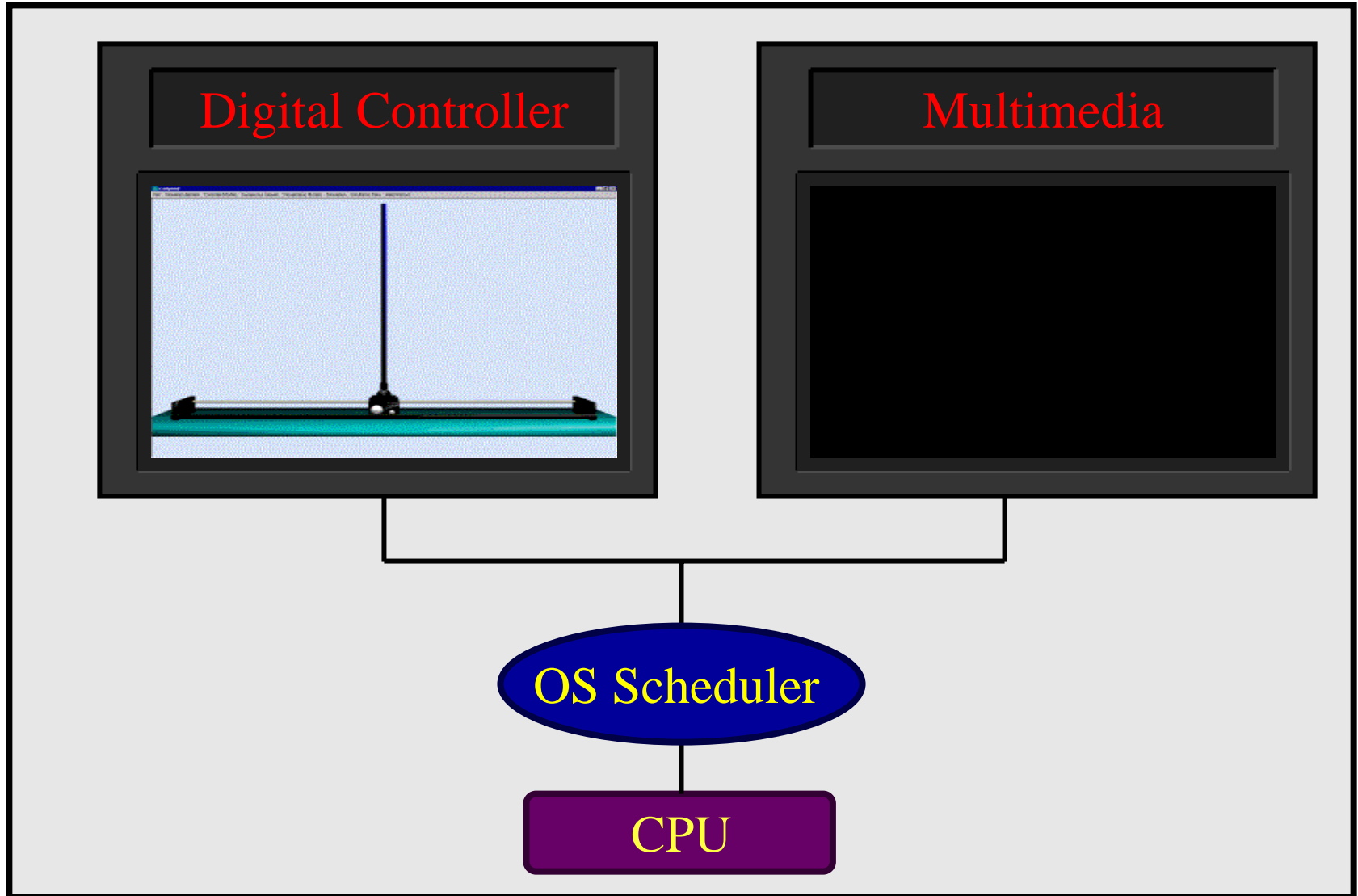


# Fundamental Real-Time Issue

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- To specify the timing constraints of real-time systems
- To achieve predictability on satisfying their timing constraints, possibly, with the existence of other real-time systems

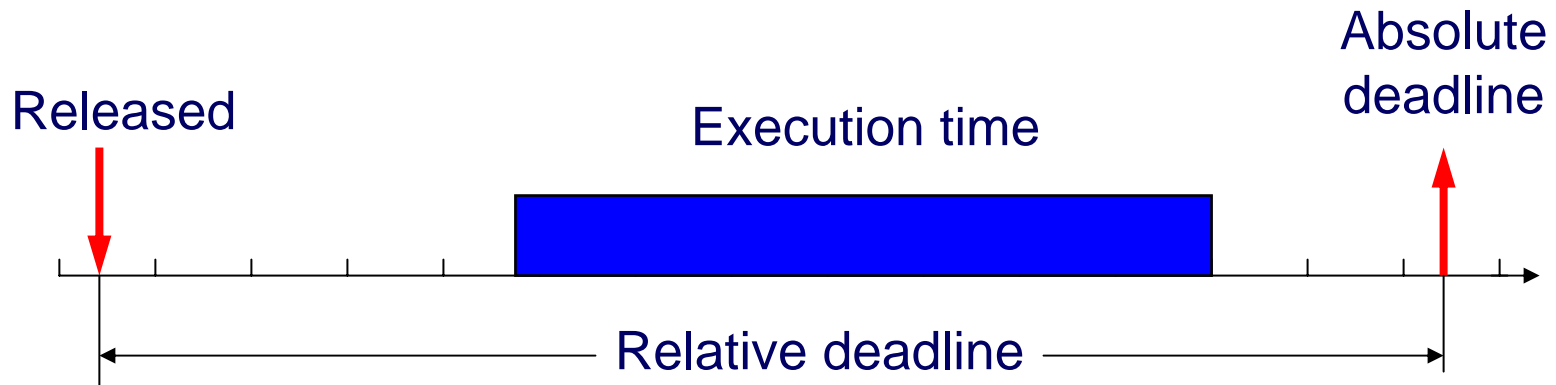
# Scheduling Framework Example



# Real-Time Workload

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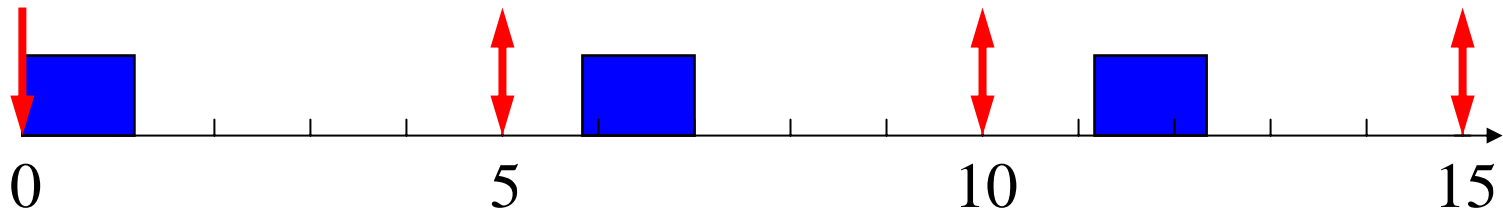
- Job (unit of work)
  - a computation, a file read, a message transmission, etc
- Attributes
  - Resources required to make progress
  - Timing parameters





# Real-Time Task

- Task : a sequence of similar jobs
  - Periodic task  $(p, e)$ 
    - Its jobs repeat regularly
    - Period  $p =$  inter-release time  $(0 < p)$
    - Execution time  $e =$  maximum execution time  $(0 < e < p)$
    - Utilization  $U = e/p$



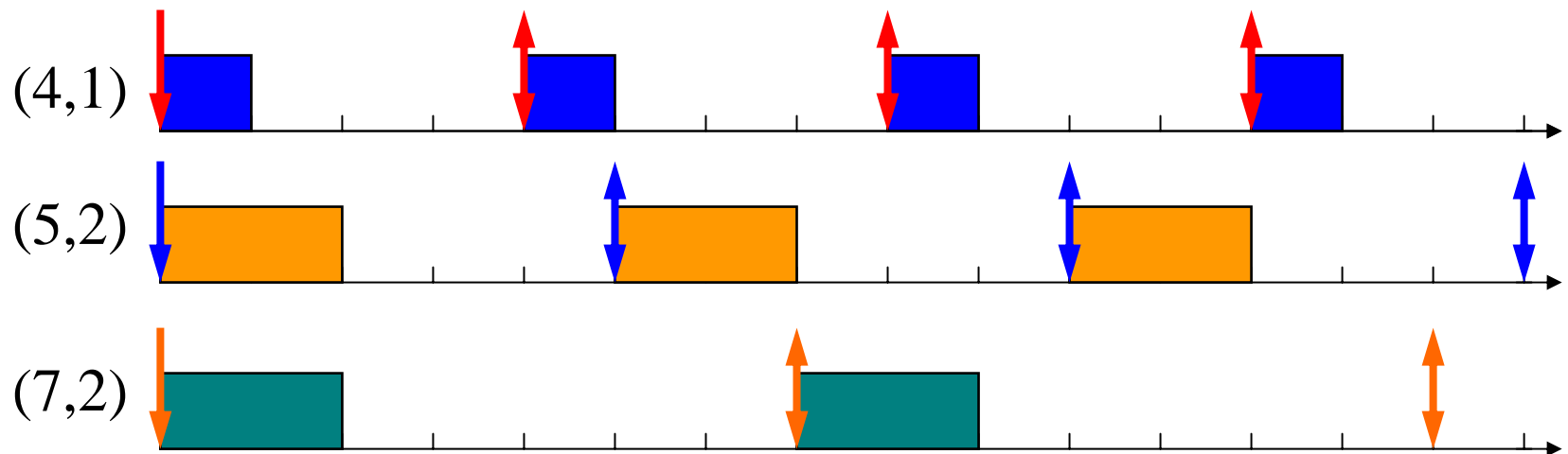
# Deadlines: Hard vs. Soft

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- **Hard** deadline
  - Disastrous or very serious consequences may occur if the deadline is missed
  - Validation is essential : can **all** the deadlines be met, even under worst-case scenario?
  - Deterministic guarantees
- **Soft** deadline
  - Ideally, the deadline should be met for maximum performance. The performance degrades in case of deadline misses.
  - Best effort approaches / statistical guarantees

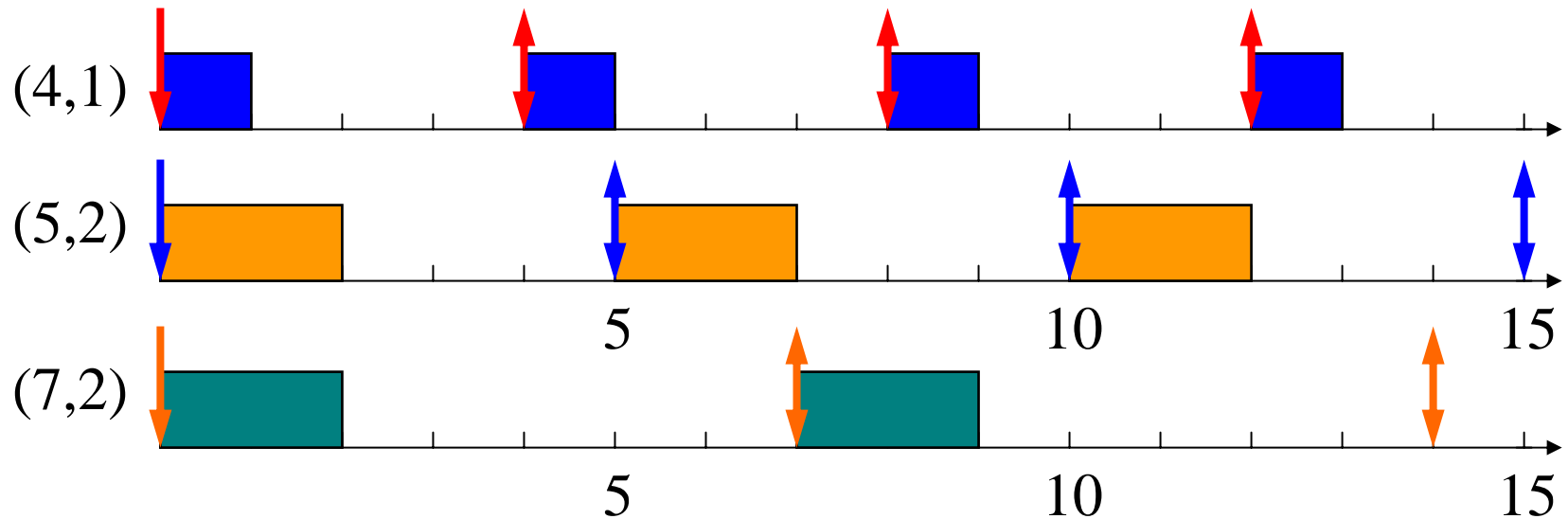
# Schedulability

- Property indicating whether a real-time system (a set of real-time tasks) can meet their deadlines



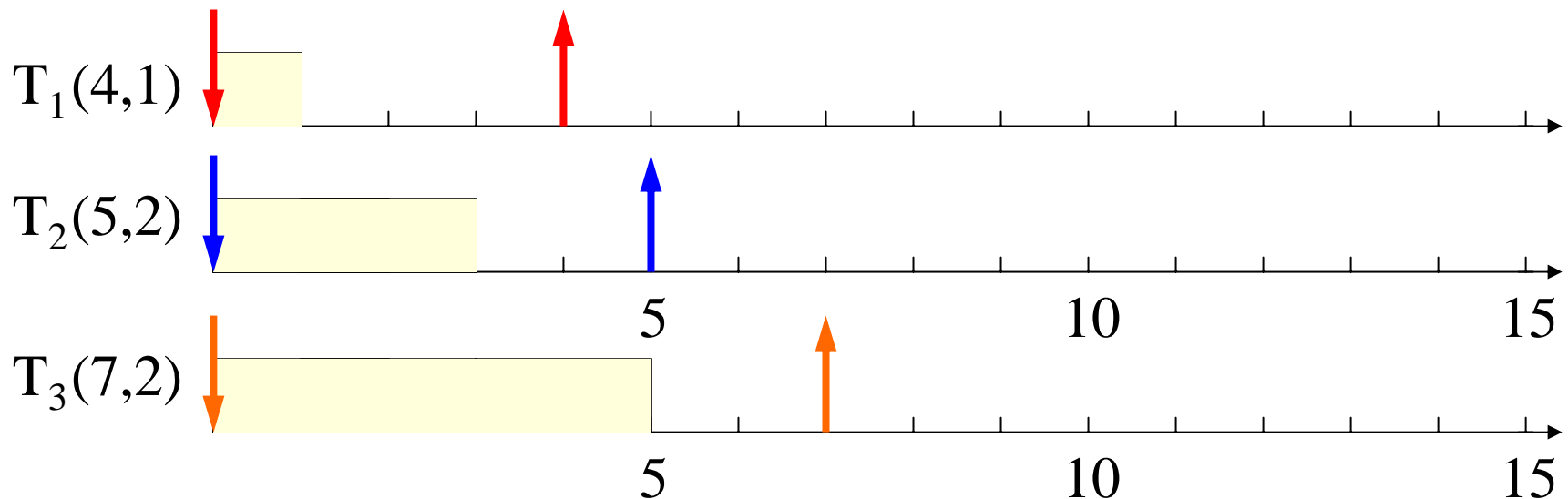
# Real-Time Scheduling

- Determines the order of real-time task executions
- Static-priority scheduling
- Dynamic-priority scheduling



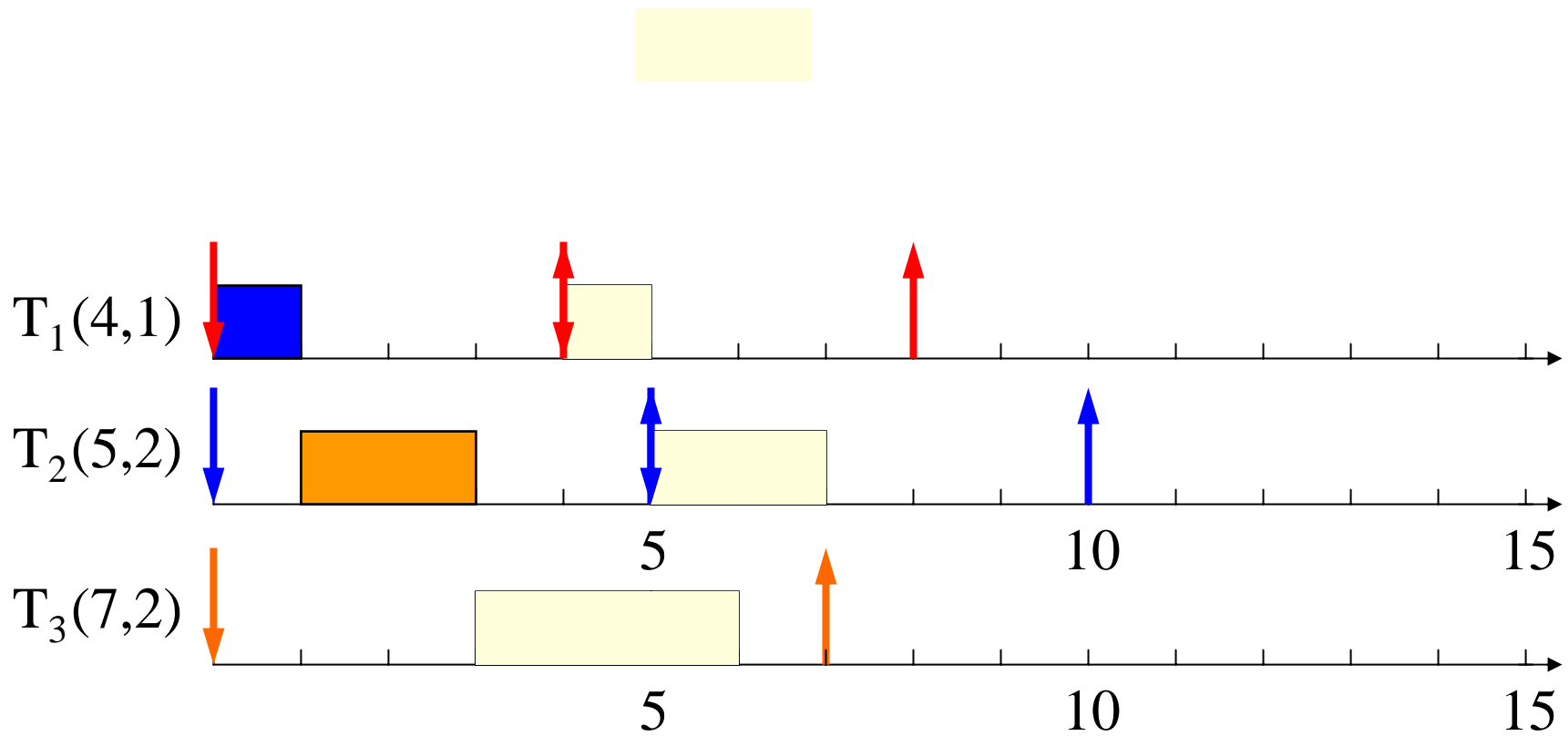
# RM (Rate Monotonic)

- Optimal static-priority scheduling
- It assigns priority according to period
- A task with a shorter period has a higher priority
- Executes a job with the shortest period



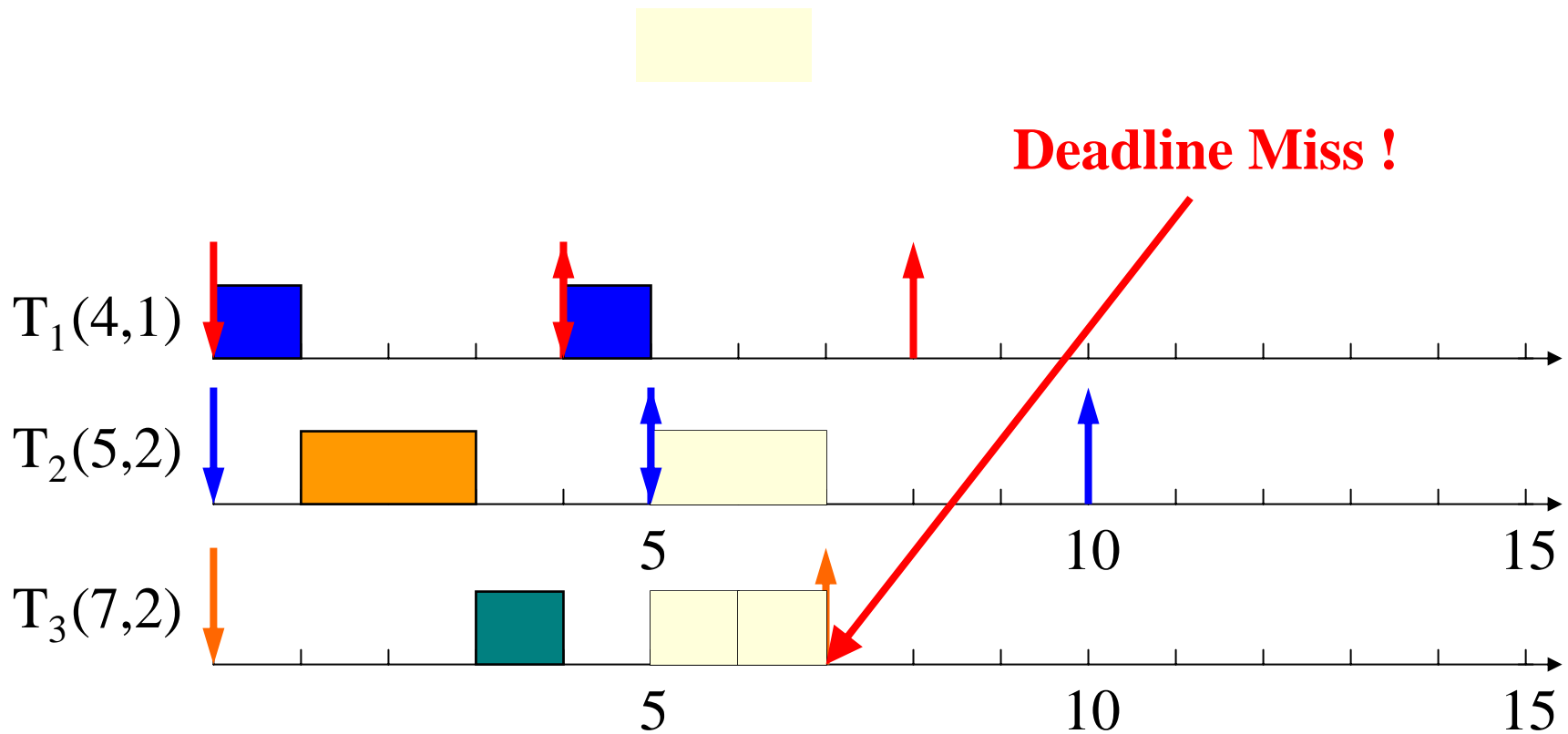
# RM (Rate Monotonic)

- Executes a job with the shortest period



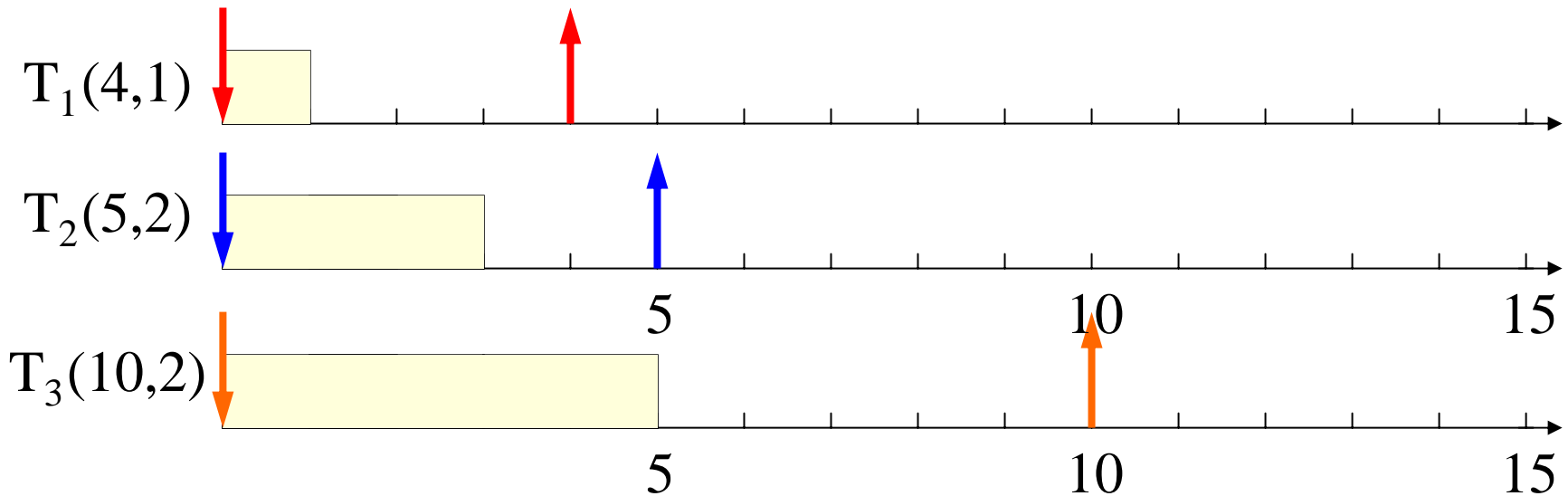
# RM (Rate Monotonic)

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# Response Time

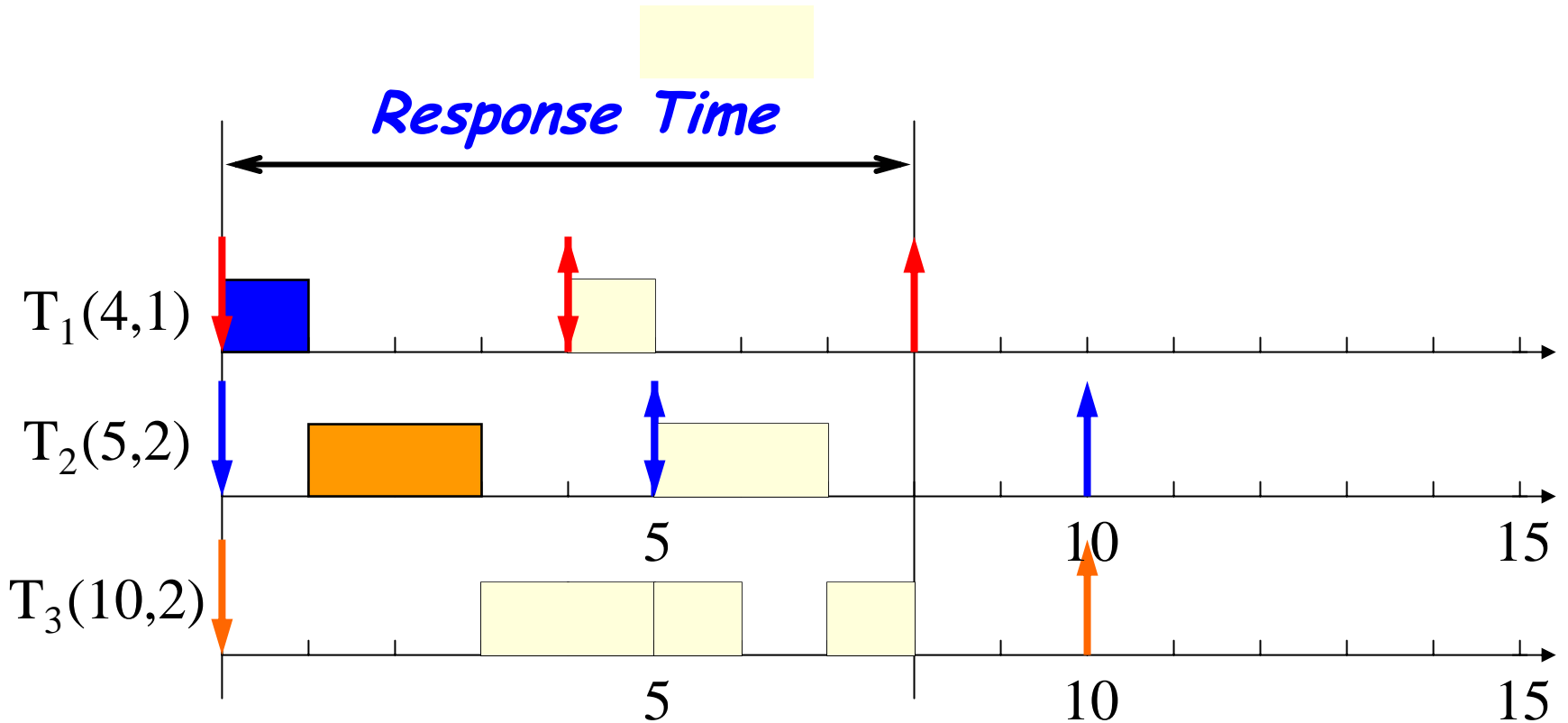
- Response time
  - Duration from released time to finish time





# Response Time

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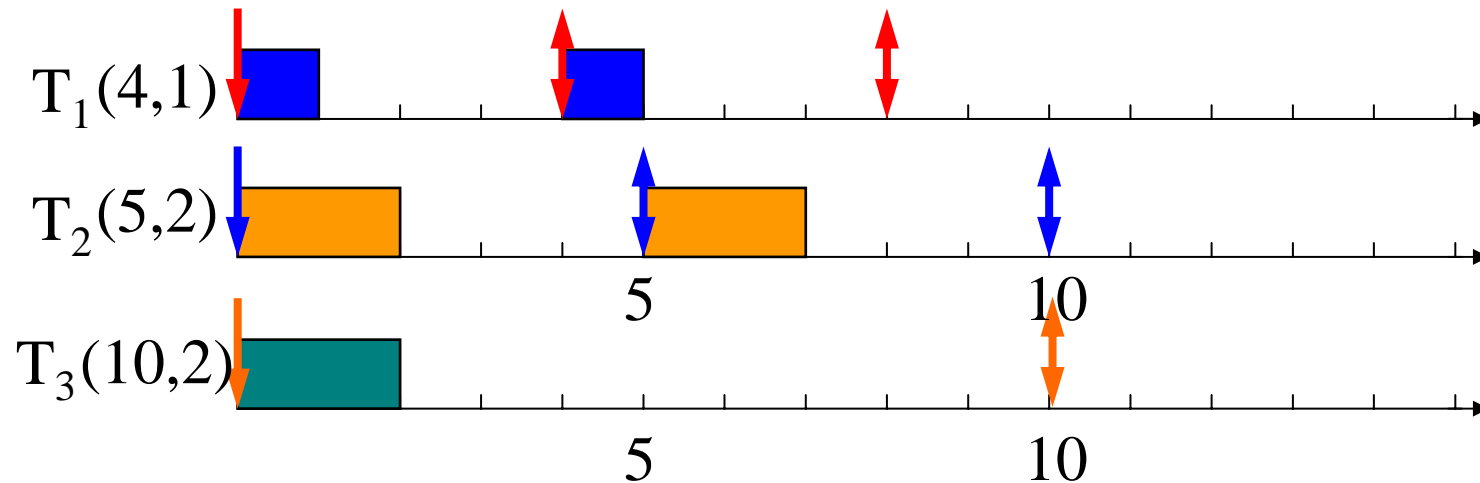


# Response Time

- Response Time ( $r_i$ ) [Audsley et al., 1993]

$$r_i = e_i + \sum_{T_k \in HP(T_i)} \left\lceil \frac{r_i}{p_k} \right\rceil \cdot e_k$$

- $HP(T_i)$ : a set of higher-priority tasks than  $T_i$



# RM - Schedulability Analysis

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- Real-time system is schedulable under RM  
if and only if  $r_i \leq p_i$  for all task  $T_i(p_i, e_i)$

Joseph & Pandya,

“Finding response times in a real-time system”,

The Computer Journal, 1986.

# RM – Utilization Bound

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- Real-time system is schedulable under RM if

$$\sum U_i \leq n (2^{1/n} - 1)$$

Liu & Layland,

“Scheduling algorithms for multi-programming in a hard-real-time environment”, *Journal of ACM*, 1973.

# RM – Utilization Bound

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- Real-time system is schedulable under RM if

$$\sum U_i \leq n (2^{1/n} - 1)$$

- Example:  $T_1(4,1)$ ,  $T_2(5,1)$ ,  $T_3(10,1)$ ,

$$\begin{aligned}\sum U_i &= 1/4 + 1/5 + 1/10 \\ &= 0.55\end{aligned}$$

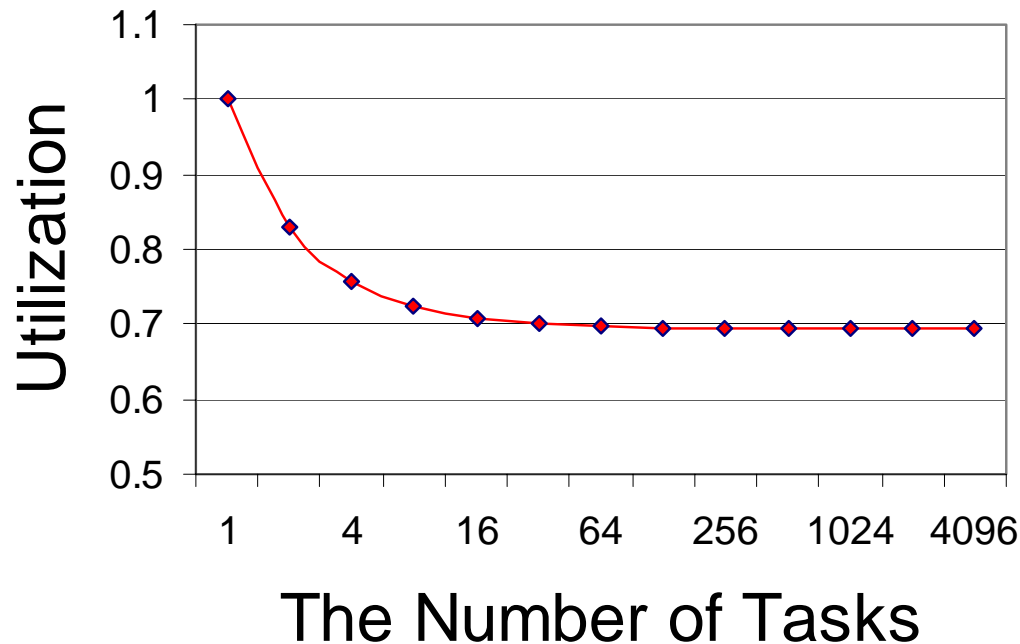
$$3 (2^{1/3} - 1) \approx 0.78$$

Thus,  $\{T_1, T_2, T_3\}$  is schedulable under RM.

# RM – Utilization Bound

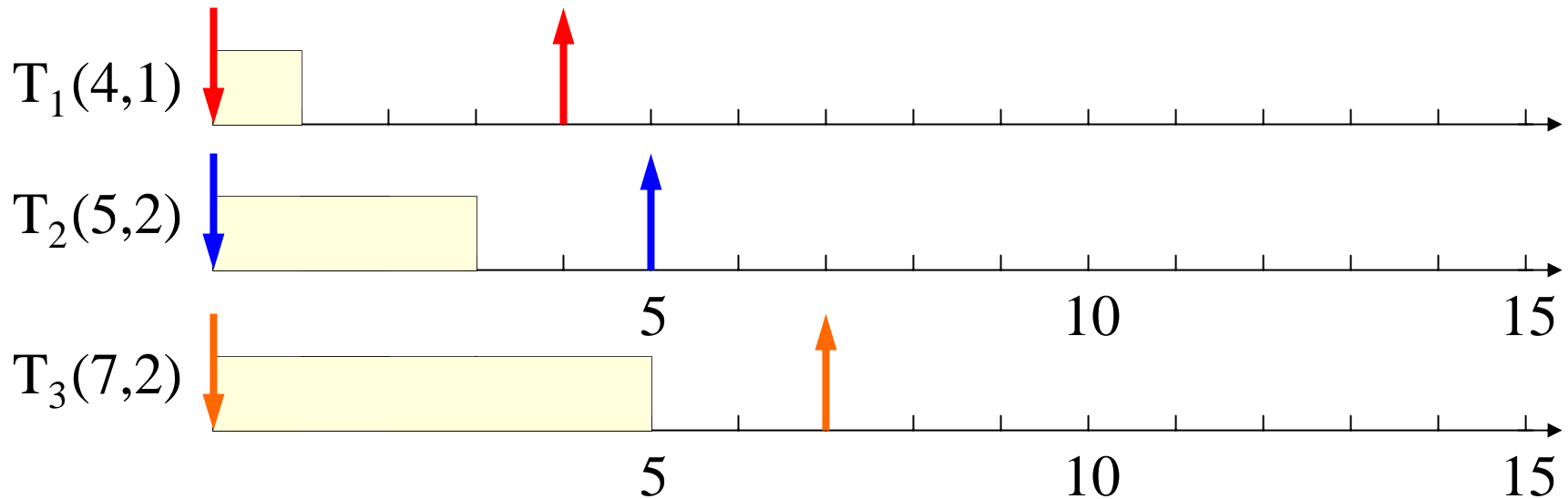
- Real-time system is schedulable under RM if  $\sum U_i \leq n (2^{1/n} - 1)$

## RM Utilization Bounds



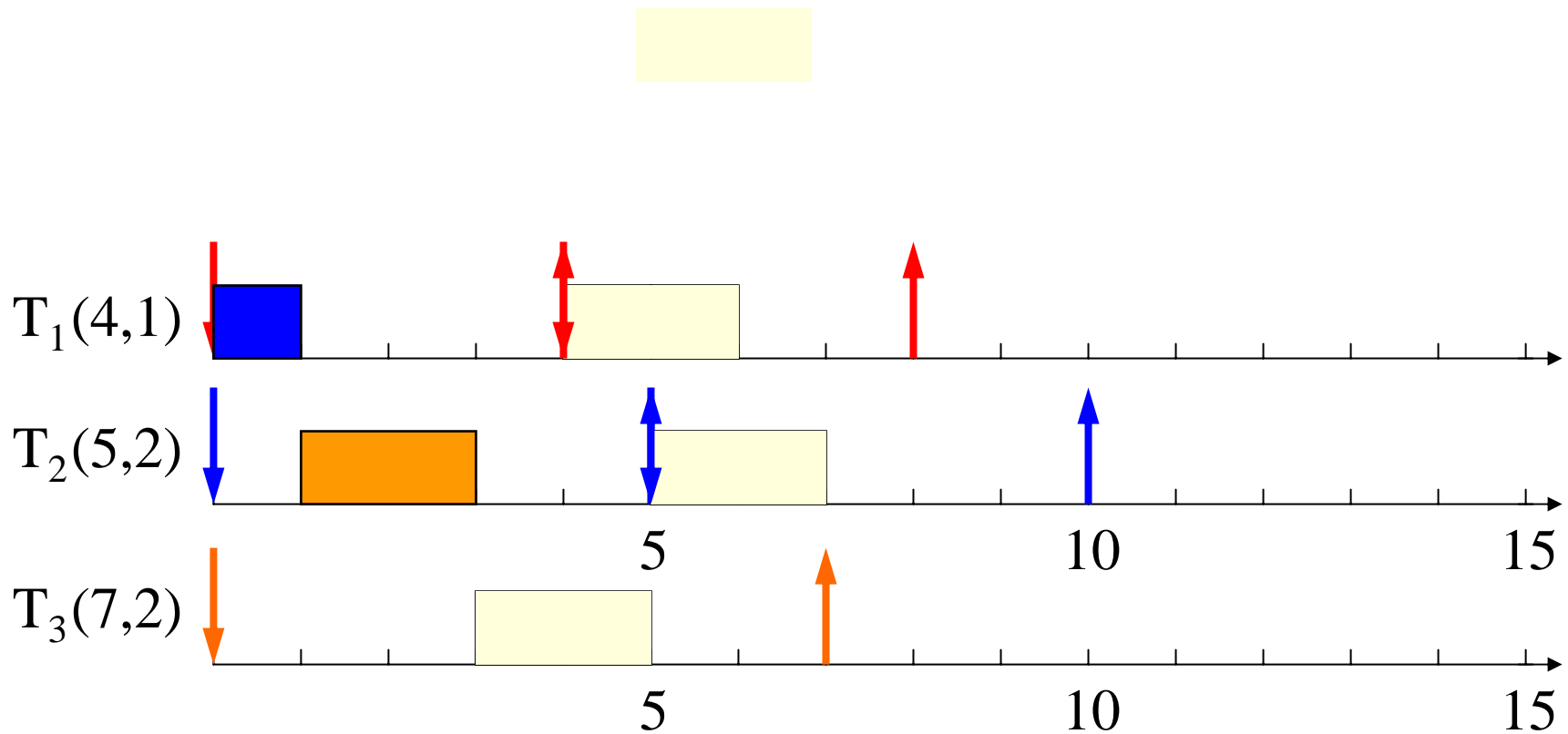
# EDF (Earliest Deadline First)

- Optimal dynamic priority scheduling
- A task with a shorter deadline has a higher priority
- Executes a job with the earliest deadline



# EDF (Earliest Deadline First)

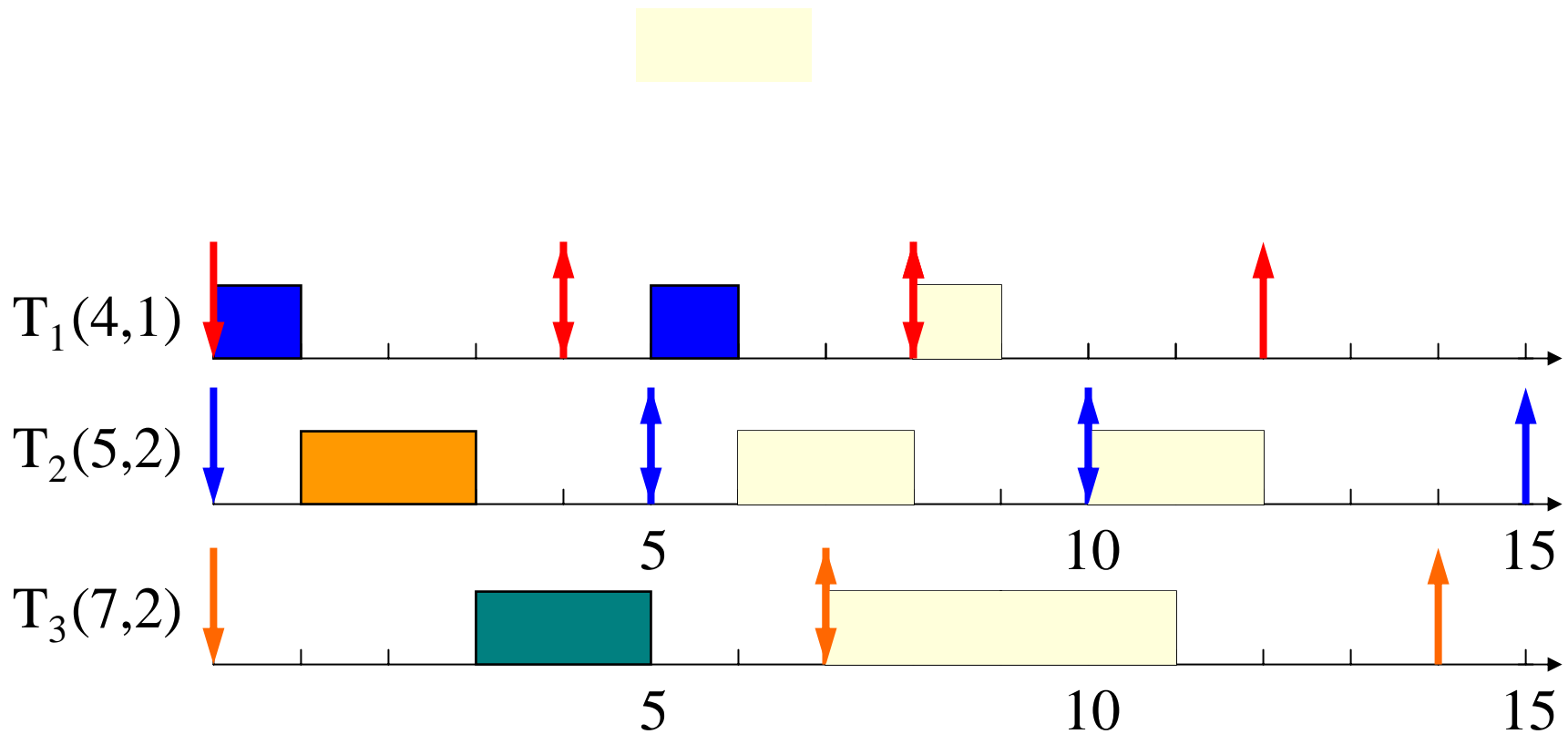
- Executes a job with the earliest deadline





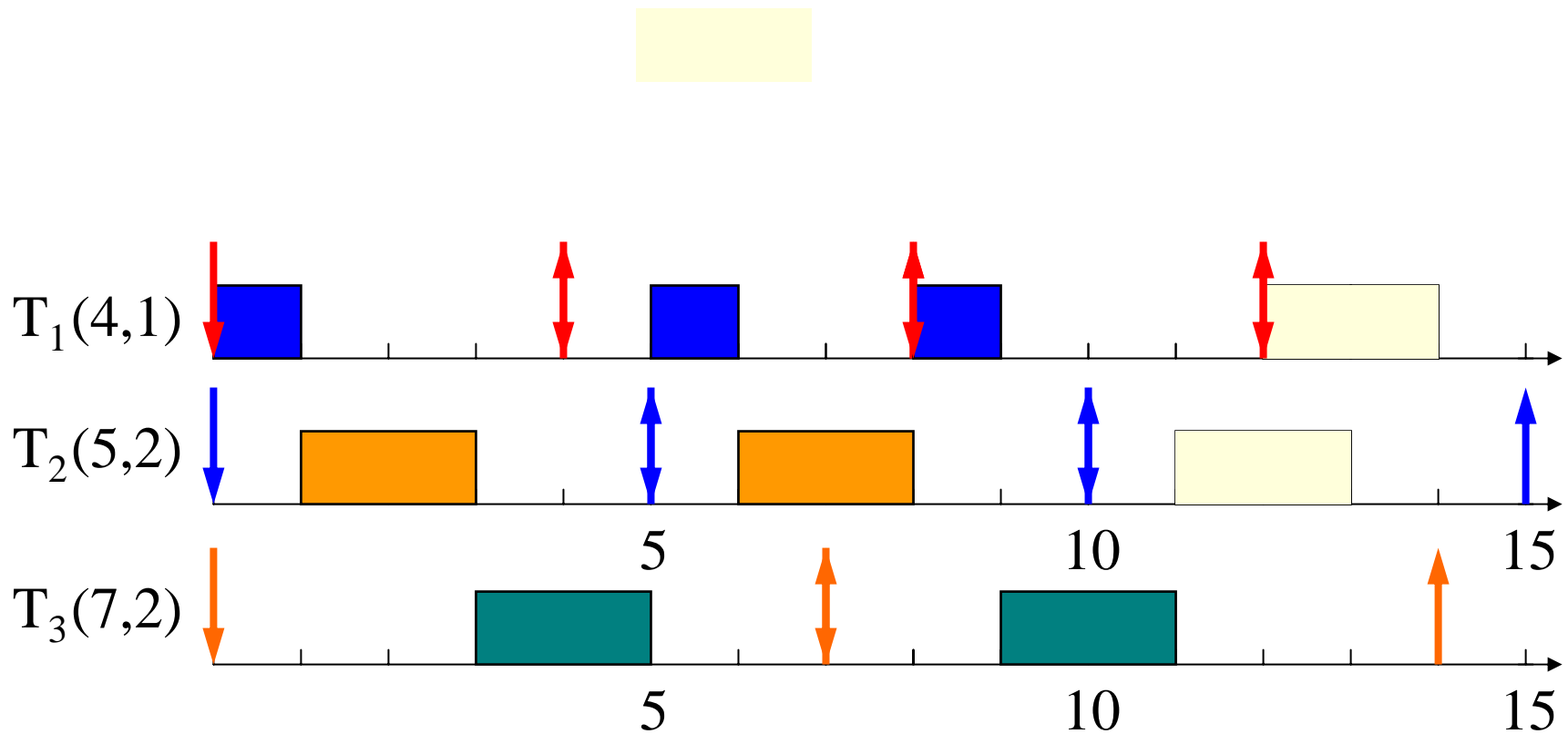
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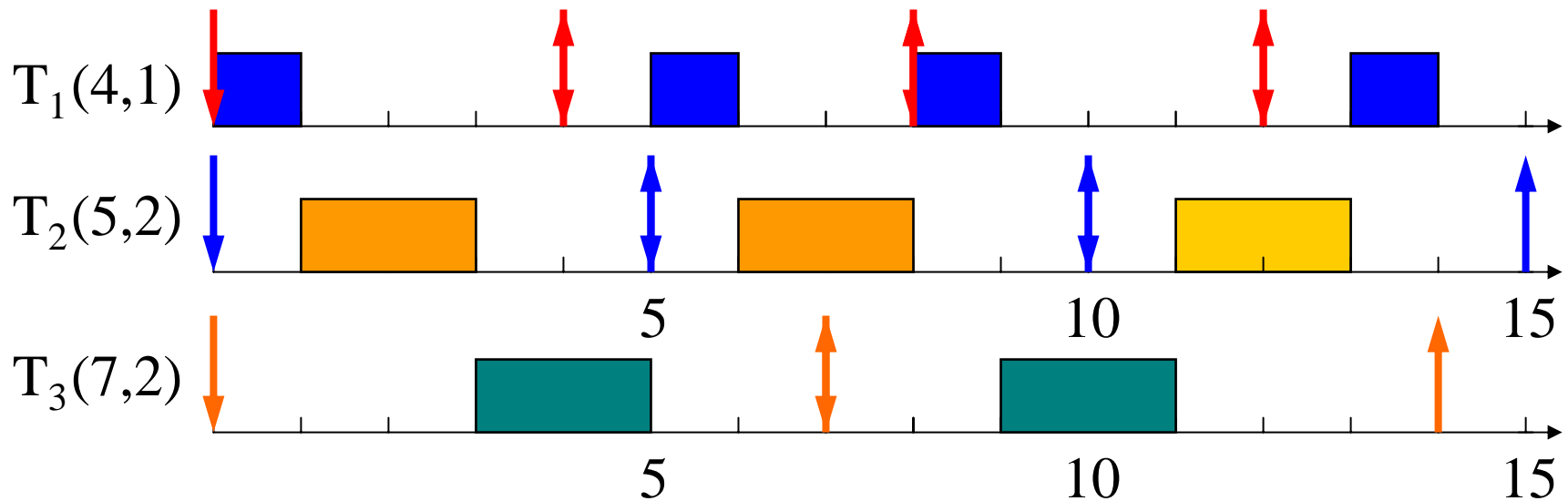
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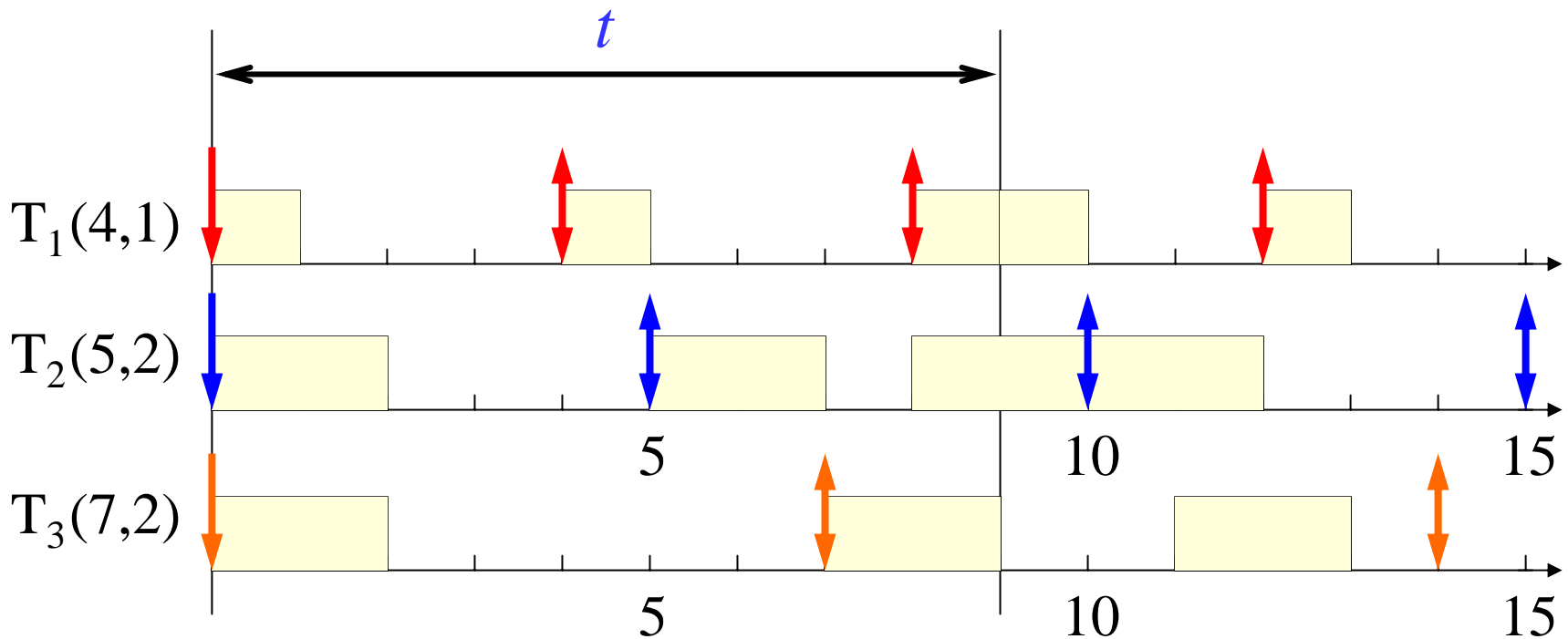
# EDF (Earliest Deadline First)

- Optimal scheduling algorithm
  - if there is a schedule for a set of real-time tasks, EDF can schedule it.



# Processor Demand Bound

- Demand Bound Function :  $dbf(t)$ 
  - the **maximum processor demand** by workload over any interval of length  $t$



# EDF - Schedulability Analysis

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- Real-time system is schedulable under EDF if and only if  $dbf(t) \leq t$  for all interval  $t$

Baruah et al.

“Algorithms and complexity concerning the preemptive scheduling of periodic, real-time tasks on one processor”, Journal of Real-Time Systems, 1990.

- Demand Bound Function :  $dbf(t)$ 
  - the **maximum processor demand** by workload over any interval of length  $t$

# EDF – Utilization Bound

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- Real-time system is schedulable under EDF if and only if

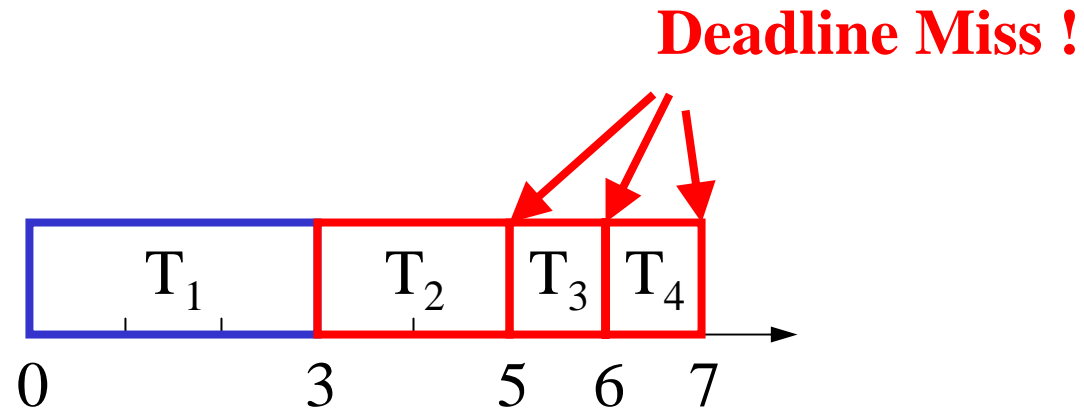
$$\sum U_i \leq 1$$

Liu & Layland,

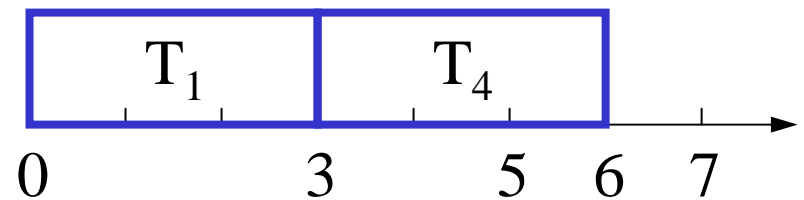
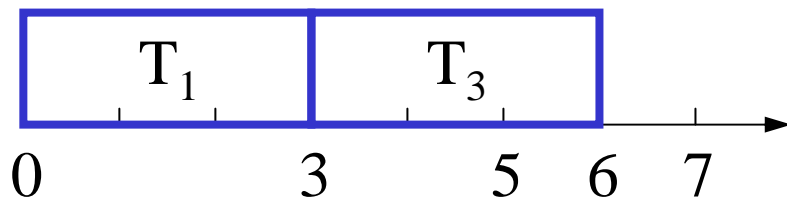
“Scheduling algorithms for multi-programming in a hard-real-time environment”, *Journal of ACM*, 1973.

# EDF – Overload Conditions

- Domino effect during overload conditions
  - Example:  $T_1(4,3)$ ,  $T_2(5,3)$ ,  $T_3(6,3)$ ,  $T_4(7,3)$



Better schedules :



# RM vs. EDF

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- Rate Monotonic
  - Simpler implementation, even in systems without explicit support for timing constraints (periods, deadlines)
  - Predictability for the highest priority tasks
- EDF
  - Full processor utilization
  - Misbehavior during overload conditions
- For more details: Buttazzo, “Rate monotonic vs. EDF: Judgement Day”, EMSOFT 2003.